

Mechanical ExpressionsTM Manual

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Getting Started

Need Help?

There are many ways to get help with *Mechanical Expressions*.

In both the PDF manual document and the embedded Help system you can:

- Use the table of contents to get details on using a tool, an icon or a menu.
- Use the index for help on a particular topic, such as "parametric equations".

Inside the *Mechanical Expressions* Help system you can:

- Use the Search tool to find all topics based on a key word, such as "constraints".
- Browse through help with the up - "Previous page", and down - "Next Page" arrows . This will step you through the help subtopics in a logical sequence.
- You can click on [colored text](#) which links you to more information.

Tool Tips:

When you move the cursor over any icon on the screen, the name of the icon appears briefly below the cursor.

Linked Text

Some words in the program's **Help** system are highlighted and underlined. When you place the cursor over this text, the cursor becomes the hand symbol. This text indicates a [link](#) to more information on the subject. Click the text to jump to the related help page.



The Display and How It's Organized

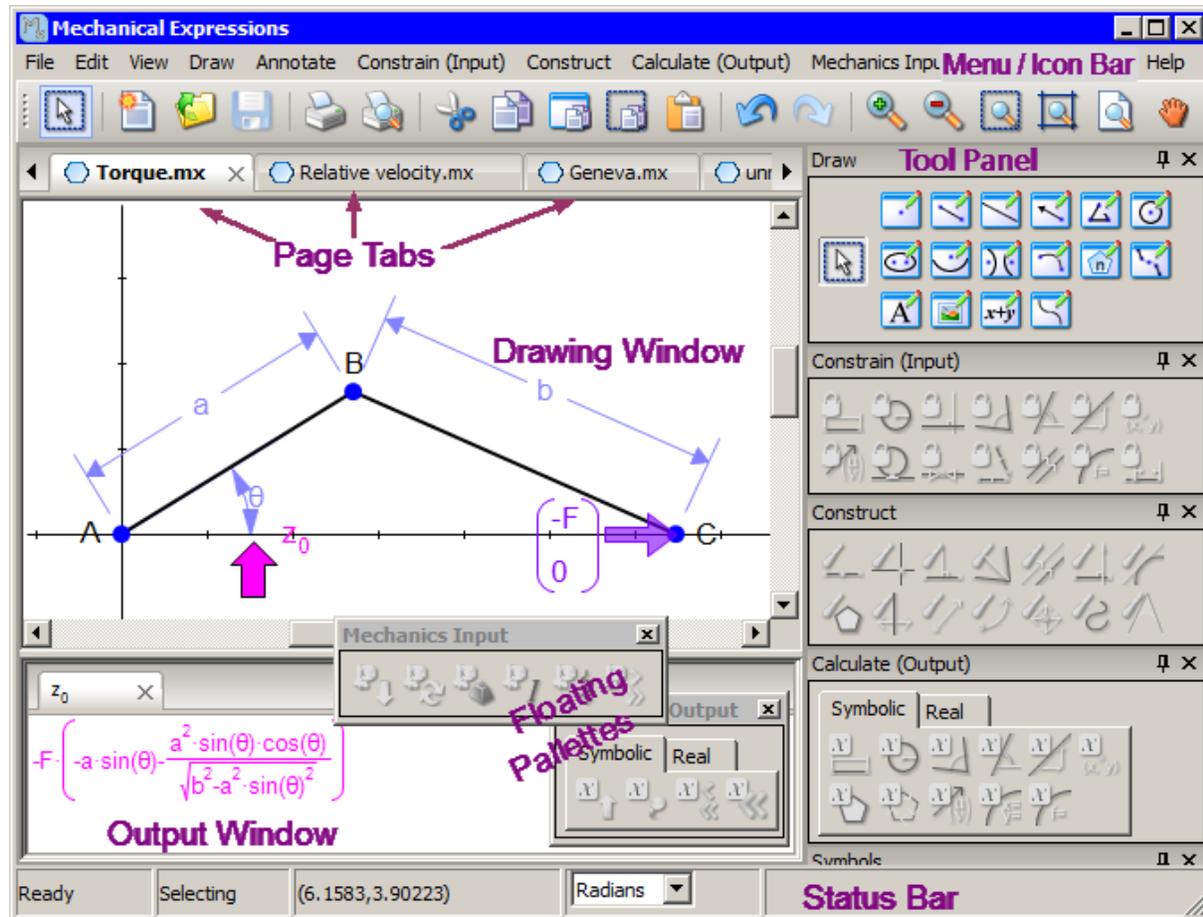
Many of the menu items in the drop down menu bar at the top of the screen correspond to one of the icons or buttons across the top of the display window or in one of the toolboxes.

Icons across the top of the screen comprise the standard Windows **File**, **Edit**, **View** and **Help** commands. The construction and calculation tools are displayed along the side of the drawing window. These toolboxes can be displayed on the [left or right panel, top or bottom panel, floating in a separate window, or hidden](#).

The output window can be displayed below the drawing window to show large expressions.

The [status bar](#) at the bottom of the window displays the following (from left to right):

<Menu Help> <Current Mode> <Cursor Coordinates> <Angle Mode>



The Status Bar

The status bar at the bottom of the screen prompts the following information (from left to right):



- **Menu Help** - summary of a selected menu item.
- **Current Mode** - Each icon in the drawing toolbox represents a mode. Tools requiring additional inputs after clicking the tool will display further prompts in this field.
- **Cursor Coordinates** - Displays the current coordinates of the cursor in the diagram.
- **Angle Mode** - A drop down window for conveniently changing from Radians to Degrees and *visa versa*. This default can also be changed in the [Preferences](#) dialog - **Edit / Preferences / Math**.



Customizing Your Display

You can arrange the display as it suits you.

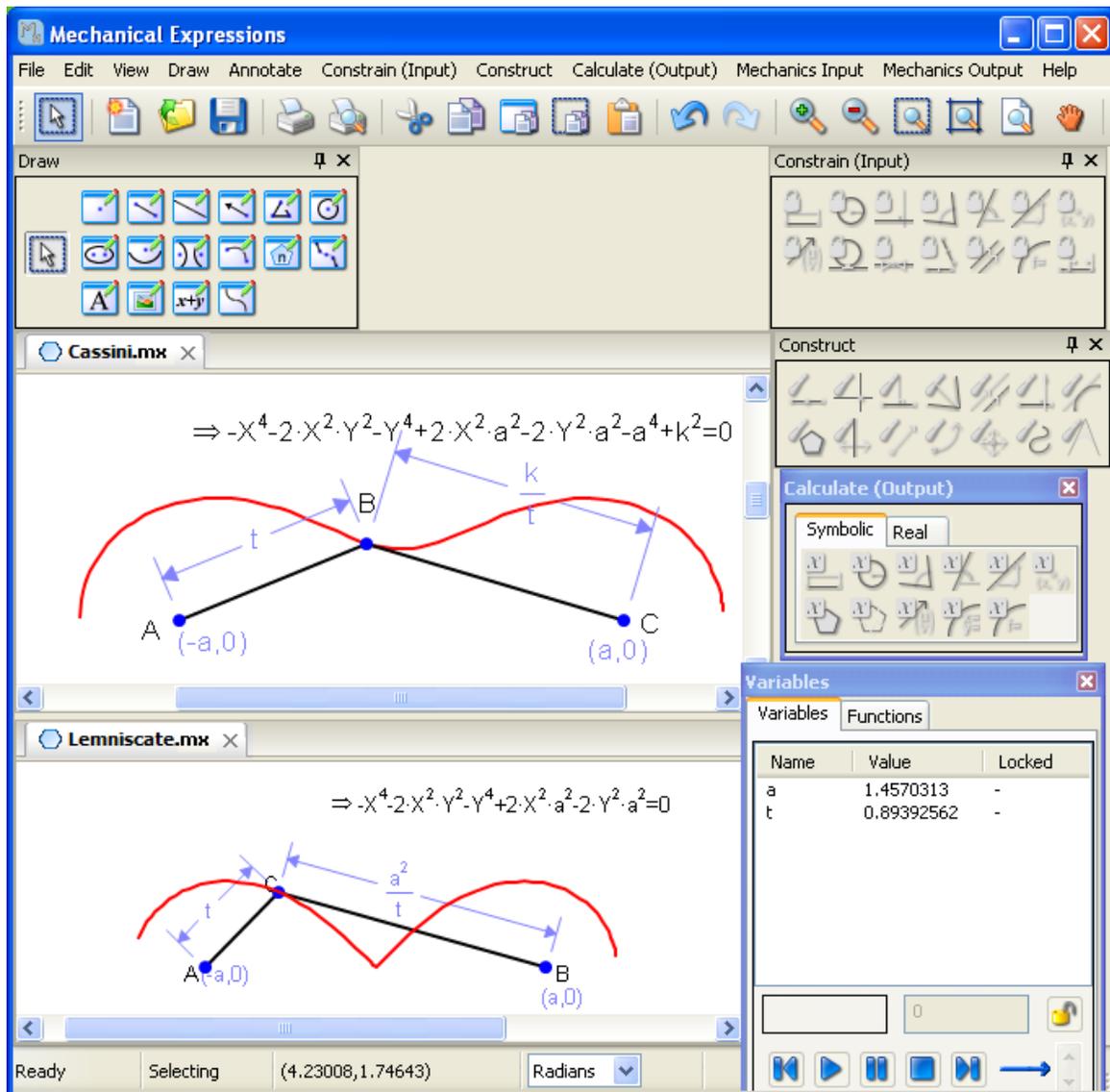
[Arranging Toolboxes](#) - Anchored or floating toolboxes can be placed around the drawing window.

[Hide / Show Toolboxes](#) - You may want to hide toolboxes which you rarely use.

[Saving your configuration](#) - Use the **View / Tool Panel Configurations**.

[Arranging projects](#) - You can open multiple project files and arrange them in the drawing window using the page tabs.

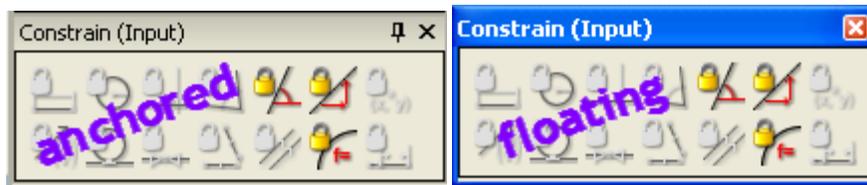
In the example below three toolboxes (**Draw**, **Constrain (Input)**, and **Construct**) are anchored, four (**Calculate (Output)**, **Variables**, **Mechanics Input** and **Mechanics Output**) are floating, and three (**Annotate**, **Symbols** and **Annotation Symbols**) are hidden. Two slightly different locus examples are displayed for comparison.



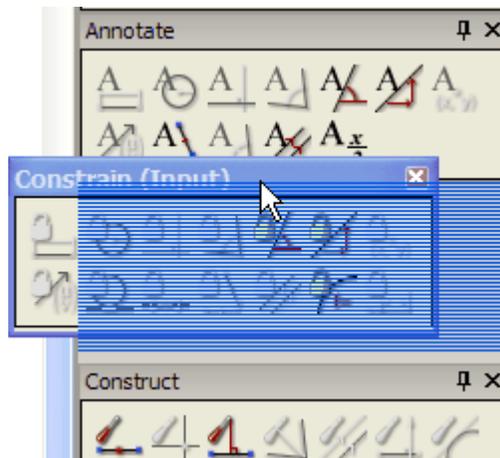
Arranging Toolboxes

You can move the toolboxes around the periphery of the drawing window by clicking the title bar and dragging.

Click the pushpin on the upper right corner of individual toolboxes to make it a "floating" box that you can drag anyplace on the screen. Floating boxes have a colored title bar -

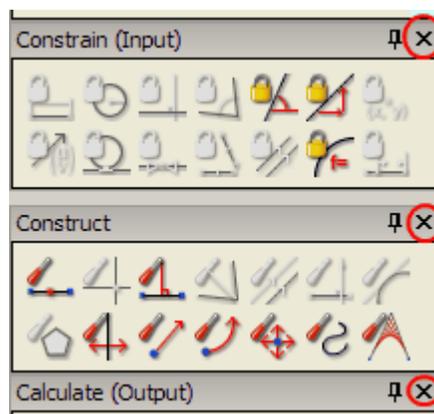


To re-anchor the toolbox, drag the box until a blue shadow appears at the position where you want it, then release the mouse button. You may want to readjust the screen size for optimal viewing.



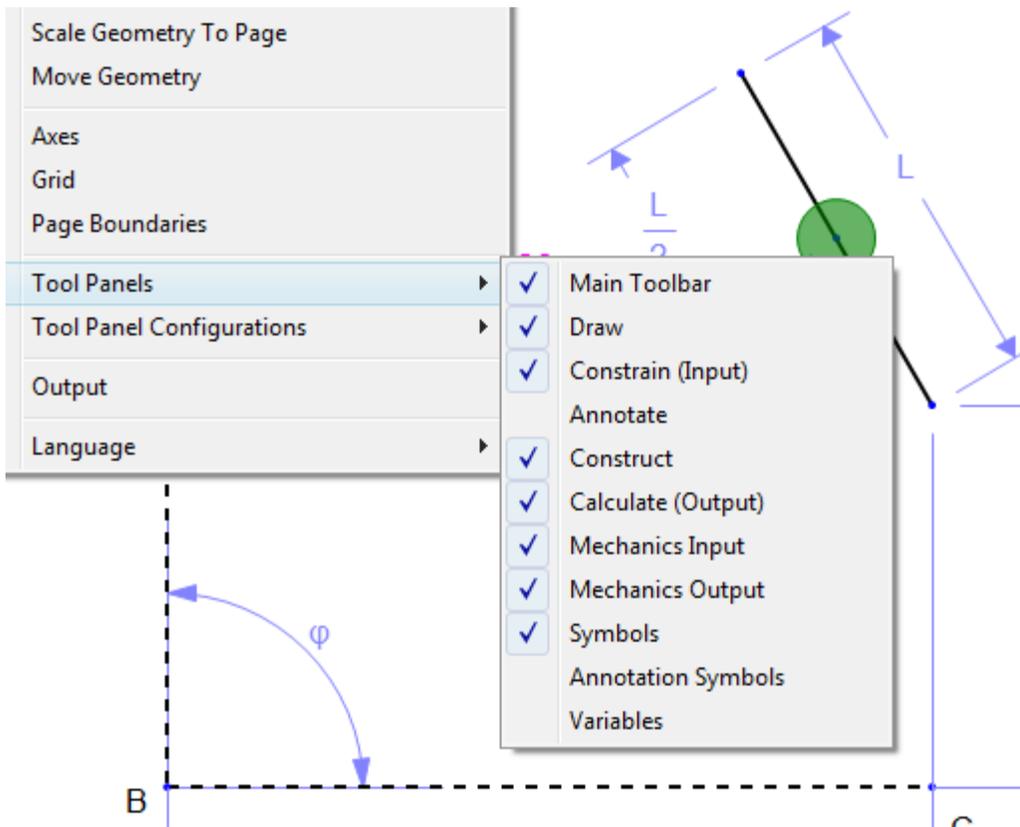
Hiding / Showing Toolboxes

Use the X on the upper right corner of individual toolboxes to hide them.



To display a hidden toolbox, select **View / Tool Panels**. The submenu lists the toolboxes and the **Main Toolbar** (the icon strip at the top of the window). Boxes shown are preceded by a check, those without a check are

hidden.



Click a toolbox name to change its state.

Saving the Configuration

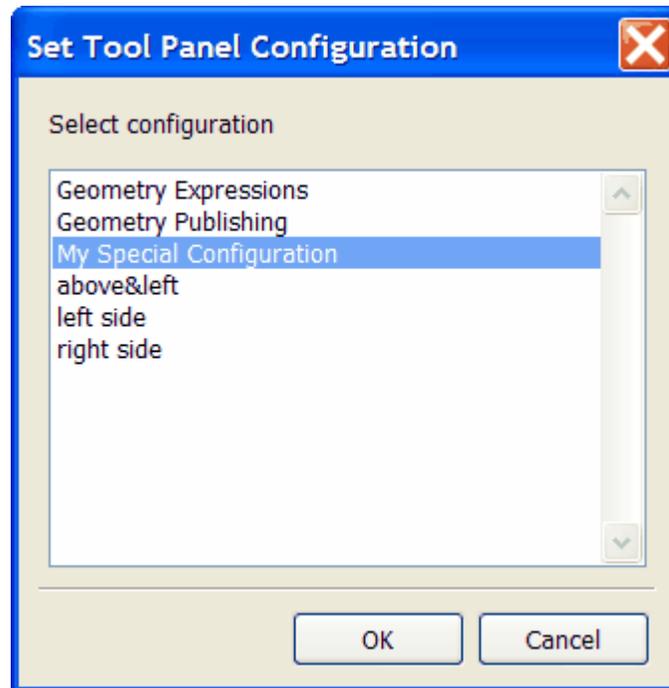
After configuring the screen to your preference, you can save this arrangement in case it gets messed up, or perhaps you need the tools arranged differently for different projects. This is easy with the **View / Tool Panel Configurations** menu selection. You can give a name to an arrangement of the toolbars. Several configurations can be saved in a list and referred to as needed.



Add - to save the current screen configuration. You will be prompted for a name to reference this configuration.

Delete - if you no longer will use a certain configuration you can delete it from your list.

Set - to change a configuration which you have saved, simply select the configuration name from your list. Check out the configurations that come with the program.

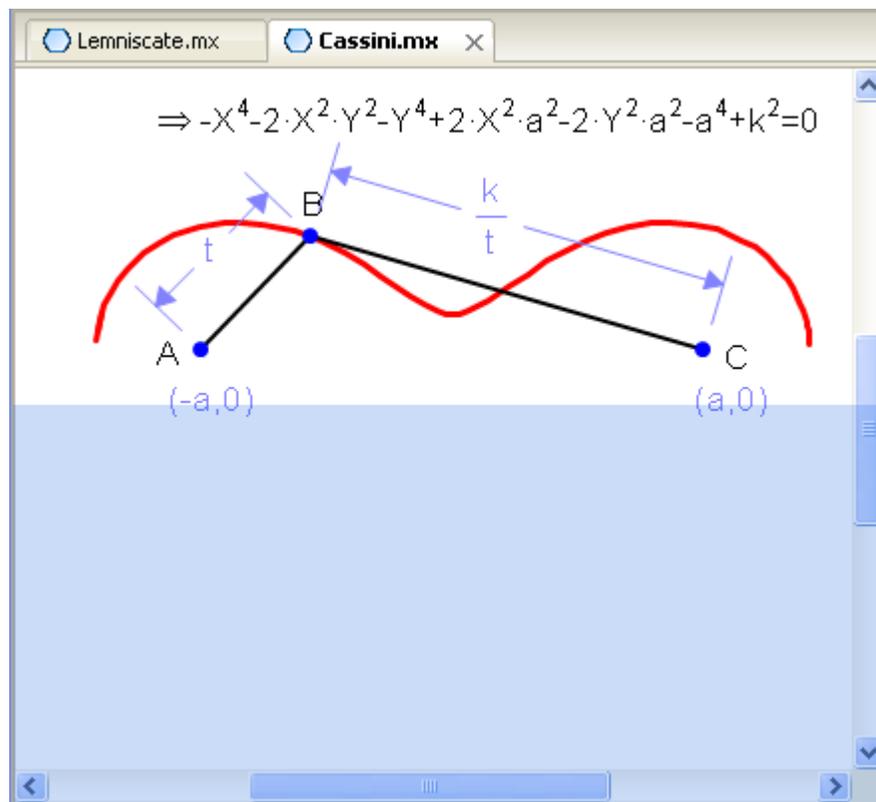


Default - reset tool panels back to the default configuration.

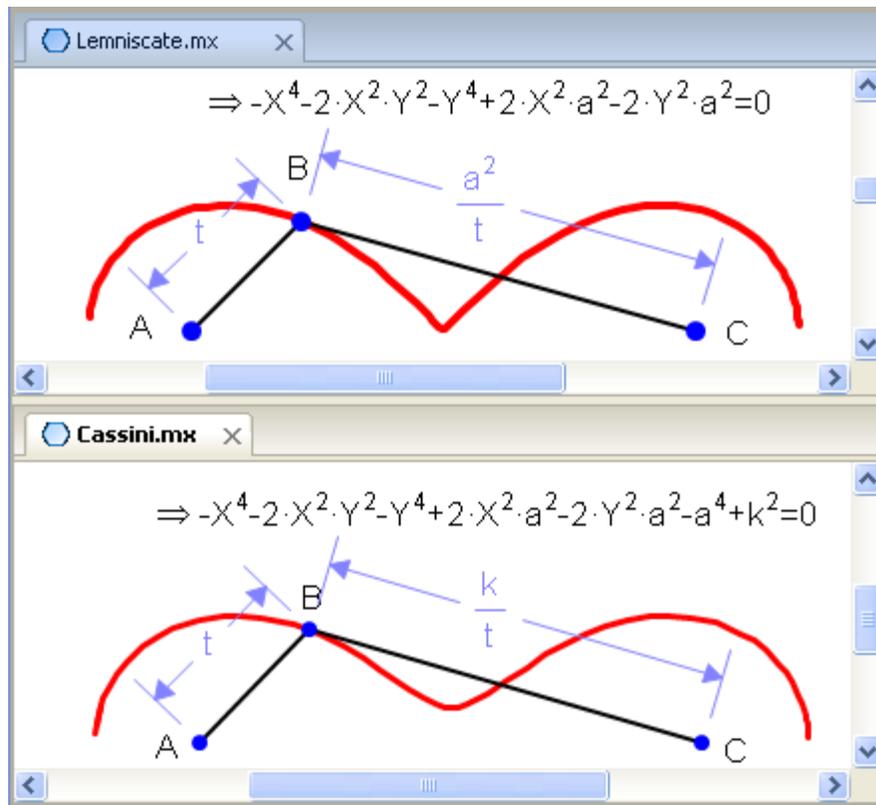
Arranging Project Pages

You can open multiple project files for quick reference. By default files are overlaid. Click a page tab to bring a file to the top.

Comparing drawings side by side - click the page tab and drag it to one side, top, or bottom of the window. A shadow of the drawing gives you an indication of how the drawings will be arranged before you release the mouse button.



Returning to overlaid configuration - drag one tab and position it over the other tab. The shadow will appear only on the title bar, then release the mouse button.



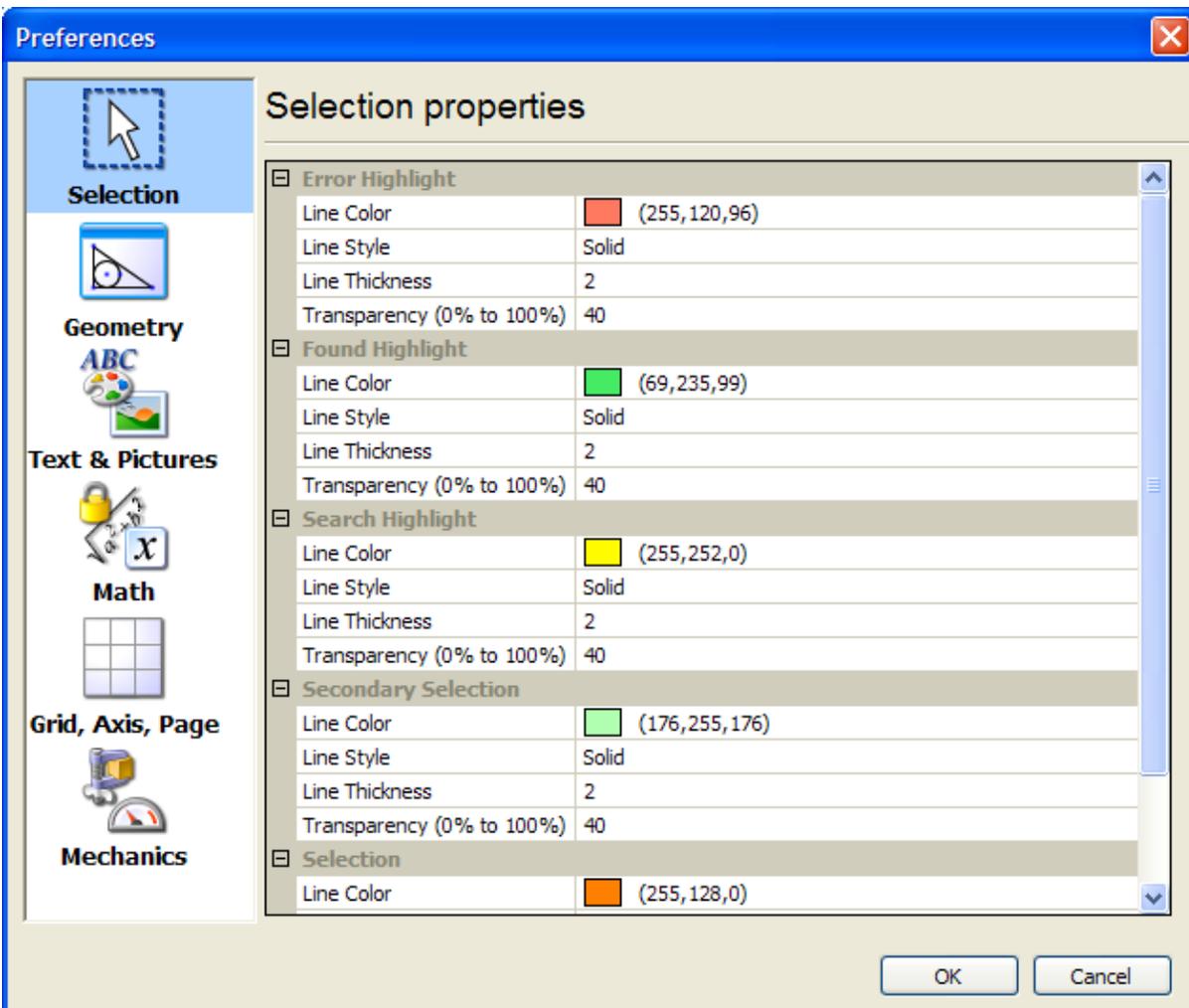


Adjusting the Default Settings

Select **Preferences** from the **Edit** menu (or in the Mac version, **Mechanical Expressions / Preferences...**) to modify the program's general defaults. Mechanics defaults are set separately under [Edit / Mechanics Environment](#).

The default settings are grouped by type, listed on the left side of the **Preferences** dialog. Click the icon to display the desired page.

These settings are also available for editing a selected object or group of objects individually without changing the defaults, using the [Selection Context Menu](#).

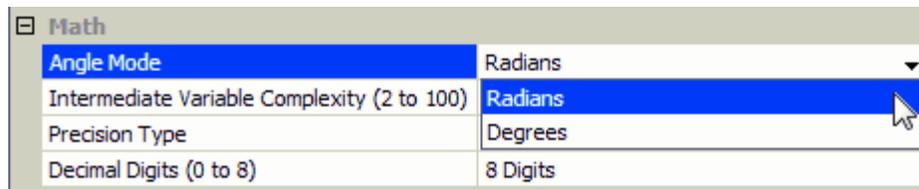


 Selection	set the line color and style for each selection type.
 Geometry	set font related properties for labels; color and size / style for other geometric elements.
 Text & Pictures	set font properties for text, the rotation angle and the transparency level of an inserted picture, and the <u>Pinned</u> state for Text and Pictures . Pinned Text and Pictures will not move relative to the Page Boundaries as the result of a <u>Scale</u> operation.
 Math	set the properties for alphanumeric input and output; mathematical calculation defaults.
 Grid, Axis, Page	set properties of the Major and Minor Grid, the coordinate Axes, the drawing's background color, and the Page Boundary lines.
 Mechanics	set font related properties for mechanics <u>input</u> and <u>output</u> expressions; color and size / style for other mechanics elements.

To see the possible values for each property, click the row. An icon will appear at the right end of the row (except the Point Size selection under the Font property -you can enter the point size directly).

<input type="checkbox"/> Math	
Angle Mode	Radians
Intermediate Variable Complexity (2 to 100)	15
Precision Type	Significant Figures
Decimal Digits (0 to 8)	8 Digits

Click the icon to display the selection dialog  or drop-down menu of choices .



Changing a default for a type of drawing entity will apply to all entities of that type except ones whose properties have been individually set, by selecting it and then choosing **Edit / Properties** or right clicking **All Properties** from the **Selection Context** menu. Likewise, text, pictures

or expressions that were individually pinned  or unpinned

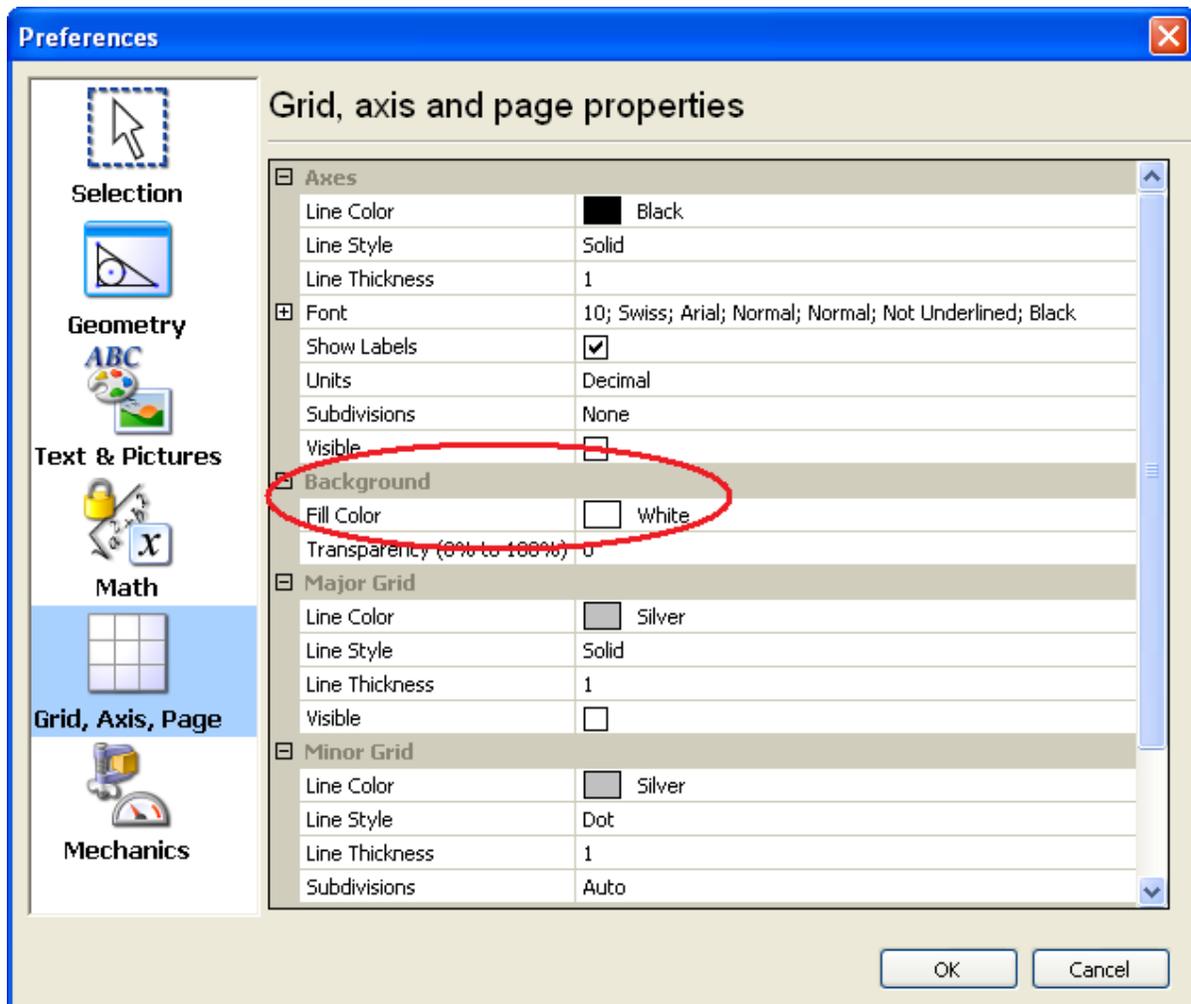


will not be affected by changes to the default Pinned settings.

Changing Background Color

You can now change the drawing's background color to something other than white with the following steps:

1. Select **Edit / Preferences...** (or in the Mac version, **Mechanical Expressions / Preferences...**)
2. Click the **Grid, Axis, Page** tab
3. Change the Fill Color in the **Background** section. The color will be applied to all pages.

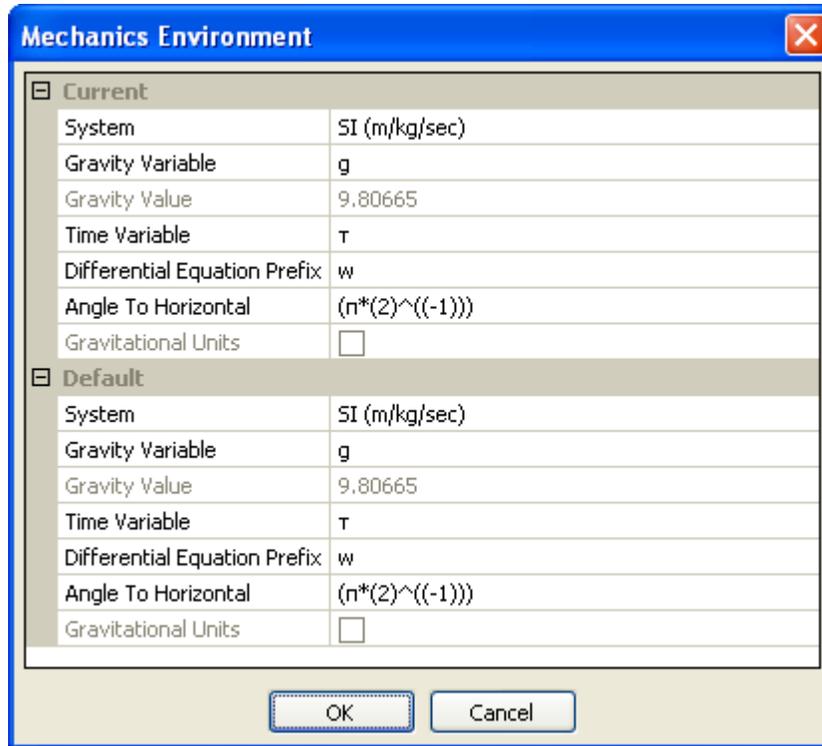


You can change the drawing's background color for a particular file by open the file, right click on the screen (without anything highlighted), then select "Display Properties...", and then change the color.



Setting the Mechanics Environment

To set the **Mechanics Environment** defaults select **Edit / Mechanics Environment**.



System - Choices for the system units are:

- SI (m/kg/sec)
- CGS (cm/kg/sec)
- FPS (ft/lbs/sec)
- IPS (in/lbs/sec)
- Custom - set the **Gravity Value** and the **Gravitational Units** check box.

To select the **System** units, click the row and the arrow icon  to display the drop down menu of choices.

To change any of the following entries, select the value and retype it.

Gravity Variable - g is a reserved word for the gravitational constant (unless you replace it with another symbol). Do not use this symbol for

any other variable.

Gravity Value - set to the gravitational constant (9.8, or a value you can change if you are working in Custom System units)

Time Variable - τ (tau) is a reserved word for time (unless you replace it with another symbol). Do not use this symbol for any other variable.

By default τ is set to 0. You can change this value in the [Variables](#) toolbox.

Differential Equation Prefix - choose a prefix for the equations of motion for the [Differential Equations](#) function provided in the [Mechanics Output](#) menu.

Angle To Horizontal - the default is $\pi/2$, viewing the model from the side with gravity acting straight down. A horizontal model, (angle 0 to horizontal), would view the model from the top and have no gravitational force.

Gravitational Units - when working with standard system units, this selection is grayed and the check box is set by the system: checked when working with weight units (FPS and IPS), cleared when working in mass units (SI and CGS). You can change the entry when working in Custom units.



File Handling

Mechanical Expressions uses standard Windows file **Open** and **Save** operations. Save your files regularly with the handy  icon at the top of the screen.

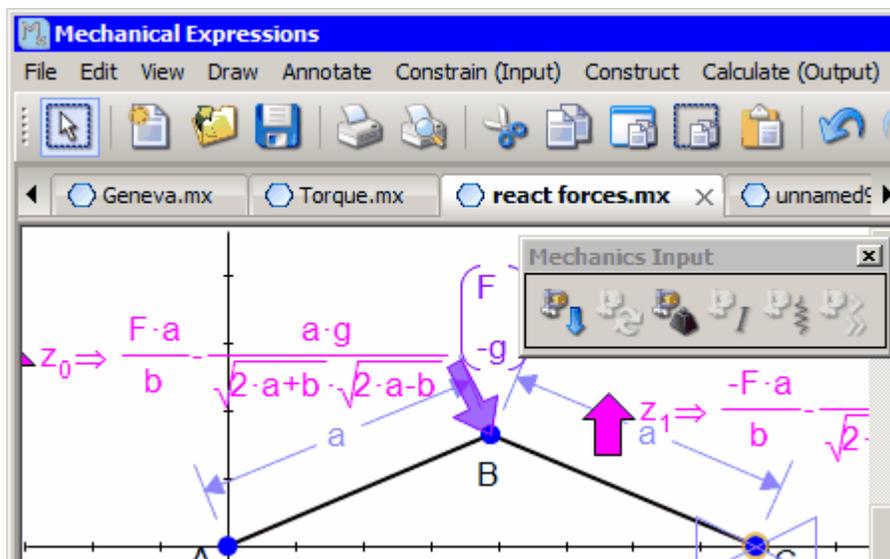
The data files generated from your drawings will have the extension ".mx".

You may create multiple data files and have them open in a session. By default, each file is on separate page with the tabs across the top of the drawing window. Click the tab to view the file.

If you are preparing a multi-paged lesson, you can save the pages together as a **Workbook**, with the file extension ".mxw". This is a completely separate file from the .mx files.

The **Open / Save (As) / Close** [Workbook file selections](#) apply only to the workbook.  and the **File / Save** commands will NOT save the workbook files. They only affect the individual .mx files.

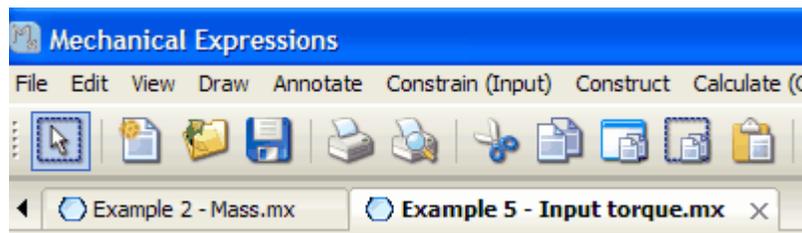
Files can also be [arranged for comparison viewing](#).



Workbooks and Individual .mx Files

Workbooks are a handy way of putting lessons together.

- You can make a workbook by opening new tabs (**File / New**).
- You can **Open** .mx files that you have already created to make them part of your workbook.
- You can create pages from a combination of the above.



When all of the pages are together on the page tab bar, select **Save Workbook (As)** from the file menu.

 Note: saving the workbook does NOT update any of the individual .mx files displayed in the workbook, since the workbook file is an entirely separate file (.mxw). If you want to keep the individual .mx file up to date with the workbook page, you must use the regular **File / Save** for each page / file. But, if you forget, you can always save it from the workbook at any time.

Likewise, saving an individual page, **File / Save**, of an open workbook does NOT update the workbook file (.mxw). However, if you forget to save the workbook, but save a page (.mx), you can always open the .mx file again from your open workbook file and resave the workbook.

If you don't want to keep individual copies of all your workbook pages, then you just have to remember to use the **Save Workbook** file selection.

However, to give the workbook pages custom names (instead of unnamed7.mx), you must save the individual page (for example, Lesson 1 Ellipse.mx) at least once. After the first time, you don't need to continue to save the .mx file.

Only one workbook file can be open at a time. If you open a workbook file

while other individual files or another workbook file is open, they will be closed, after, of course, prompting you to save them if you have made changes.



MathML

All mathematical expressions in *Mechanical Expressions* are written in *MathML*, so you can copy and paste directly to or from any other *MathML* program.

Usually the standard **Edit / Copy** or Ctrl-C command should work. If this doesn't give you the desired result, try the **Edit / Copy As** command. Select from the submenu of choices appropriate to your application.

If you copy an expression that uses [Intermediate Variables](#), the algebra system will create a function from the pasted expression.

To **Paste** math into *Mechanical Expressions* it must be *Content MathML*.

- *Maple* creates *Content MathML* by default.
- To create *Content MathML* in *Mathematica v6.0*, execute the following commands:

```
SetOptions[XML`MathML`ExpressionToMathML, "NamespacePrefixes"
> {}, "Formats" > {"ContentMathML"}]
```

```
SetOptions[XML`MathML`BoxesToMathML, "NamespacePrefixes" > {},
"Formats" > {"ContentMathML"}]
```

```
SetOptions[Export, ConversionOptions > {"NamespacePrefixes" > {}},
"Formats" > {"ContentMathML"}]
```

```
SetOptions[ExportString, ConversionOptions > {"NamespacePrefixes"
> {}}, "Formats" > {"ContentMathML"}]
```

- To create *Content MathML* in *Mathematica v7.0* or higher, execute the following commands

```
ExportString[expression, "MathML", "Presentation"-> False, "Content"
-> True]
```

Then copy the content *MathML* representation (the exported mathematical expression) as Plain Text and paste it into *Mechanical Expressions*.



Some Opening Examples

Your installation comes with several examples - look in the **Examples** subdirectory. For step by step instructions through some example sets, see *Mechanical Expressions Examples.pdf* which can be found under the **Doc** subdirectory in your *Mx* installation.

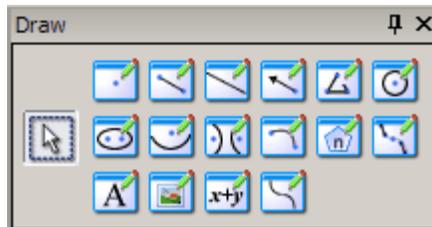


Tools

Drawing

Using the Drawing Tools

The **Draw** toolbox contains the drawing commands and the [Selection Arrow](#). The drawing commands can also be invoked from the **Draw** menu.



Unlike commands in the other toolboxes, Drawing commands are always available and require no pre-selection. Many of the commands are active until you change to a different one or press the Esc key or click the selection arrow , e.g. you can make multiple points until you select another tool or press esc. The selection mode, indicated by the selection arrow cursor, , is used for invoking all other commands. You can find the active command mode by noting which button is pressed or looking at the [current mode](#) on the status bar.



[Point](#)



[Line Segment](#)



[Infinite Line](#)



[Vector](#)



[Polygon](#)



[Circle](#)



[Ellipse](#)



[Parabola](#)



[Hyperbola](#)



[Arc](#)



[N-gon](#)



[Curve Approximation](#)



[Text](#)



[Picture](#)



[Expression](#)



[Function](#)

Before you start your drawing, select **Edit / Preferences / Geometry** to set various attributes, such as line color / style, fill color / style and transparency level, of the various drawing elements.

You can [change the attributes](#) of individual drawing elements by selecting them, right click the mouse, and choose **All Properties** from the context menu.

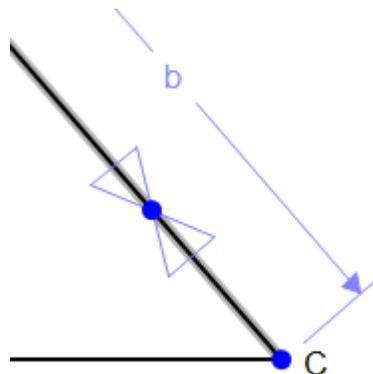
Adding a Point



To insert a point in your drawing, follow these steps:

1. Click the **Point** icon  in the **Drawing** toolbox or select **Point** from the **Draw** menu.
2. Move the crosshairs  into position.
3. Click the mouse to place the point under the crosshairs.

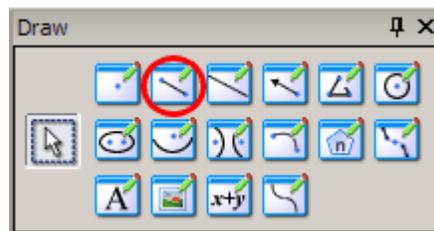
When the crosshairs are positioned over some geometry an incidence symbol (bowtie) is displayed around the point and the geometry is highlighted. A click of the mouse will create the point incident to the highlighted geometry.



Each point is displayed with a letter label. You can [change the label](#) from the [Select mode](#) .

Point is a modal command. You can continue making points until you choose the select arrow or another drawing tool.

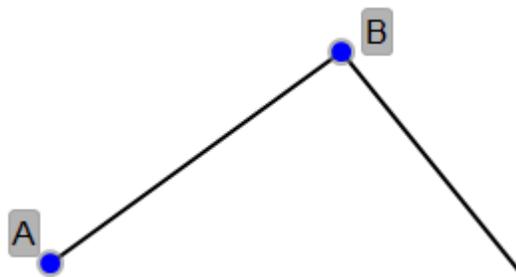
Adding Line Segments



To add line segments to your geometry follow these steps:

1. Click on the **Line Segment** icon  in the **Draw** toolbox or select **Line Segment** from the **Draw** menu.
2. Position the cursor  in the drawing window.
3. Click the mouse to place each endpoint.

Each line segment is displayed with a letter label for each endpoint.

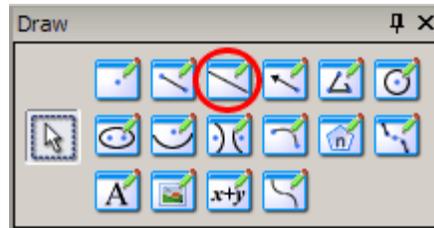


You can [change the label](#) from the [Select mode](#) .

To abort a line segment in the middle of the drawing operation, hit the "esc" key.

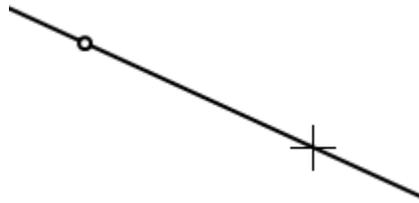
Line Segment is a modal command. You can continue making segments until you choose the select arrow or another drawing tool.

Drawing Lines



Lines are similar to line segments except they have infinite length.

1. Click the **Infinite Line** icon  in the **Draw** toolbox or select **Infinite Line** from the **Draw** menu.
2. Position the line cursor  in the drawing window.
3. Click the cursor to anchor the line at the cursor position. The anchor point will be displayed on the line.



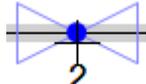
4. Move the cursor in the drawing window to position the line and click the cursor when you get the line in the desired orientation.

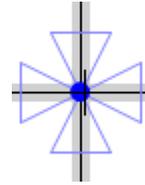
Lines are infinite and do not have points associated with them unless you specifically [place one](#) on the line.

Line is a modal command. You can continue making lines until you choose the select arrow or another drawing tool.

Active Axes -

The x and y axes have the properties of perpendicular infinite lines. When the crosshairs are positioned over an axis, the incidence symbol (bow tie)

is displayed at the intersection and the axis is highlighted.  When



the cursor is at the origin, both axes are highlighted . Points and End points of line segments can be placed directly on the axes without using the **Constrain / Incident** tool when the bow tie is displayed.

Drawing Vectors

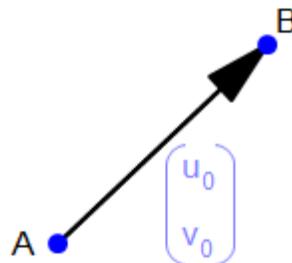


To add vectors to your geometry follow these steps:

1. Click the **Vector** icon  in the **Draw** toolbox or select **Vector** from the **Draw** menu.
2. Position the cursor  in the drawing window.
3. Click the mouse to place each endpoint.

Each vector is displayed with a letter label for each endpoint.

Drawing vectors is similar to drawing line segments, but vectors are [constrained with coefficients](#) of the form:



Vector is a modal command. You can continue making vectors until you choose the select arrow or another drawing tool.

Drawing Polygons



You can quickly create a multisided figure with these steps:

1. Click the **Polygon** icon  in the **Draw** toolbox or select **Polygon** from the **Draw** menu.
2. Position the cursor  in the drawing window.
3. Move the cursor and click once to place each vertex.
 - As you create the sides of the polygon, each vertex is automatically assigned a letter name. You can [change the label](#) in Select  mode.
 - When you create the last side of the polygon by clicking on the first vertex, the polygon will be filled with the default fill color, style and transparency.
 - To change the appearance of the polygon (color or style), select  it, right click, and choose **All Properties** from the context menu.
 - **Polygon** is a modal command. You can continue making polygons until you choose the select arrow or another drawing tool.

Polygons can be filled with the color, style, and transparency level of your choice. See the [Edit / Preferences](#) menu, **Geometry** tab to set the default. To change the color / style /transparency level of selected polygons, select the polygon(s), right-click, and select **All Properties** from the [Selection Context](#) menu (or **Edit / Properties** from the menu bar).

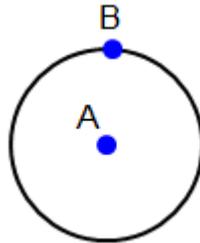
Drawing Circles



To add a circle to your diagram, follow these steps:

1. Click the **Circle** icon  in the **Draw** toolbox or select **Circle** from the **Draw** menu.
2. Move the cursor  in the drawing window to the position of the center of the circle and click once.
3. Move the cursor to draw the circle in the desired size and click again.

Notice the circle is displayed with 2 points, the center and a point on the perimeter.

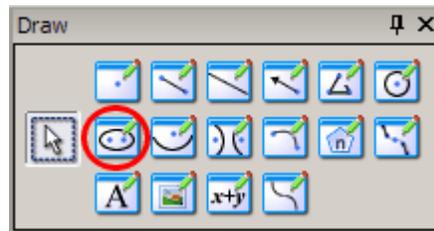


Circle is a modal command. You can continue making circles until you choose the select arrow or another drawing tool.

You can [adjust the circle](#) in Select  mode.

Circles can be filled with the color / transparency level of your choice. See the [Edit / Preferences](#) menu, **Geometry** tab to set the default. To change the color / transparency level of selected circles, select the circle (s), right-click, and select **All Properties** from the selection context menu (or **Edit / Properties** from the menu bar).

Drawing Ellipses



To create an ellipse in your diagram, follow these steps:

1. Click the **Ellipse** icon  in the **Draw** toolbox or select **Ellipse** from the **Draw** menu.
2. Move the cursor  in the drawing window to the position of one focal point. Click to place the first focus point. Move the cursor and click again to place the second focal point.
3. Then move the cursor to open the ellipse to the desired shape and click the mouse a third time.

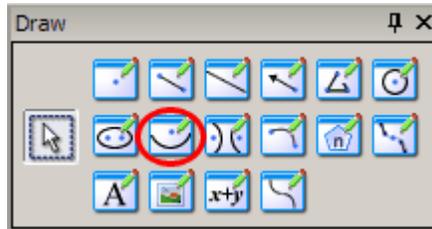


The ellipse will appear with three labeled points, the two foci and a point on the ellipse.

The **Ellipse** tool is a modal command. You can continue making ellipses until you choose the select arrow or another drawing tool.

Ellipses can be filled with the color / transparency level of your choice. See the [Edit / Preferences](#) menu, **Geometry** tab, Conic properties group to set the default. To change the color / transparency level of selected ellipses, select the ellipse(s), right-click, and select **All Properties** from the selection context menu (or **Edit / Properties** from the menu bar).

Drawing Parabolas

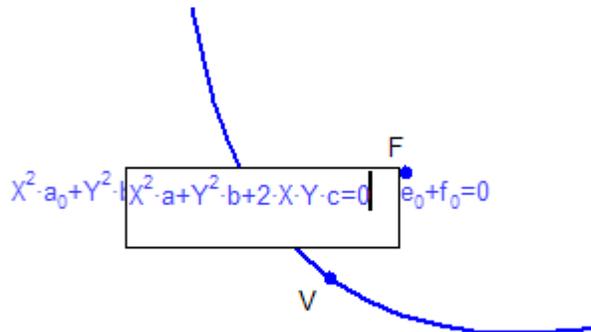


To create a parabola in your diagram, follow these steps:

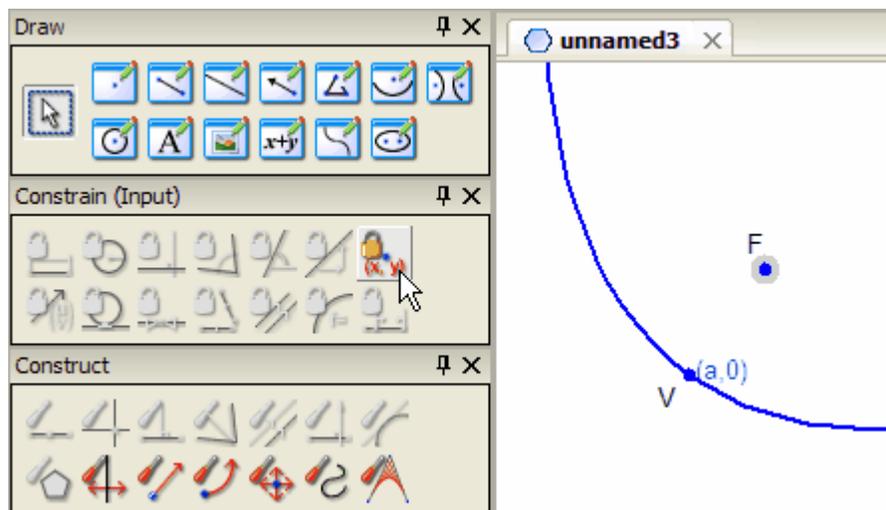
1. Click the **Parabola** icon  in the **Draw** toolbox or select **Parabola** from the **Draw** menu.
2. Move the cursor  in the drawing window to the position of the parabola's vertex. Click and drag the mouse along the major axis. Release the mouse at the focus.

After sketching the general parabola, you can constrain it in the following ways:

1. Click the parabola and select **Implicit equation**  from the **Constrain** toolbox and type or paste the formula.



2. Constrain the vertex and focus points to some coordinate values.



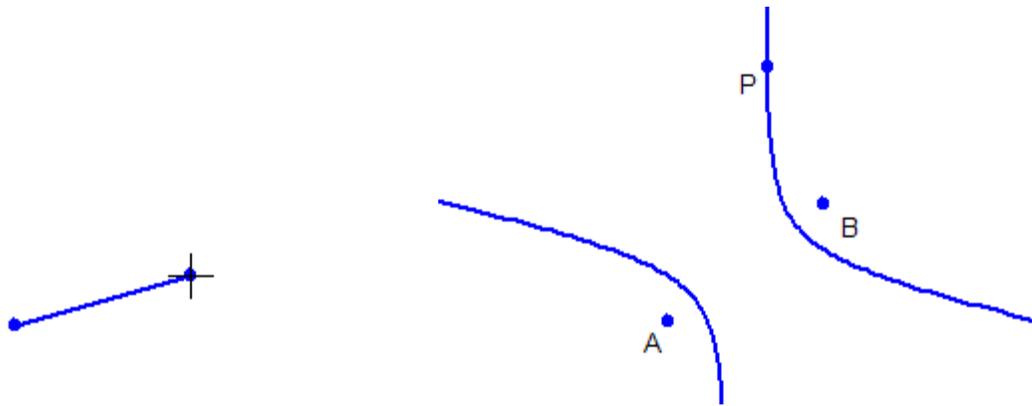
3. You can also adjust the parabola with the [Translation](#), [Rotation](#) and [Dilation](#) tools.

Drawing Hyperbolas



To create a hyperbola in your diagram, follow these steps:

1. Click the **Hyperbola** icon  in the **Draw** toolbox or select **Hyperbola** from the **Draw** menu.
2. Move the cursor  in the drawing window to the position of one focal point. Click to place the first focus. Move the cursor and click again to place the second focal point.
3. Then move the cursor to open the hyperbola to the desired shape and click the mouse a third time.



The hyperbola will appear with three labeled points, the two foci and a point on the hyperbola.

The **Hyperbola** tool is a modal command. You can continue making hyperbolas until you choose the select arrow or another drawing tool.

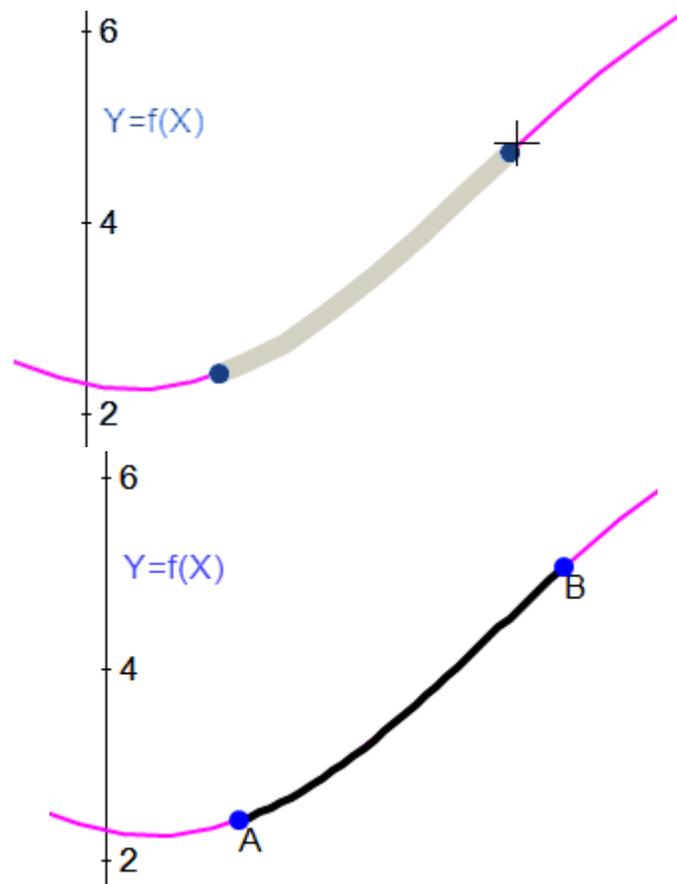
Drawing Arcs



Arcs can be placed on any of the conics - circle, ellipse, parabola, hyperbola - or any function. Points are automatically placed at the ends of the arc.

Here are the steps:

1. First draw the conic or function which will be the basis for the arc.
2. Choose the Arc tool  and move the cursor over the section of the existing curve where the arc will be defined. Click and drag the cursor over the curve.

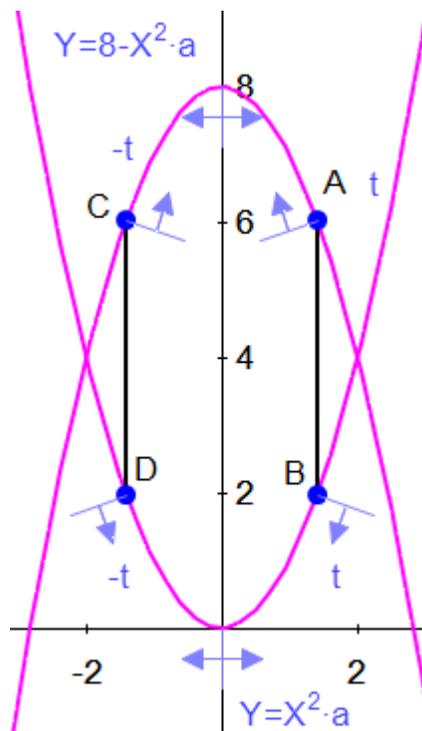


Endpoints are automatically inserted on the arc.

Curvilinear Polygons

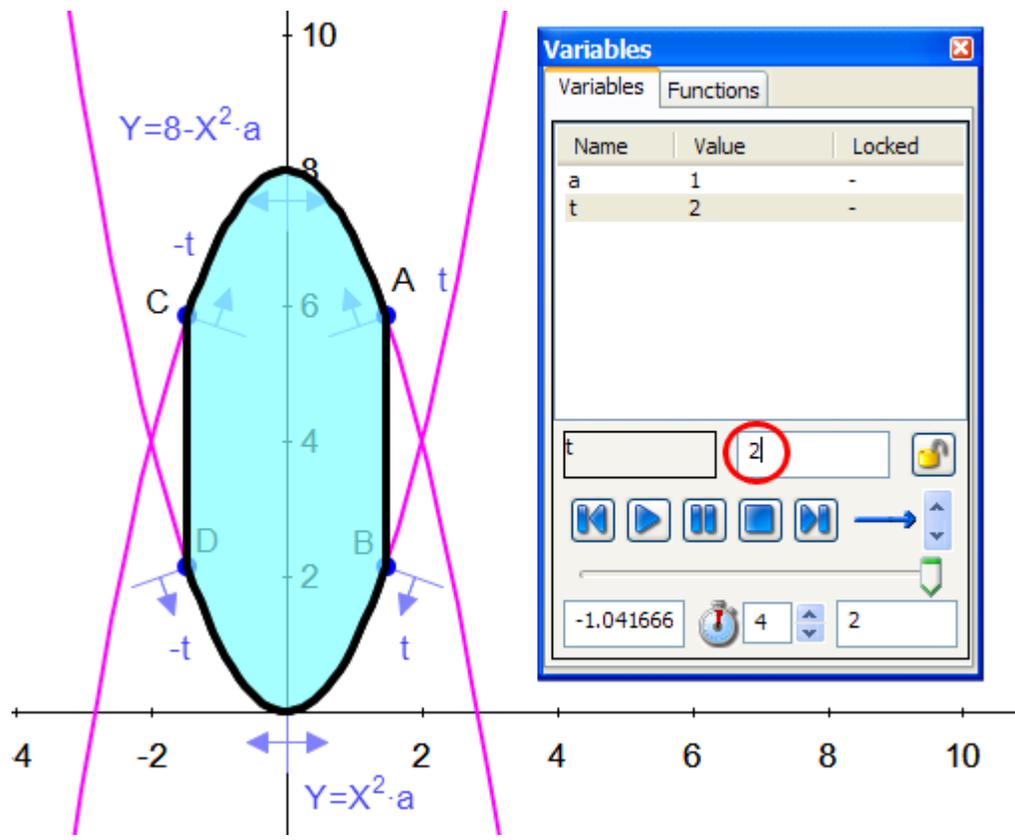
The **Arc** drawing tool lets you make curvilinear polygons for which you can assign fill properties and find areas. There are some limitations, however.

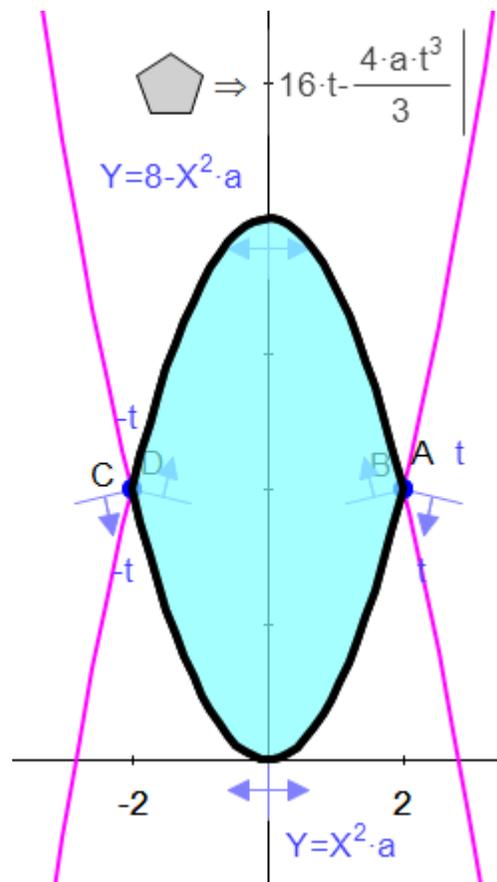
Since you can't construct a point on two intersecting curves (except for circles), you have to connect curves with line segments. If you want to connect two arcs, you have to first connect them with a line and move it to the intersection like this:



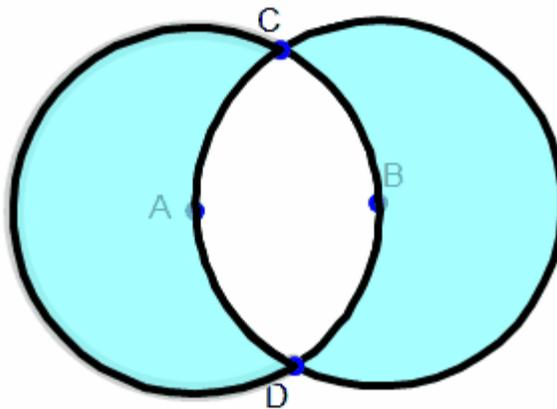
To make a curvilinear polygon of the intersecting parabolas here are the steps:

- Attach two lines.
- Make endpoints C and D $-t$ [point proportional along the curves](#).
- Make endpoints A and B t point proportional along the curves.
- Draw the two arcs - select **Draw / Arc**, from C to A and D to B.
- Select the sides and arcs of the polygon in order and click **Construct / Polygon**.
- Set $t=2$ in the **Variables** toolbox and the lines will become the intersection points.





It's easier with circles because you can place points on their intersections:



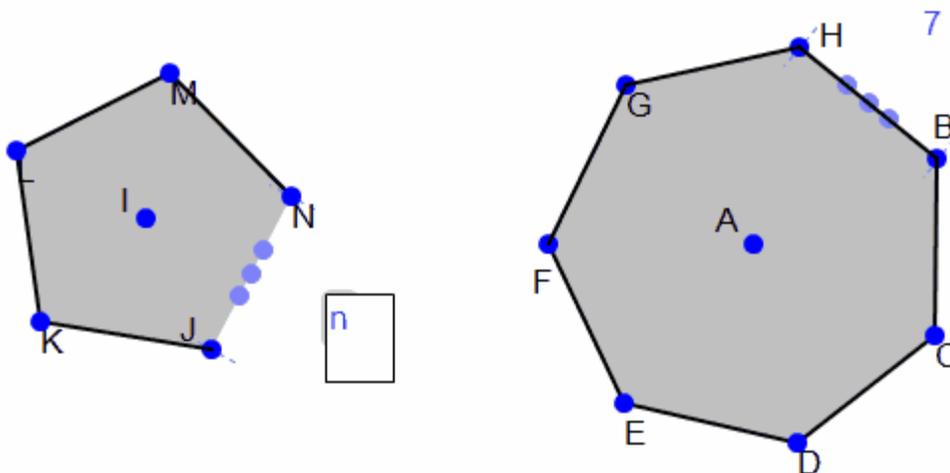
Drawing Regular Polygons



The **N-gon** tool lets you quickly draw any regular polygon. You can even work on problems where the number of sides is n , or whatever variable you choose.

Here are the steps:

1. Click the N-gon button  in the Draw toolbox.
2. Similar to drawing a circle, position the cursor to place the center of the n-gon and click to the desired size. The n-gon at first appears to be a pentagon.
3. In the data entry box, enter the number of sides you want or a variable to represent the number of sides and press Enter.



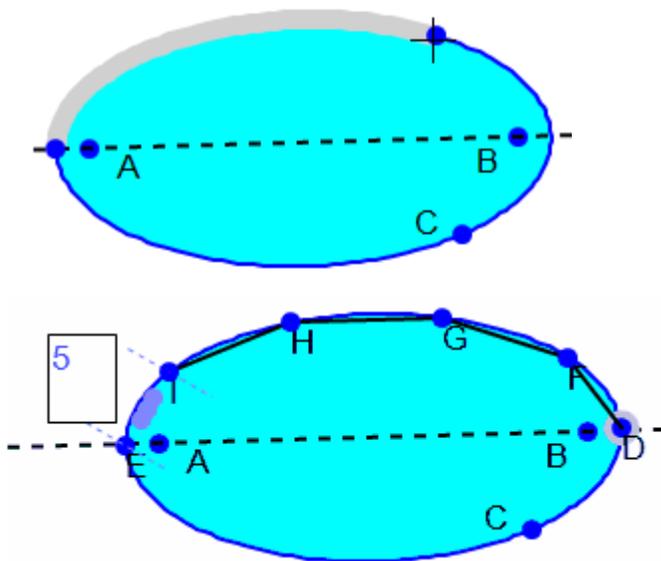
Drawing Curve Approximations



The **Curve Approximation** tool will insert a specified number of points and edges evenly spaced on a selected section of a curve or conic. This is a great tool for introducing problems using the Trapezoidal Method of integration. (Take a look at our [Gx book, Calculus Explorations](#) .)

Here are the steps:

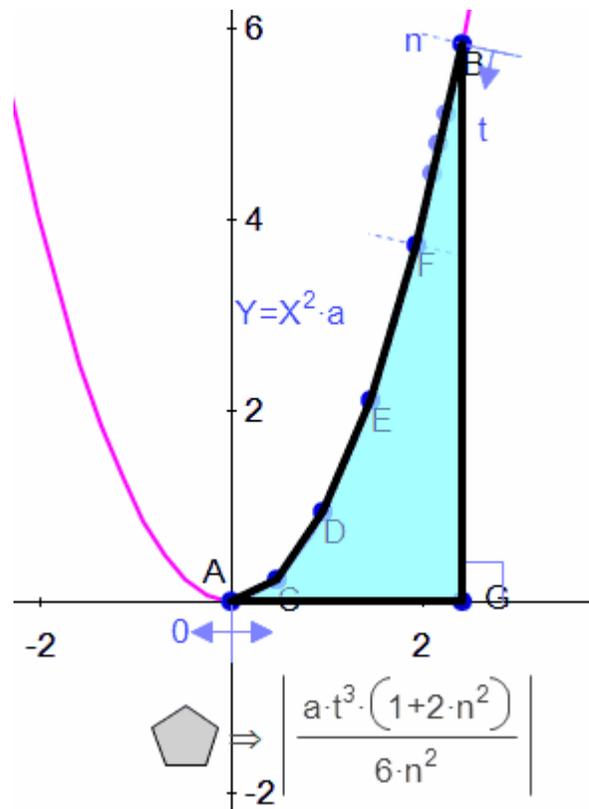
1. Click Draw / Curve Approximation .
2. Select any function, circle, ellipse or parabola and drag the cursor over the curve.
3. In the data entry box type the number of points you want on the arc.



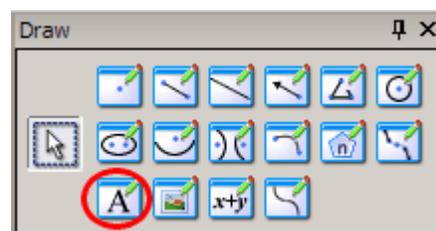
Note: It is best to draw your curve independent of existing points on the curve. Then connect other geometry to the approximation points. If you start or finish the arc with points lying on the curve (e.g. point C in the ellipse above) and later decide to delete the curve approximation,

attached geometry may also get deleted.

Here is the area of a function using the Trapezoidal Method:



Adding Text to the Drawing



To add titles or other annotation to the drawing follow these steps:

1. From the **Draw** toolbox click the **Text** icon  or select **Text** from the **Draw** menu.

2. Position the text cursor  at the upper left corner where you would

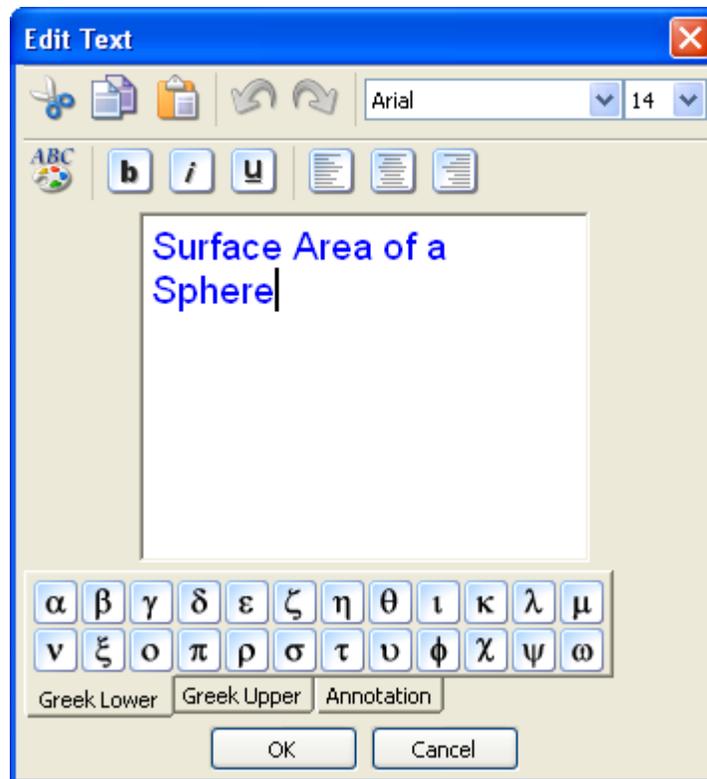
like your window of text located.

3. Click and drag to form your text box to the appropriate size.
4. Enter and format your text in the [Edit Text dialog](#).

Enter mathematical statements using the [Annotation / Expression](#) tool.

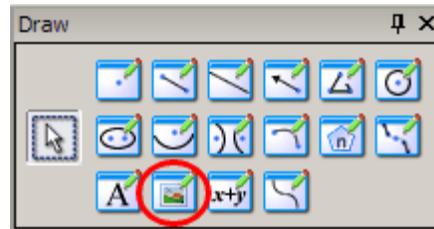
Inserting and Editing Text

In the **Edit Text** dialog you can enter and format the text that will be displayed in your defined text window.



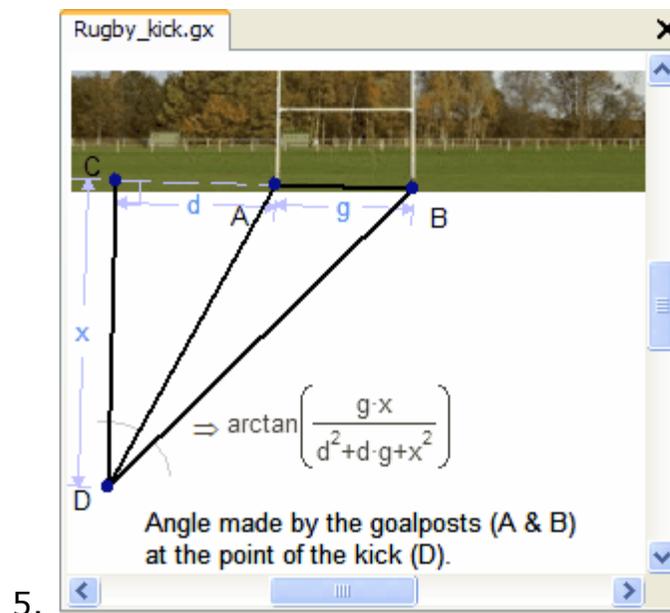
The default text formatting for this dialog is set in **Edit / Preferences / Text & Pictures**.

Using Pictures in the Drawing



Liven up your examples with a picture or two, or use an image for reference points in your drawing. Here's how:

1. Click the **Picture** icon  in the **Draw** toolbox or select **Picture** from the **Draw** menu.
2. Click and drag the cursor to delimit the area where you want to place the picture.
3. Find your image in the **Select Image File** dialog. Image formats include: **.bmp**, **.gif**, **.jpg**, **.pcx**, **.png**, and **.tif**
4. After entering an image, you will be in **Select**  mode.

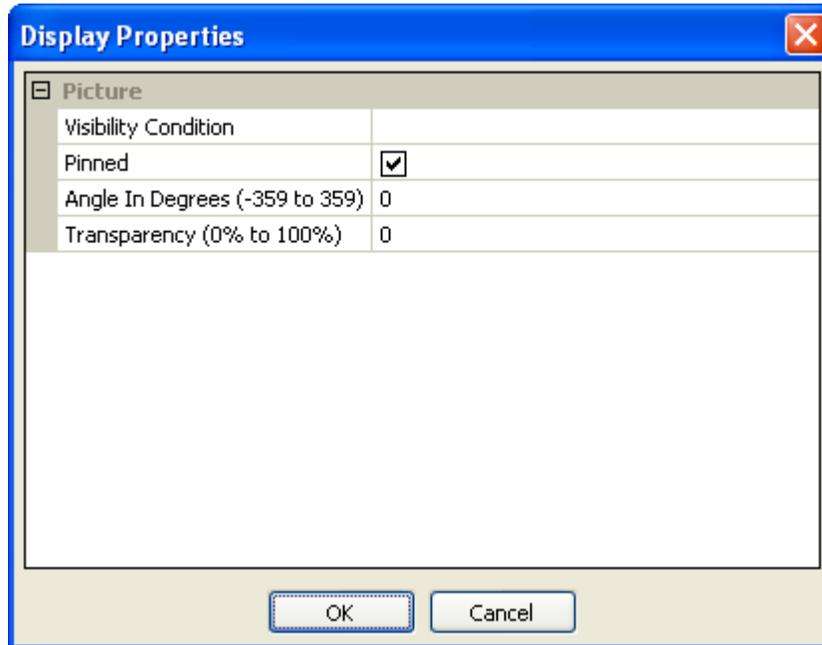


Pictures are always inserted under your drawing objects, so you can add a picture at any time.

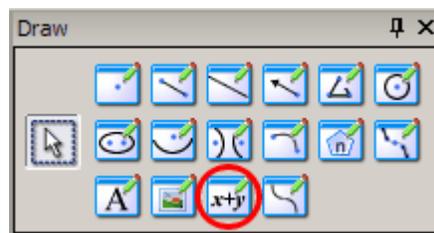
In **Select**  mode you can move a picture, as with any drawing object.

The inserted picture can be rotated and the transparency level can be set in the **Display Properties** dialog box.

- Right click on a highlighted picture and then select **All Properties**
- Or select **Properties** from **Edit** menu.



Adding Expressions

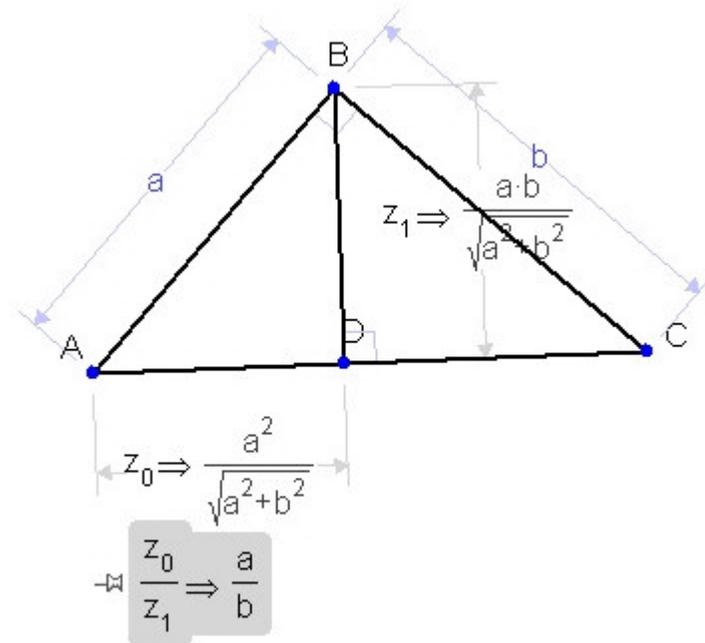


You can type an algebraic expression in the drawing window and *Mechanical Expressions* will solve it with whatever information it has available. Here are the steps:

1. From the **Draw** toolbox click the **Expression** icon  or select **Expression** from the **Draw** menu.
2. Move the expression cursor  to the position where you want it to appear in the drawing window and click to display the data entry box.

- Enter the expression using numbers, variables, and output expression names. Use the [Symbols](#) toolbox to help you enter mathematics.

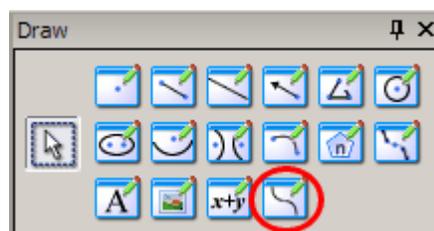
Adding an expression to the diagram can help you work out relationships in the geometry. Here is an example making use of the **Expression** tool to see the relationship between similar triangles.



Sides a and b are perpendicular, and AC is perpendicular to BD . We obtained the [Output](#) of lengths AD and BD using the [Show Name button](#).

The expression to solve is the relationship of the two lengths: z_0 / z_1 . The system immediately evaluates the expression as $\Rightarrow a/b$.

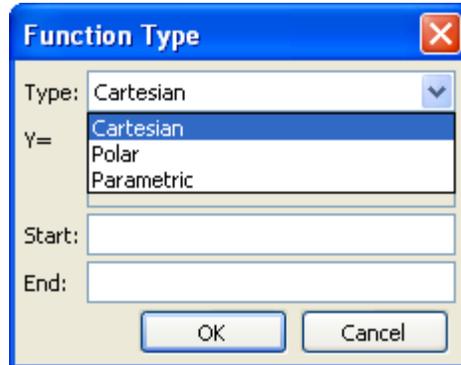
Creating Functions



- Click the **Function** icon  in the **Draw** toolbox or select **Function**

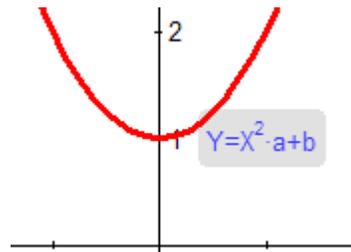
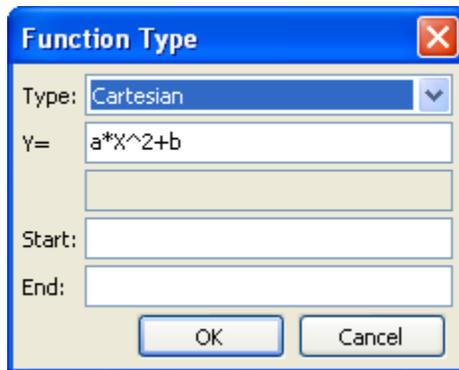
from the **Draw** menu

2. Click the drop-down list button to select the function type that you want to use in your drawing.



Cartesian Function

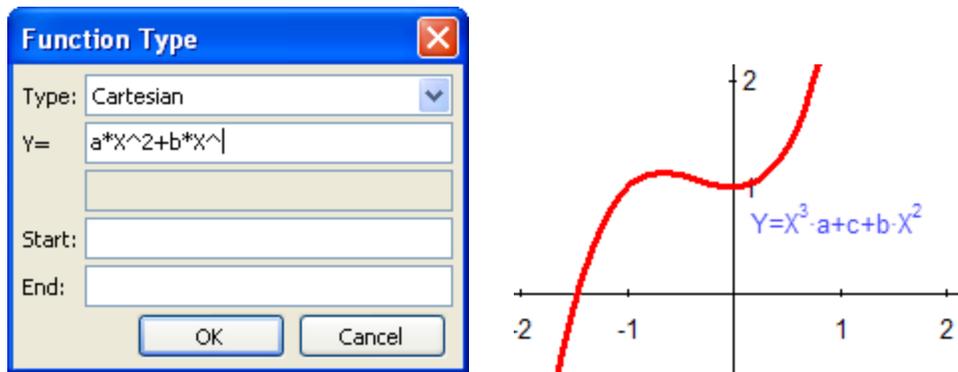
When you select **Cartesian** from the **Function Type** dialog, the next line contains a general form of the function in terms of Y.



You can define a domain of the function by enter values for Start and End. If you want to draw function with indefinite domain, leave these fields blank.

You can define this function in these ways:

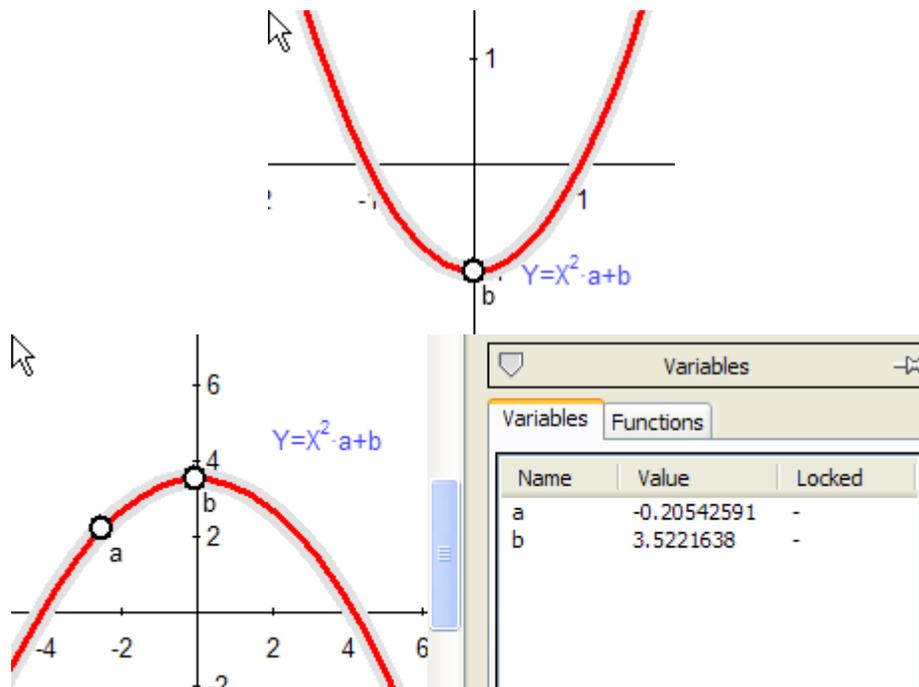
- Modify the formula directly:



- Modify the function interactively using "handles". In the drawing window, click the function to select it. Click and drag it and a circle appears on the curve. This handle represents one of the variables in the equation. You can click and drag this handle around the drawing. Click and drag another place on the function and another moveable handle appears if there is another variable in the equation.

This feature is a wonderful way to understand exactly how the equation represents the function.

In the first example, a click of the curve gives you the b handle, the y -intercept, and lets you drag the function up and down. Click and drag another place on the curve and you get the a handle to change the shape of the curve.

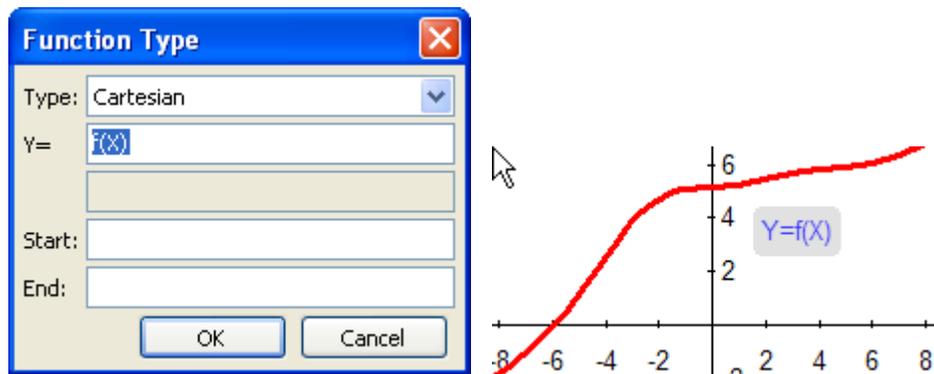


Notice the **Variable** toolbox displays the changing values as you move the handles.

- Modify the function after it's drawn by double clicking the function tag and changing it in the edit box.
- Modify the domain of the function after it's drawn by double clicking the curve.

The Generic Function $f(X)$

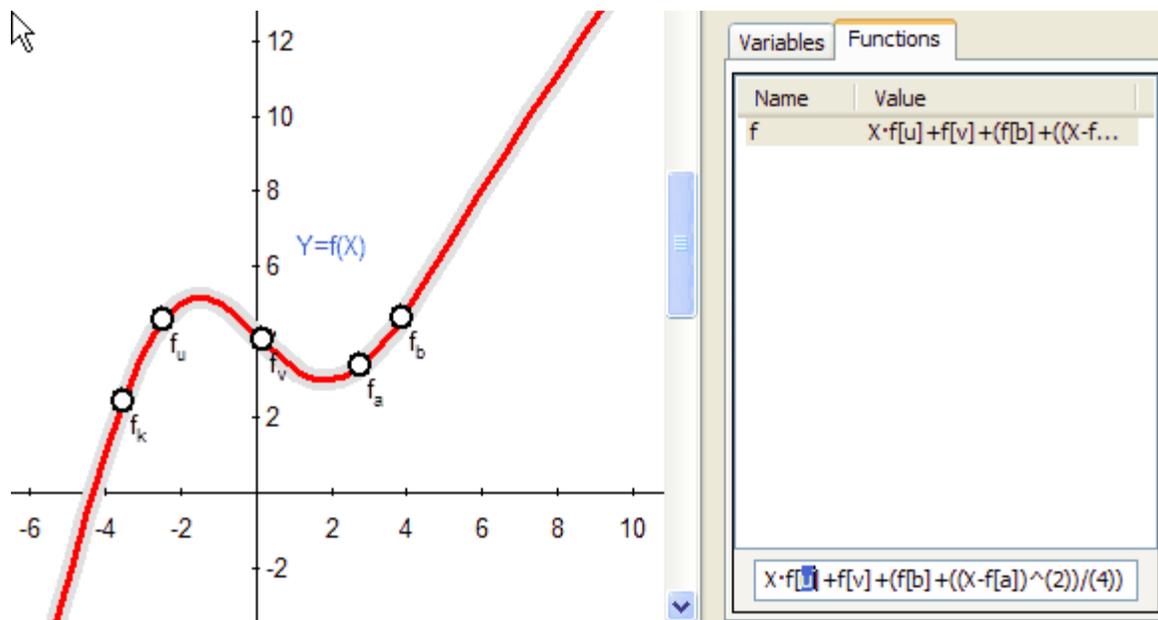
To use the generic form of a function, $Y=f(X)$, select **Cartesian** from the **Function Type** dialog, enter $f(X)$ in the edit window and click **OK**:



Click the **Functions** tab of the **Variables** toolbox to see the values used in the function.

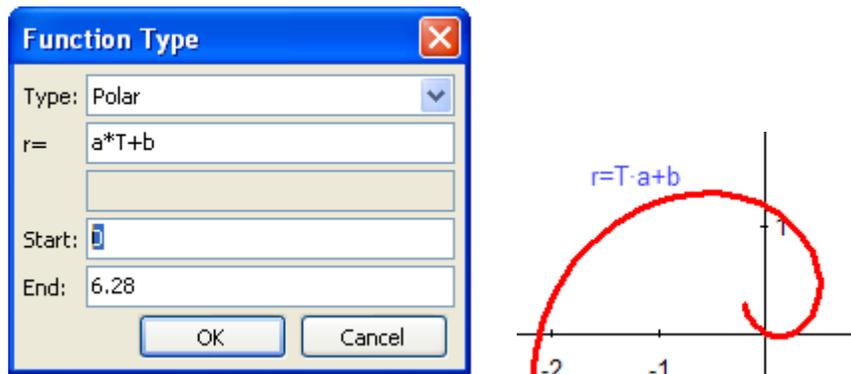
You can define this function in these ways:

- Modify the edit line at the bottom of the **Functions** tab. (Use your keyboard arrow keys to move through the whole function.)
- Modify the function interactively using "handles". In the drawing window, click the function to select it. Click and drag it and a circle appears on the curve. This handle represents one of the variables in the equation. You can click and drag a handle around the drawing to change the curve. Click and drag another place on the curve and another moveable handle appears if there is another function variable in the equation. In the general function in this example we have 5 possible handles: $f(a)$, $f(b)$, $f(k)$, $f(u)$, and $f(v)$.



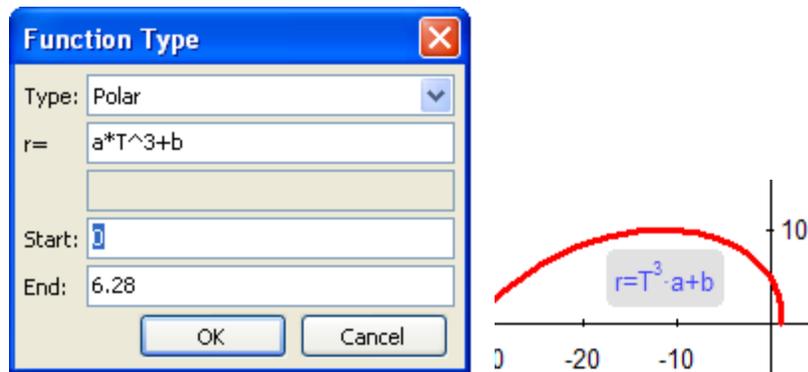
Polar Function

When you select **Polar** from the **Function Type** dialog, the next line contains the general form of the function in terms of the radial coordinate, r and the polar angle, T .



You can define this function in these ways:

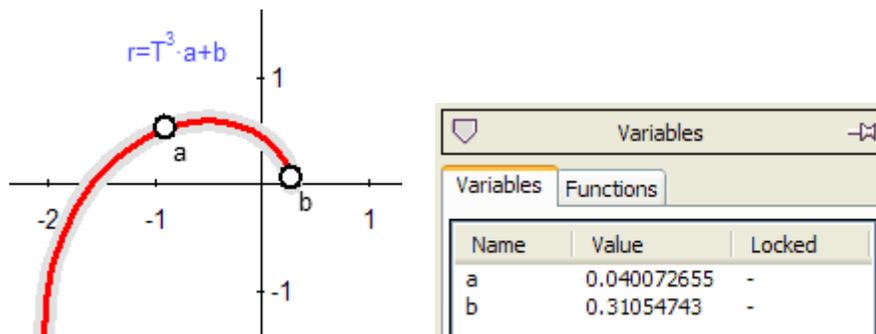
- Modify the formula and the curve domain directly:



- Modify the function interactively using "handles". In the drawing window, click the function to select it. Click and drag it and a circle appears on the curve. This handle represents one of the variables in the equation. You can click and drag this handle around the drawing. Click and drag another place on the function and another moveable handle appears if there is another variable in the equation.

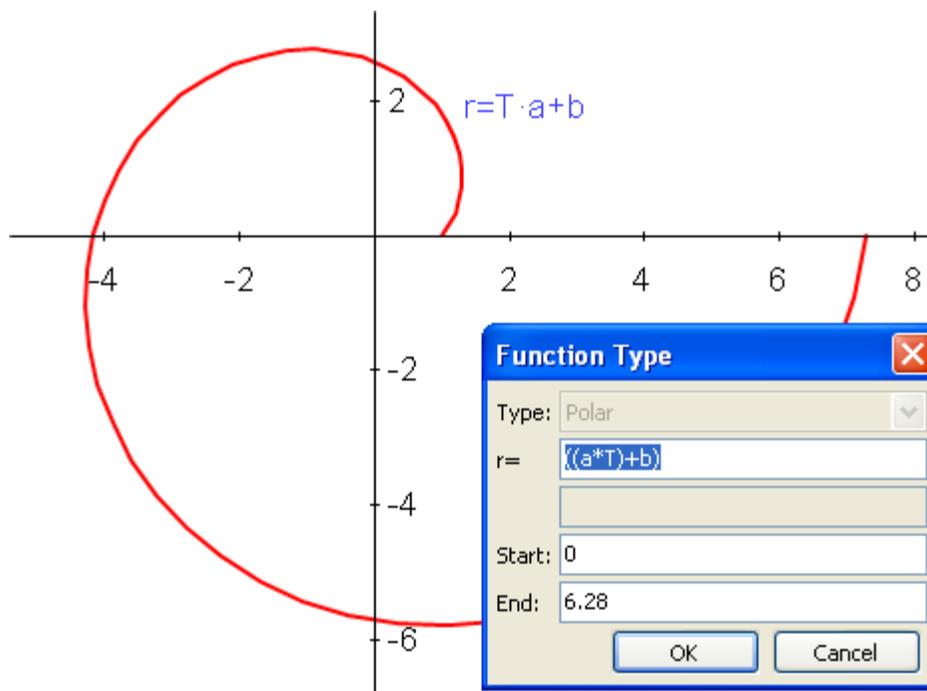
This feature is a wonderful way to understand exactly how the equation represents the function.

In the example above, the second click gives you the a handle; click and drag another place on the curve and you get the b handle to change the shape of the curve.



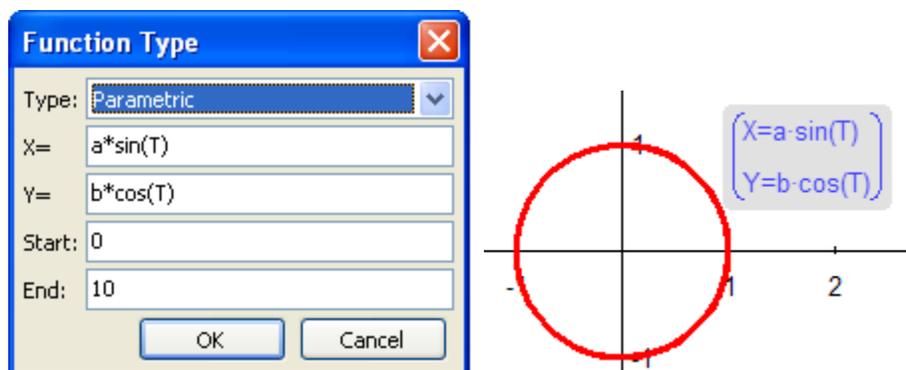
Notice the **Variable** toolbox displays the changing values as you move the handles.

- Modify the function after it's drawn by double clicking the function tag.
- Modify the domain of the function after it's drawn by double clicking the curve:



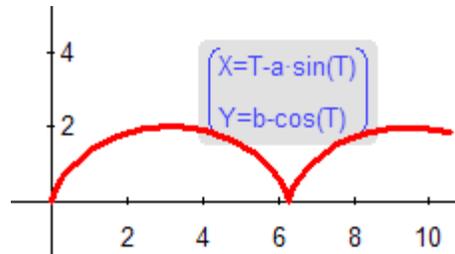
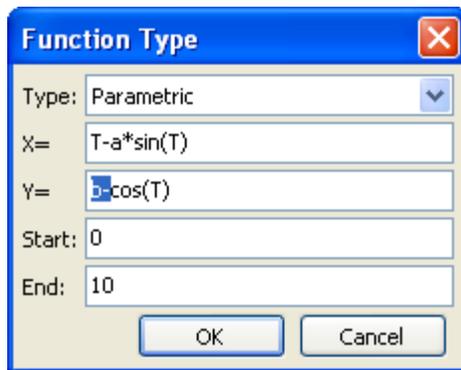
Parametric Function

When you select **Parametric** from the **Function Type** dialog, the next line contains the general form of the function in terms of X and Y and a parameter, T.



You can define this function in these ways:

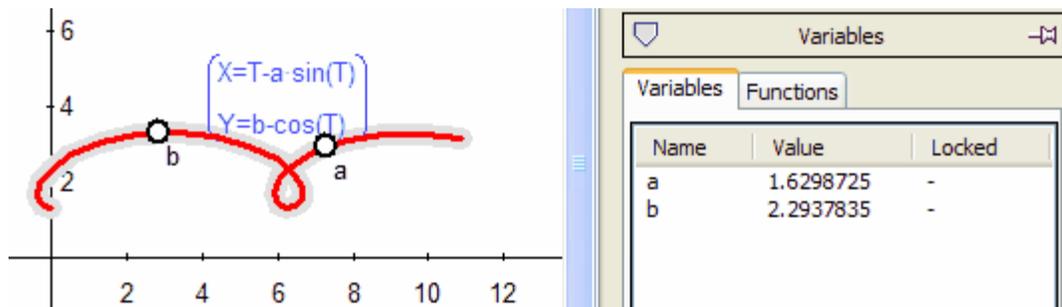
- Modify the formula and its domain directly:



- Modify the function interactively using "handles". In the drawing window, click the function to select it. Click and drag it and a circle appears on the curve. This handle represents one of the variables in the equation. You can click and drag this handle around the drawing. Click and drag another place on the function and another moveable handle appears if there is another variable in the equation.

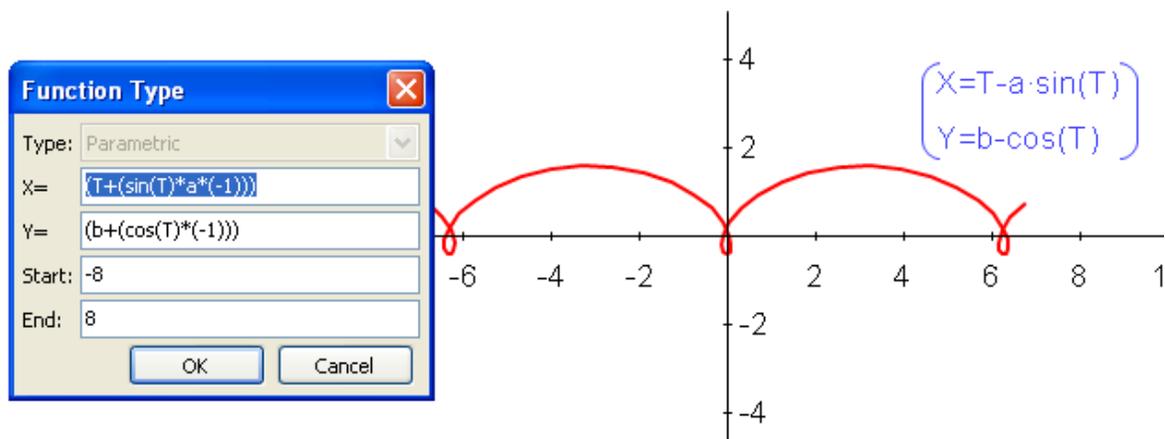
This feature is a wonderful way to understand exactly how the equation represents the function.

In the example above, $X=T-a*\sin(T)$, $Y=b*\cos(T)$, a click and drag gives you the b handle, and lets you drag the function up and down. Click and drag another place on the curve and you get the a handle to change the shape of the curve.



Notice the **Variable** toolbox displays the changing values as you move the handles.

- Modify the function after it's drawn by double clicking the function tag.
- Modify the domain of the function after it's drawn by double clicking the curve:



Piecewise Function

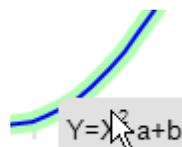
A piecewise function or expression can be created using the **Piecewise** symbol:



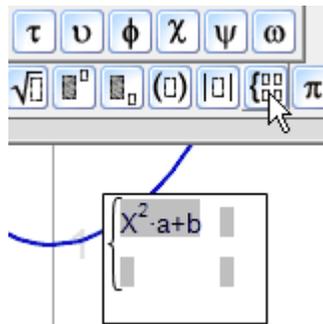
or the [built-in function](#) - `piecewise({expression1, domain1},{expression2, domain2}...,{last expression, otherwise})`. The reserved word, "otherwise" is an option available for the last condition.

Here we show how to enter the sequence of values, followed by conditions:

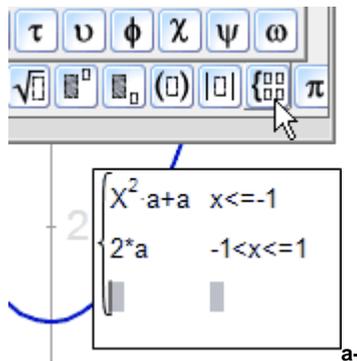
- Create a function.
- Double click the equation to edit.



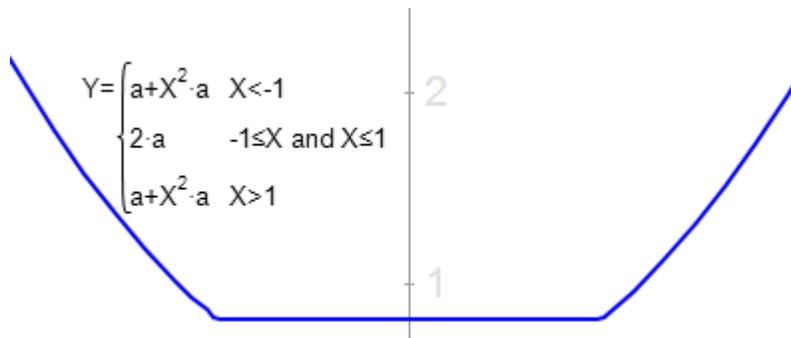
- From the edit box click the **Piecewise** icon in the **Symbols** toolbox. Four small gray boxes will appear, including the one containing the original equation.



- Fill in your piecewise parameters - equations in the left column and their domain in the right column. To expand the function, click the **Piecewise** icon again for an additional row.



Here's the finished piecewise function:



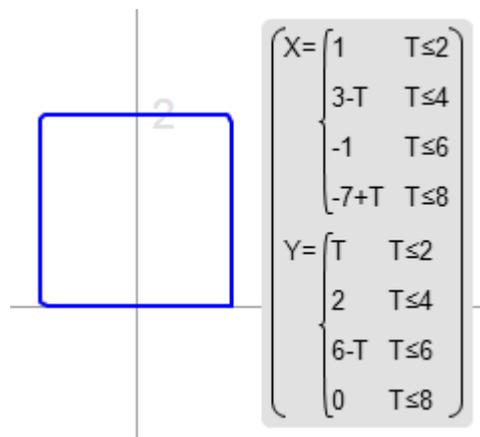
Piecewise Parametric Example

Any of the functions available in *Mechanical Expressions* can be piecewise, including parametric functions. Take this square for example.

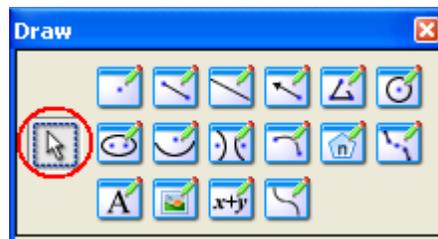
- Click the **Draw / Function** tool 
- Select **Parametric** from the drop down Type window.
- Enter the first value (side) for the square and the range for the parameter values - hit enter. Don't worry about the shape of the function, it's not defined yet.

4. Double-click the function and select the x value
5. Click the **Piecewise** icon
6. Enter the x values for each side of the square. When you run out of gray boxes, click the **Piecewise** icon again to get another row.
7. Now do the same for the y value, select the T parameter and click the **Piecewise** icon 3 times. Use the arrow keys on your keyboard or your mouse to move to the next gray box.

Here is the function:



The Selection Arrow

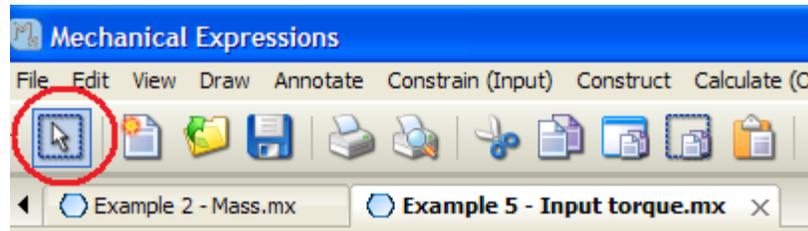


When you are finished with the drawing functions, click the selection arrow  to enable other functions or [adjust your drawing](#).

With the arrow, you must first select elements of the drawing in order to enter [constraints](#) and [constructions](#) and to [output calculations](#).

Many of the tools require you to select [multiple objects](#).

The **Selection** arrow is also available from the icon bar at the top of the screen.



Selecting Multiple Objects

Many of the **Constrain**, **Construct**, and **Calculate** tools require that you select more than one object.

To select more than one object:

- Click the selection arrow  on the tool bar.
- Hold down the CTRL or SHIFT key as you click the objects you want to select.

If you click the wrong object while holding down the CTRL key, click it again and it will become unselected.

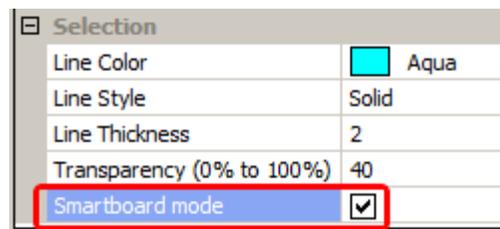
If all of the objects you wish to select fall within a rectangular region, you can use the selection box:

- Click on the selection arrow  on the tool bar or the **Drawing** toolbox.
- Draw a rectangle around all of the objects by clicking and dragging.

If you are using *Mechanical Expressions* on a *Smartboard*, turn on [Smartboard mode](#) to make multiple selections without using the *Ctrl* or *Shift* keys. In this mode selections accumulate. Clicking a blank space in the drawing does not clear the selections. Clicking on an item a second time unselects only that item.

Smartboard Mode

To turn on the **Smartboard** mode select **Edit / Preferences / Selection**; in the Selection group and check (click) the Smartboard mode selection box.



When the box is checked, selections accumulate until you click a command. Clicking a selected item a second time unselects that item, but any other selected items stay selected. To clear all the selections, select **Clear Selection** under the **Edit** menu or click all the selected objects again.

Adjusting the Drawing

Click the [Select](#) arrow , either from the **Drawing** toolbox or the icon bar, to move, rotate or delete selected object(s) in the drawing.

You can change a constraint value, annotation or label by double clicking it, retyping the value or variable and then pressing the enter key.

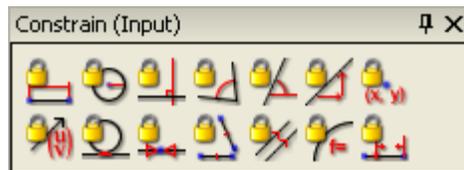
The [Scale, Zoom](#)   and **Move / Pan**  functions have a mouse shortcut:

- The scroll wheel on your mouse can be used to **Scale** the drawing up or down. Hold down the ctrl key while moving the wheel and the operation becomes a **Zoom**.
- Right-click and drag the mouse anywhere in the drawing window to **Move** or **Pan**.

The **Move geometry** icon  is a modal command. It stays active until you select  or choose another mode (e.g. any **Draw** tool).

Constraints

Using Drawing Constraints



After sketching the geometry of a problem, constrain it with measurements, coordinates and implicit equations in real or symbolic terms. The drawing responds automatically to the assigned input constraints. *Mechanical Expressions* will [automatically add any constraints](#) you leave out.

Since [annotations](#) may look identical to constraints, use the icon, , to **Distinguish Constraints / Annotations**. The icon is a toggle; to turn off the marks, click it again.

Initially, all the constraints in the toolbox are inactive. You must first select the parts for your drawing that will be constrained. Constraint choices are listed below along with the drawing elements that must be preselected. Be careful when selecting geometry objects, if extra things are selected that are not related to the constraint (like other constraints) the constraints will remain inactive. This can happen by mistake, especially when using the selection box tool.

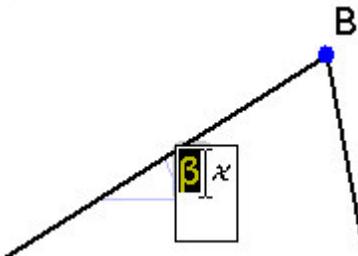
	Constraint	Preselected Objects
	Distance / Length	Two of any combination of points, lines, line segments, vectors, or polygon sides.
	Radius	A circle
	Perpendicular	Two of any lines, segments, vectors, or polygon sides.
	Angle	Two of any lines, segments, vectors, or polygon sides.
	Direction	A line, segment, vector, or polygon side.

	Slope	A line, segment, vector, or polygon side.
	Coordinate	A point
	Coefficients	A vector
	Tangent	A circle or locus and a line, segment, vector, or polygon side.
	Incident	A point and a line, segment, vector, polygon side, circle or locus.
	Congruent	Two or three of any line segment, vector, or polygon side.
	Parallel	Two or three of any line segment, vector, or polygon side.
	Implicit Equation	A circle, line, segment, vector, or polygon side.
	Point Proportional Along Curve	A point and a line, segment, vector, polygon side, or locus

Occasionally you may try to add too many constraints to the geometry, causing a conflict. The system will help you correct this problem in the [Resolve Constraint Conflict](#) dialog.

Changing a Constraint

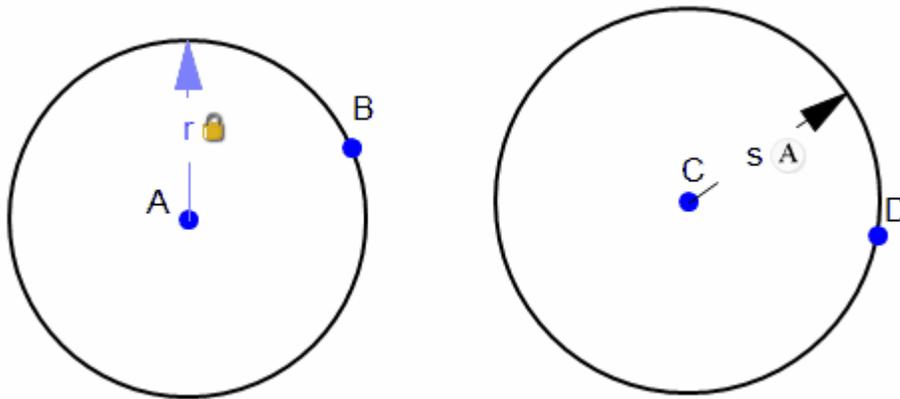
To change a constraint, double click it with the selection arrow,  retype the value or variable and press the enter key.



Distinguishing Constraints from Annotations

Your drawing is defined by [Constraints](#) on geometry elements. [Annotations](#) are like labels and have no influence on the geometry measurements. The original default settings ([Preferences / Math](#)) fix **Constraint** lines and text in blue and **Annotation** lines and text in black. To further distinguish these use the **Distinguish Constraints /**

Annotations  toggle button on the main icon bar.



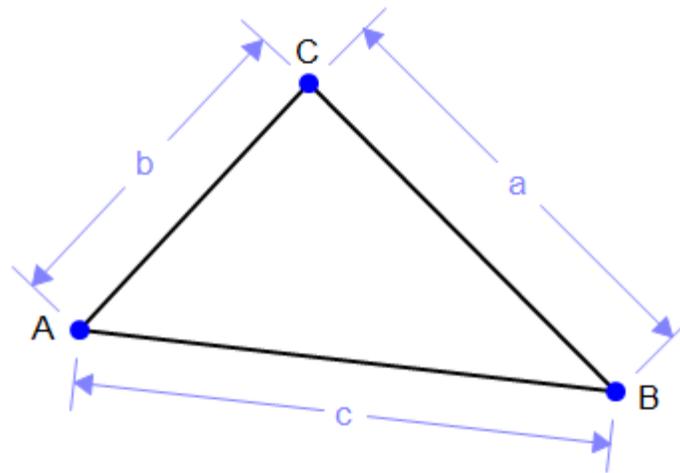
When active, the button is highlighted - , and a  is placed next to all constraints and a  is placed next to all annotations.

As with all toggles, you can turn these marks off with another click of the  button.

System Added Constraints

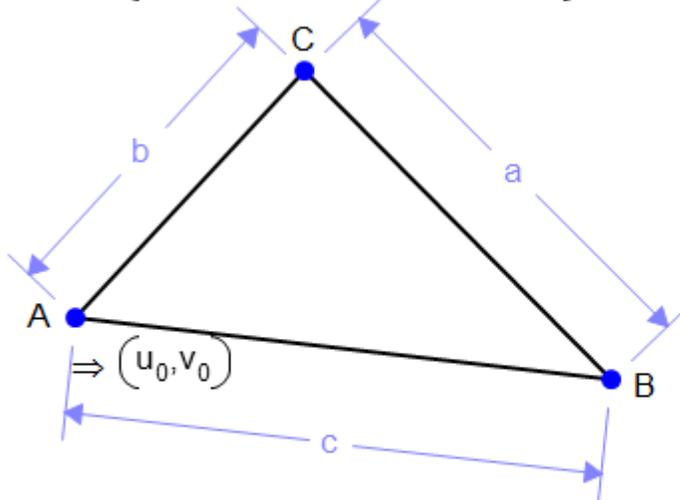
In *Mechanical Expressions*, you do not need to fully constrain your model. Any parameters you have left unconstrained are filled in by the geometry engine.

For example, the following drawing is constrained only modulo a rigid transformation (typical for many geometry problems).



So if you ask for the coordinates of any of the points, they will be given in terms of system added variables:

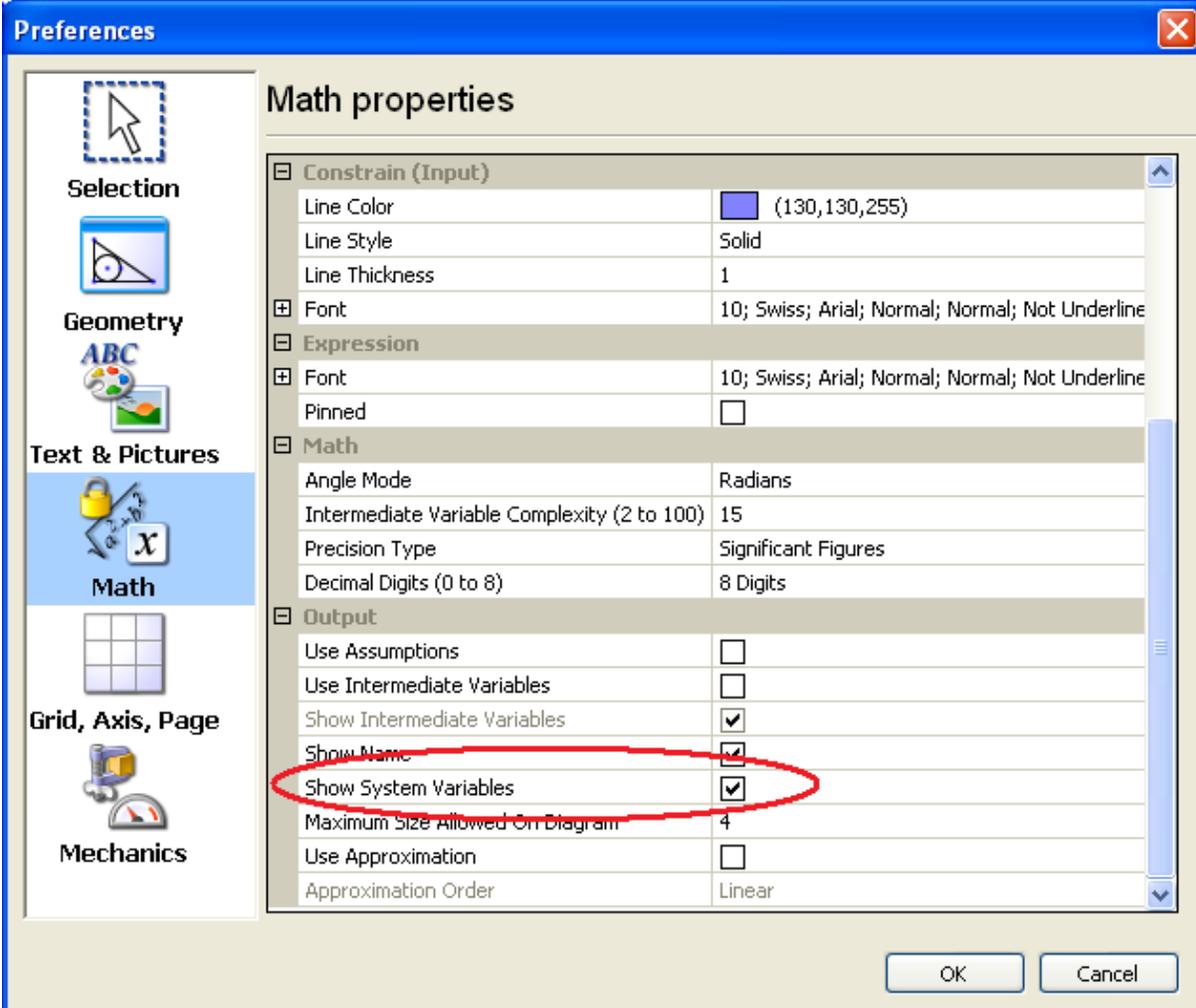
$$\Rightarrow (u_0 + b \cdot \cos(\theta_0), v_0 + b \cdot \sin(\theta_0))$$



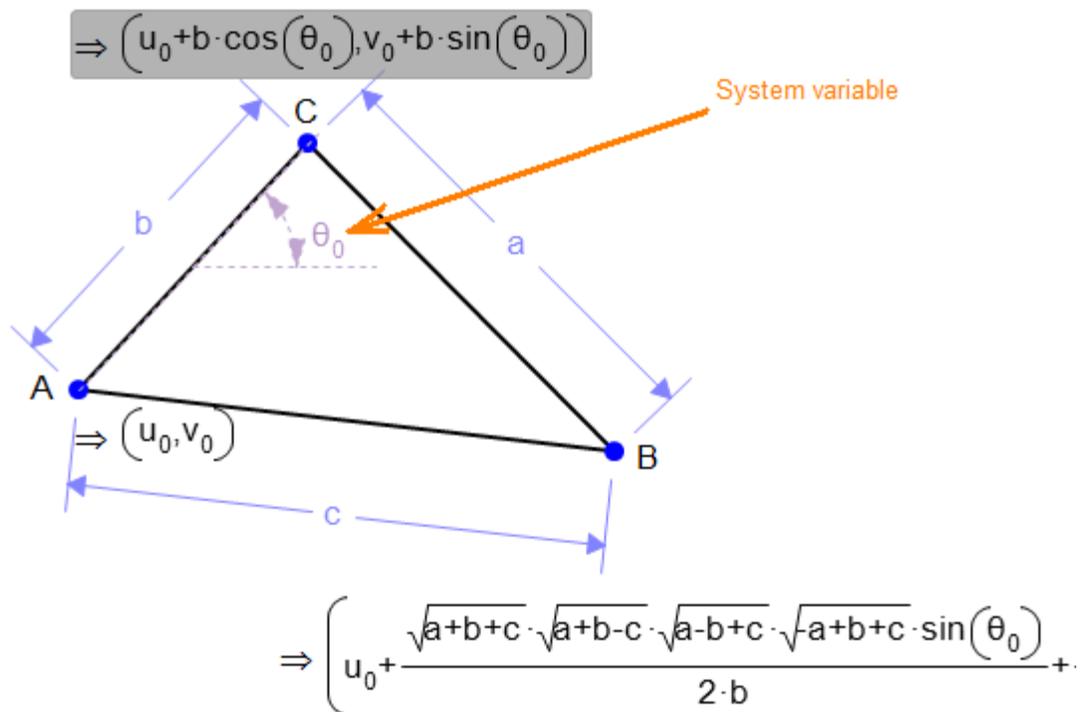
$$\Rightarrow \left(u_0 + \frac{\sqrt{a+b+c} \cdot \sqrt{a+b-c} \cdot \sqrt{a-b+c} \cdot \sqrt{a+b+c} \cdot \sin(\theta_0)}{2 \cdot b} + \right.$$

Clearly the system has added variables for the location of point A, and for the direction of line AC.

To display these variables, check the default setting, Show System Variables, found in the **Edit / Preferences** [menu selection](#) on the **Math** page (left panel) under **Output**.

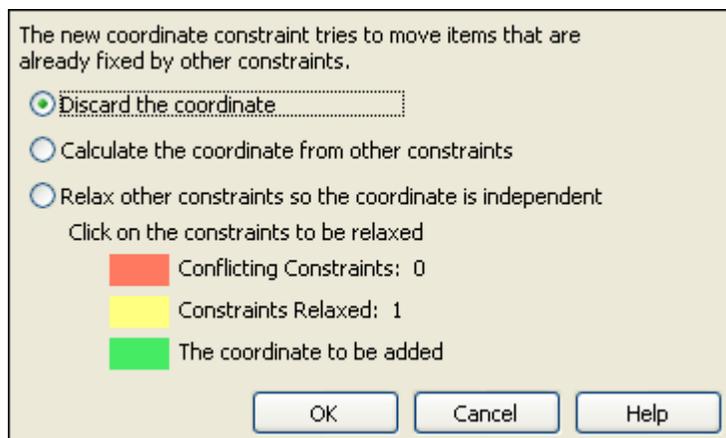


When the box is checked, you will see the system variables when you select the output:



Constraint Conflicts

If you enter a constraint for some geometry which is already constrained by another constrained object you will see a message like the one below.



In this case, the **Coordinate** constraint was already determined by the other two sides and an angle constraint on the triangle. There are three ways of dealing with this problem:

1. Hit the **Cancel** button to leave the drawing as it was without the new

constraint.

2. Click the first button, "Calculate the coordinates from other constraints" (the default choice). This is similar to the first choice, it eliminates the new constraint, but also calculates the selected geometry's value. In this case, the coordinates of point C would be calculated and displayed.
3. If you choose "Relax other constraints so the coordinate is independent", this will keep the new constraint you just entered and allow you to eliminate one of the **red highlighted** constraints (*figure 1*). When you select one of these constraints (in *figure 2* below we clicked on θ), the highlight changes to gray. After you click **Ok**, the selected constraint, the angle θ in this case, is calculated and displayed (*figure 3*).

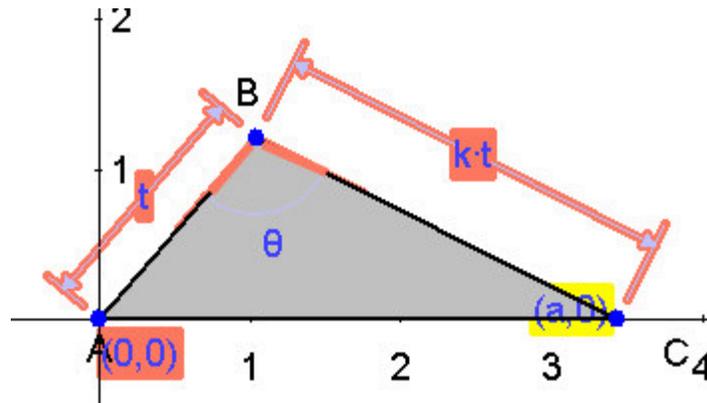


Figure 1

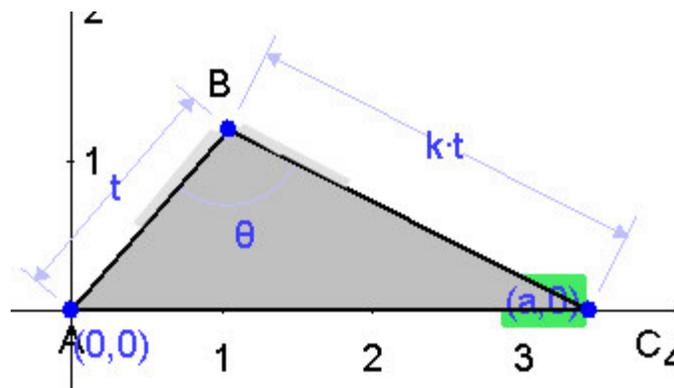


Figure 2

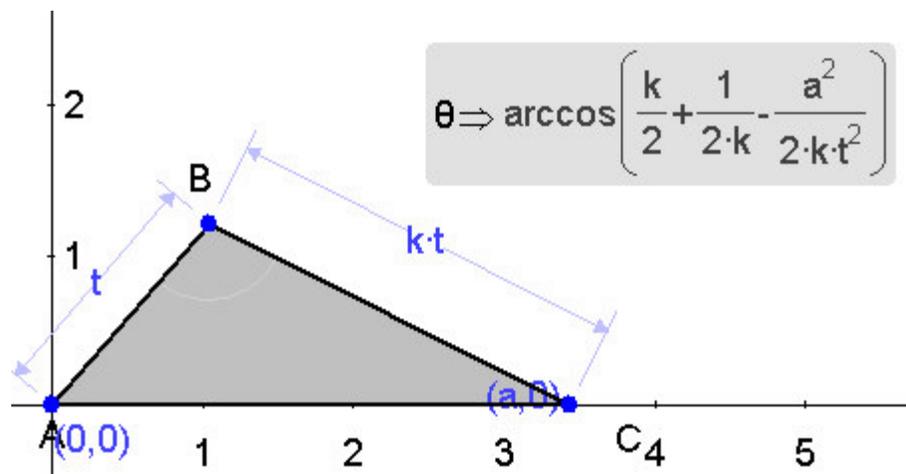
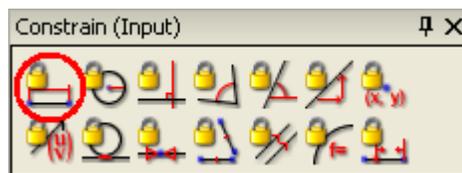


Figure 3

Distance / Length Constraint

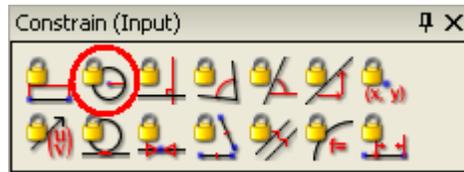


The **Distance / Length** constraint lets you specify the following dimensions:

- Length of a line segment, vector, or polygon side
- Distance between two points or a point and any one of the line types listed above.
- To enter a constraint:
 1. [Select](#)  the appropriate drawing object(s). When you make your selection, the **Distance / Length** icon will light up .
 2. Click the icon, enter the constraint value, either real or symbolic, and press enter. You can press enter without typing a value to accept the system's default value.

You can click the constraint and drag it to adjust its placement on the drawing.

Radius Constraint

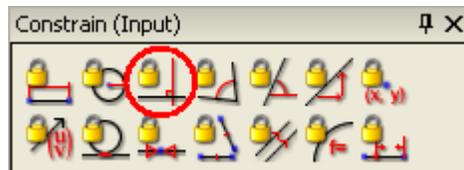


To specify the radius of a circle:

1. From [select](#) mode , click the circle. The circle will be highlighted as well as the icon .
2. Click the **Radius** icon, enter the constraint value, either real or symbolic, and press enter. You can press enter without typing a value to let the system insert a variable name.

You can click the constraint and drag it to [adjust](#) its placement on the drawing.

Perpendicular Constraint

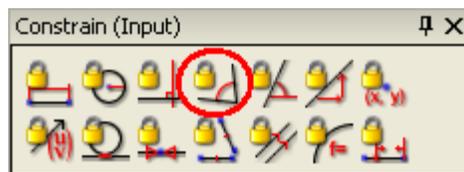


Any two of lines, segments, vectors or polygon sides can be constrained to be perpendicular with these steps:

1. [Select](#)  two from the line types listed above.
2. Click the **Perpendicular** icon .

The lines are redrawn and the perpendicular constraint is attached.

Angle Constraint

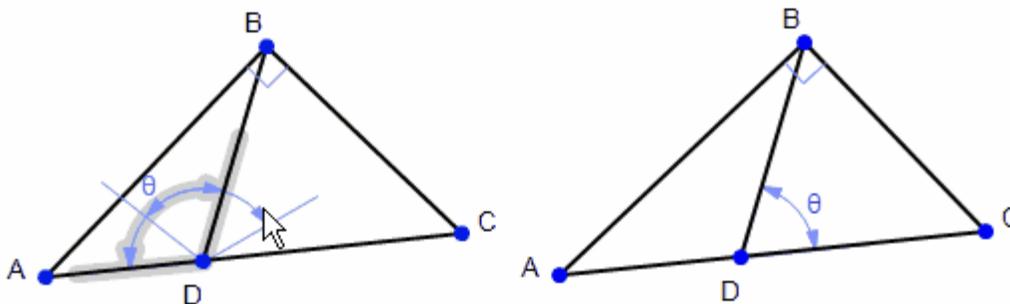


Any two of lines, segments, vectors or polygon sides can be constrained with an angle value or variable name with these steps:

1. [Select](#)  two from the line types listed above.
2. Click the **Angle** icon .
3. Enter the constraint, real or symbolic. If you enter a real value, the lines will be adjusted to reflect the constraint.

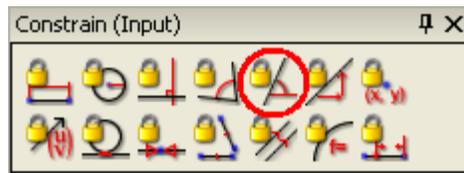
Which Side to Constrain?

Sometimes when identifying angles, the constraint falls on the wrong one. In the example below, we wanted BDC, not BDA. Just click the cursor over the constraint arrow and drag it to the other side, then release the mouse button - done!



Note: The angular units are displayed in the lower right of the screen. Change the default Angle Mode in the **Edit / Preferences / Math Properties** menu, **Math** settings group.

Direction Constraint

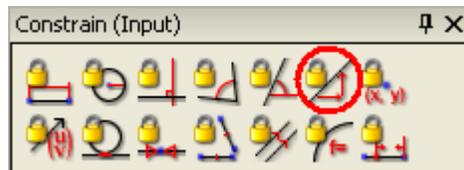


Constrain any of the line types; line, line segment, vector, or polygon side, to a direction measured from the horizontal.

1. [Select](#)  one of the line types listed above.
2. Click the **Direction** icon .
3. Enter the constraint, real or symbolic. If you enter a real value, the line will be adjusted to reflect the constraint.

Note: The angular units are displayed in the lower right of the screen. Change the default (Degrees or Radians) in the **Edit / Preferences** menu.

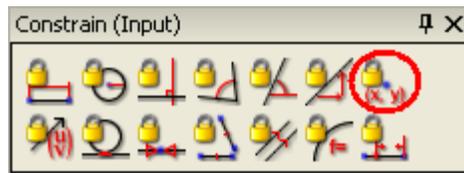
Slope Constraint



Specify a slope for any of the line types; line, line segment, vector, or polygon side.

1. [Select](#)  one of the line types listed above.
2. Click the **Slope** icon .
3. Enter the constraint, real or symbolic. If you enter a real value, the line will be adjusted to reflect the constraint.

Coordinate Constraint

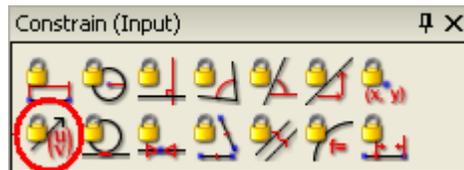


You can give coordinates to any point in your drawing:

1. [Select](#)  a point.
2. Click the **Coordinate** icon .
3. Enter the constraint, real or symbolic. If you enter a real value, the line will be adjusted to reflect the constraint, even if the coordinate axes are not displayed.

To change the coordinates shown, double click and type over the highlighted value in the data entry box.

Constraining Vector Coefficients

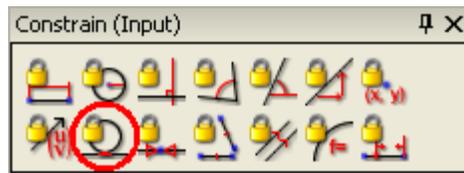


You can specify coefficients for a vector with the following steps:

1. [Select](#)  a vector.
2. Click the coefficients icon .
3. Enter the coefficients separated by a comma.

Note: Don't forget the parentheses or an error message appears.

Tangent Constraint

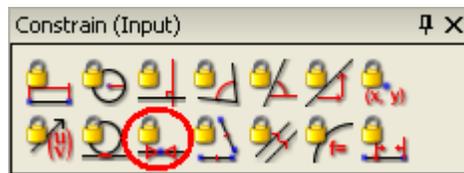


Any of the line types; line, line segment, vector, or polygon side can be made tangent to a circle or locus with these steps:

1. [Select](#)  a line of the types listed above and the circle or locus.
2. Click the **Tangent** icon  from the **Constrain** tool box or select **Tangent** from the **Constrain** menu.

The line and curve immediately become tangent.

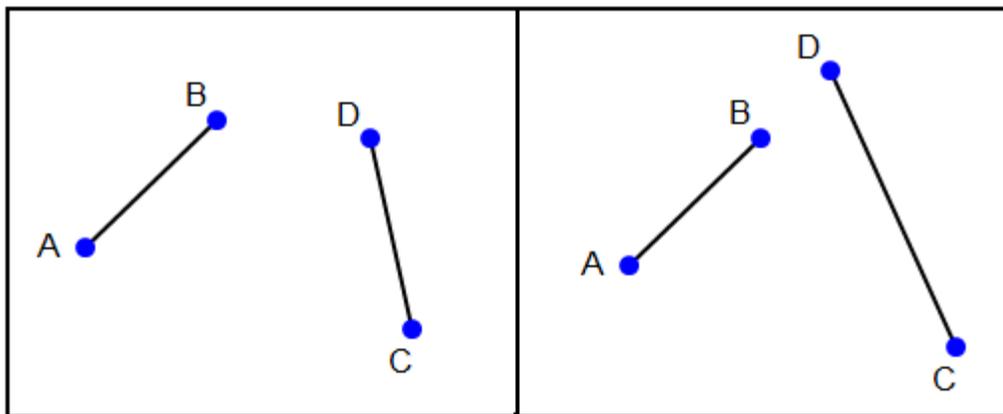
Incident Constraint



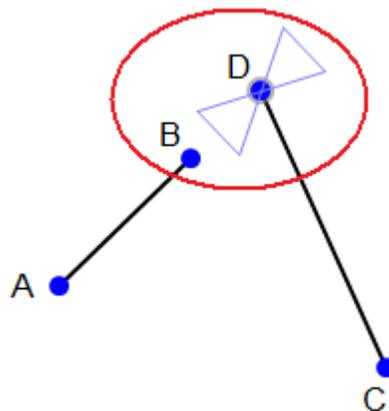
Constrain a point to be incident to any other geometry; line, segment, vector, polygon side, circle or locus with these steps:

1. [Select](#)  the point and the other geometry listed above.
2. Click the **Incident** icon  from the **Constrain** toolbox, or select **Incident** from the **Constrain** menu.

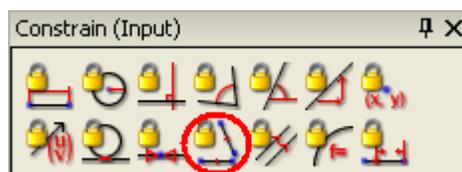
The point is moved to meet the line or curve, or the extension of the line. Below is an example of the latter, point D is moved to lie on the extension of line segment AB.



If you select the point or the line, incidence is indicated by a bowtie around the point:



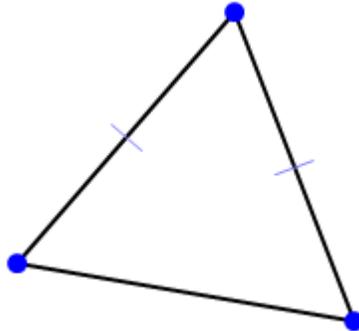
Congruent Constraint



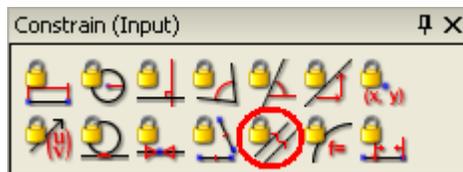
Constrain two or three of any of these geometry types: line segments, vectors, or polygon sides, to be congruent with these steps:

1. [Select](#)  two line segments.
2. Click the **Congruent** icon  from the **Constrain** toolbox, or select **Congruent** from the **Constrain** menu.

You will see matching congruency lines on the selected segments and a length will be adjusted.



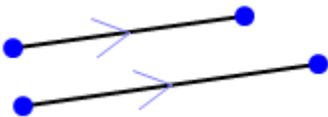
Parallel Constraint



Any two or three of the linear geometry types can be made parallel: line, segment, vector, or polygon side.

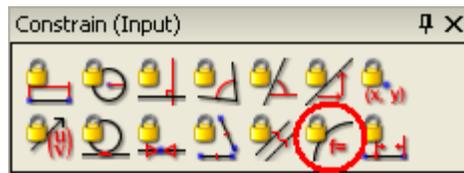
1. [Select](#)  two or three from the types listed above.
2. Click the **Parallel** icon  from the **Constrain** toolbox, or select **Parallel** from the **Constrain** menu.

The geometry will be adjusted and matching symbols



appear on the selected lines.

Implicit Equation Constraint

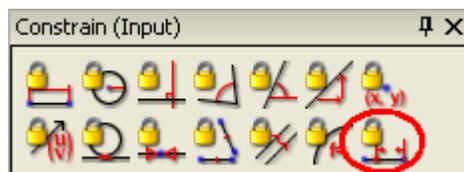


You can use symbolic variables to constrain geometry with an implicit equation. Lines, line segments, polygon sides, vectors and circles and conics can all be constrained with implicit equations.

1. [Select](#)  the geometry.
2. Click the **Implicit Equation** icon  from the **Constrain** toolbox, or select **Implicit Equation** from the **Constrain** menu.

An input window will open next to the geometry you selected. Highlighted in the window is a generic equation for the selected object; for a line, an equation like $-XA_1 + YB_1 + C_1 = 0$ might appear. You can edit the equation with different variable names or coefficients as you like. You will find these variables added to the variable list in the [Variables toolbox](#).

Point Proportional Along a Curve Constraint

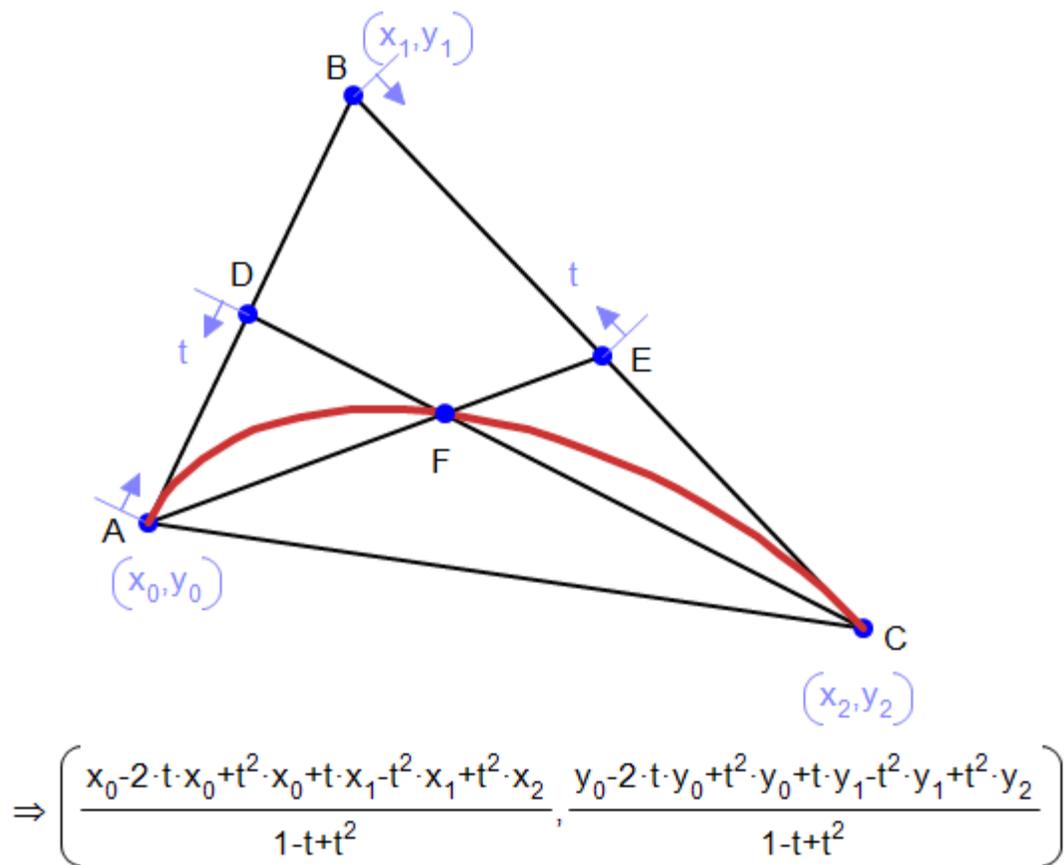


A point proportion t along a curve is defined variously for different types of curves as follows:

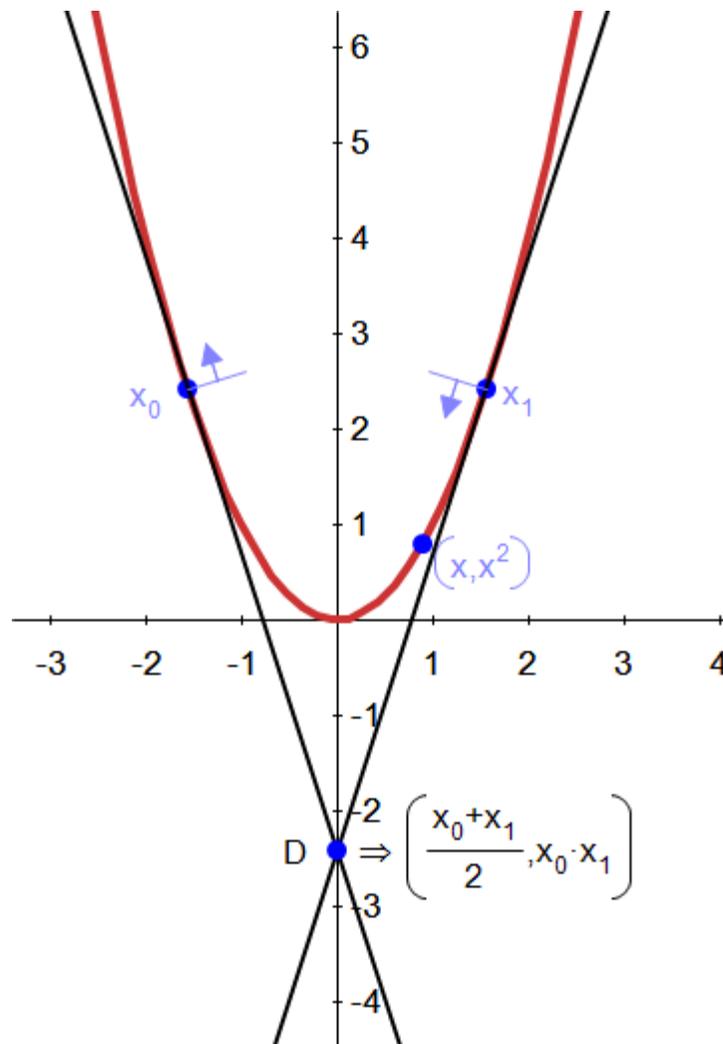
- For a **Line segment** AB , it defines the point $(1-t) \cdot A + t \cdot B$
- For a **Circle** it defines the point on the circle which subtends angle t at the center.
- For a **Locus** or envelope, it defines the point at parameter value t .
- For general **Cartesian** functions, it defines the x value of the point on the function.

- For **Polar** functions, it defines the point on the function which subtends angle t .
 - For general **Parametric** functions, it defines the point at parameter value t .
 - For an **Ellipse** of the form $X^2/a^2 + Y^2/b^2 = 1$ it defines the point $(a \cos(t), b \sin(t))$.
 - For a **Parabola** of the form $Y=X^2/4a$ it defines the point $(2at, at^2)$
 - For a **Hyperbola** of the form $X^2/a^2 - Y^2/b^2 = 1$ it defines the point $(a/\cos(t), (b \sin(t))/\cos(t))$.
1. [Select](#)  a point and one of the curves mentioned above.
 2. Click the **Point Proportional** icon  from the **Constrain** toolbox, or select **Point Proportional** from the **Constrain** menu.
 3. Enter the parameter or quantity (symbolic or real) in the data entry box.

For example, in the following diagram, D is defined proportion t along AB, and E is defined proportion t along BC. The curve is the locus of F as t varies between 0 and 1.



In the following example, the curve is the locus of the point (x, x^2) . Tangents are created at points with parameter values x_0 and x_1 on this curve.

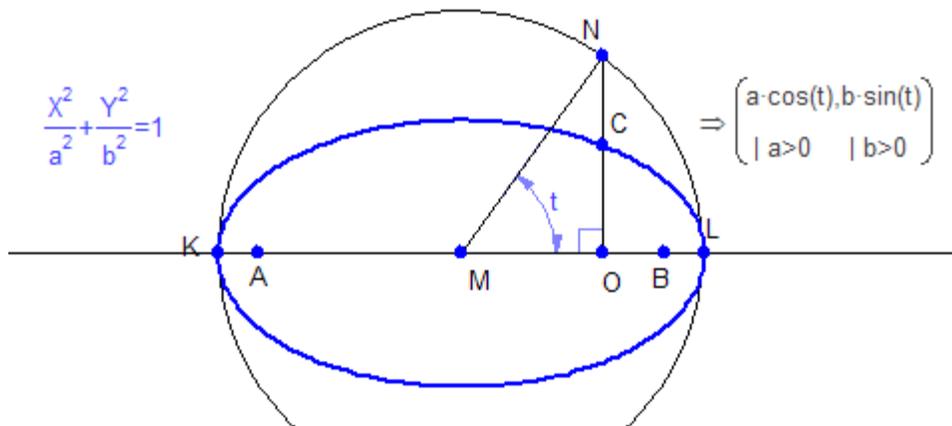


Where is Point proportional along curve for conics?

The best way to understand the location of **Point proportional along curve** command for conics is to see how we construct it geometrically for each conic:

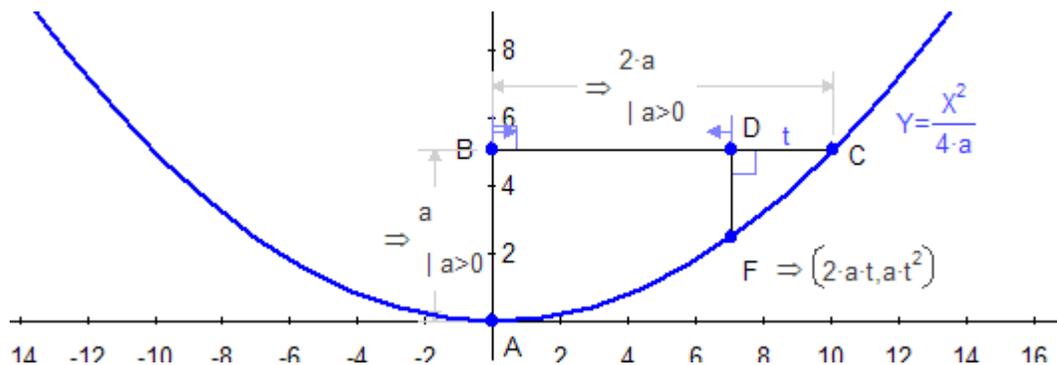
Ellipse

The ellipse with foci A and B is inscribed in circle, center M. Draw the radius MN at angle t to the major axis and drop the segment NO perpendicular to the major axis of the ellipse. When the intersection of NO with the ellipse (point C) is constrained to be t proportional along the ellipse, its coordinates will be $(a \cos(t), b \sin(t))$.



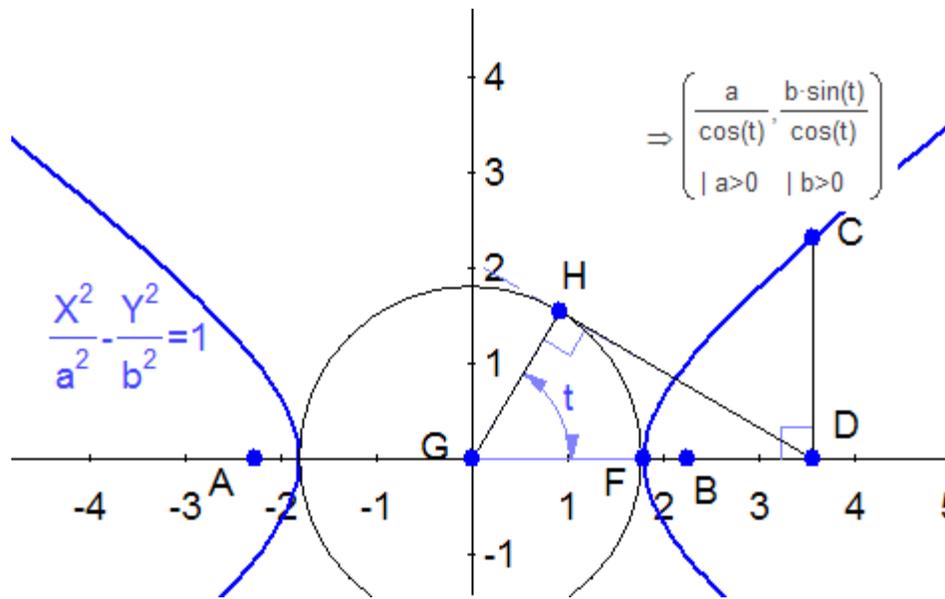
Parabola

C lies on the parabola and BC is perpendicular to the axis AB of the parabola. Point D is located proportion t along the segment. Point F is the intersection of the perpendicular to BC through D with the parabola. It has the coordinates $(2at, at^2)$ when it is constrained to parametric location t on this parabola.



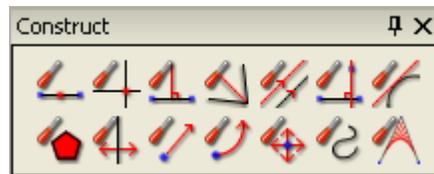
Hyperbola

CD is the perpendicular projection of C onto the axis of the hyperbola, GF is the circle centered at the center of the hyperbola which goes through the intersections of the hyperbola with its axis. H is the point of contact of this circle with the tangent from D. We can see that the angle DGH is the same as the parameter value. When point C is constrained to be at parametric location t along the curve, its coordinates are $(a/\cos(t), b \sin(t)/\cos(t))$ on this hyperbola.



Constructions

Creating Constructions



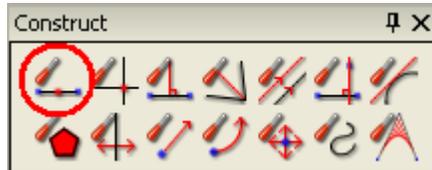
After sketching and constraining your drawing there are a whole set of constructions that can be applied to the geometry. First you must select the geometry elements which pertain to the construction. When you select the geometry the appropriate constructions will be highlighted.

The following table lists the **Constructions**, their icons, and which elements must be preselected to activate the constructions. Be careful when selecting geometry objects, if extra things are selected that are not related to the construction, the construction icons will remain inactive. This can happen by mistake, especially when using the [selection box tool](#).

	Construction	Preselected Objects
	<u>Midpoint</u>	A line segment, vector, or polygon side.
	<u>Intersection</u>	Two of: a line, segment, vector, polygon side or conic. Conics are limited to intersecting only with lines, segments and vectors.
	<u>Perpendicular Bisector</u>	A line segment, vector, or polygon side.
	<u>Angle Bisector</u>	Two of: a line, segment, vector, or polygon side.
	<u>Parallel</u>	A point and one of: a line, segment, vector, or polygon side.
	<u>Perpendicular</u>	A point and one of: a line, segment, vector, or polygon side.
	<u>Tangent</u>	A circle or curve, and optionally, a point on the curve
	<u>Polygon</u>	Three or more connected line segments or points (vertices) to form a polygon
	<u>Reflection</u>	One or more objects
	<u>Translation</u>	One or more objects
	<u>Rotation</u>	One or more objects
	<u>Dilation</u>	One or more objects
	<u>Locus</u>	A point or line that will vary with a parameter

	Trace	One or more objects that will vary with a parameter
	Area Under Arc	An arc of a Cartesian function

Midpoints of Line Segments

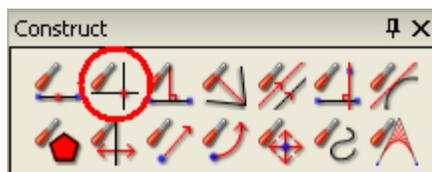


You can construct a midpoint on any line segment, vector, polygon side, or between two points by:

1. [Select](#)  two from the geometry types listed above.
2. Click the **Midpoint** tool , or select **Midpoint** from the **Construct** menu.

A point will appear in the middle of the selected line.

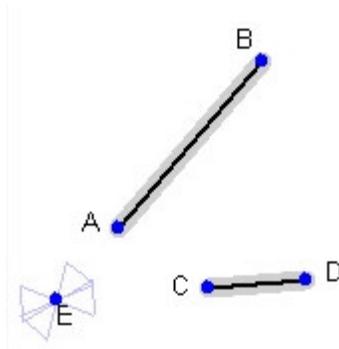
Intersections



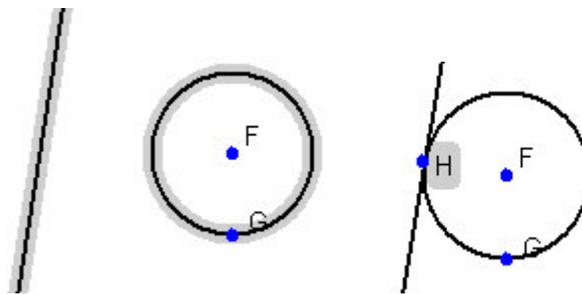
You can construct a point of intersection between any of the line types in your geometry; line, segment, vector, polygon side or circle. You can also construct intersections of circles. Conics are limited to intersections only with lines, segments or vectors.

1. [Select](#)  two from the line types listed above.
2. Click the **Intersection** tool  or select **Intersection** from the **Construct** menu.

A new point and label will appear at the intersection. If the lines are segments that do not intersect, a point will be created at the extension of the lines as with line segments AB and CD below.



If the geometry will never intersect, the selected objects are moved to form the intersection. In the example below, the infinite line and circle become tangent at the newly created point, H.



Perpendicular Bisector

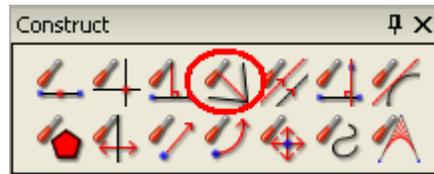


You can construct a perpendicular bisector on any line, segment, vector, or polygon side with these steps:

1. [Select](#)  any of the line types listed above.
2. Click the **Perpendicular Bisector** tool  or select **Perpendicular Bisector** from the **Construct** menu.

An infinite line will appear at right angles to the selected line.

Angle Bisector

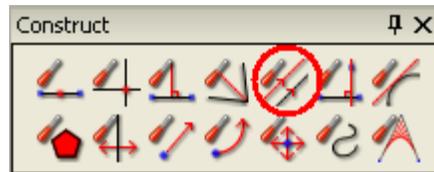


You can bisect the angle between any combination of line types; line, segment, vector, or polygon side with these steps:

1. [Select](#)  two of any of the line types listed above.
2. Click the **Angle Bisector** tool  or select **Angle Bisector** from the **Construct** menu.

An infinite line will appear between the two selected lines. You can use the [Calculate / Angle tool](#) to get the value of the bisected angle.

Parallel Constructions

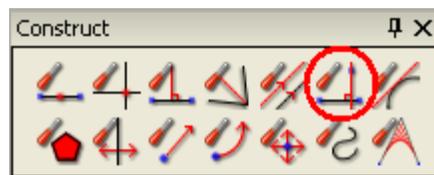


You can construct a line, through a point, and parallel to another line, segment, polygon side or vector with these steps:

1. [Select](#)  a point and a line of one of the types listed above.
2. Click the **Parallel** tool  or select **Parallel** from the **Construct** menu.

A line is constructed which is parallel to the selected line and passes through the selected point.

Perpendicular Constructions

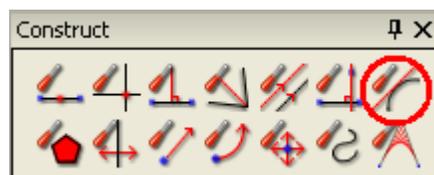


You can construct a line, through a point, which is perpendicular to another line, segment, polygon side or vector with these steps:

1. [Select](#)  a point and a line of one of the types listed above.
2. Click the **Perpendicular** tool  or select **Perpendicular** from the **Construct** menu.

A line is constructed which is perpendicular to the selected line and passes through the selected point.

Tangents

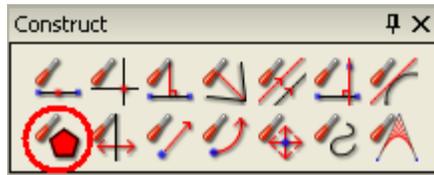


You can construct a line that is tangent to a circle or curve with these steps:

1. [Select](#)  the circle or curve. You can also select a point on the curve so that the tangent goes through the point on the curve.
2. Click the **Tangent** tool  or select **Tangent** from the **Construct** menu.

A line tangent to the selected curve will appear at the point where you selected the circle or curve, or at the selected point.

Polygon Construction

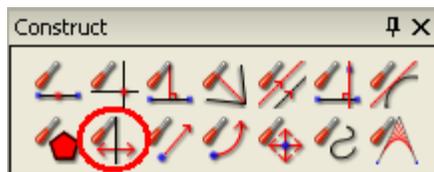


If you created a polygon with the [line segment tool](#), or your polygon was not shaded for some reason, (e.g. the drawing of the sides was interrupted or out of order) you can make joined line segments into a polygon that can be selected with a single click using this construction.

1. [Select](#)  the line segments that make up the polygon.
2. Click the **Polygon** tool  in the **Construct** toolbox, or select **Polygon** from the **Construct** menu.

The polygon will be filled and you can now select the entire polygon with a single click.

Reflection



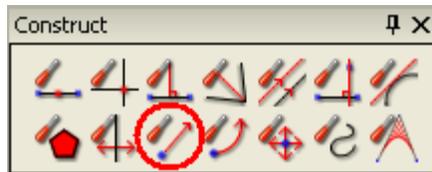
You can reflect any subset of your diagram about a line with these steps:

1. [Select](#)  one or more geometry objects to reflect.
2. Click the **Reflection** tool  in the **Construct** toolbox, or select **Reflection** from the **Construct** menu.
3. Either click the cursor to place the reflection line on the screen, adjust the angle and click again, or select an existing line as the reflection line.

A copy of your selected geometry will appear on the other side of the reflection line.

Notice all points on the reflected geometry are written as "prime", *i.e.* A becomes A'. If you reflect the geometry again, A' becomes A".

Translation



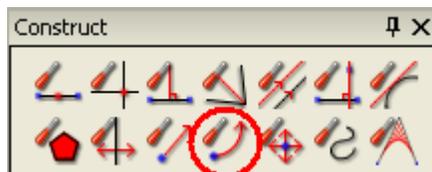
You can translate any subset of your diagram with a translation vector. Here are the steps:

1. [Select](#)  the geometry to be translated.
2. Click the **Translation** tool  in the **Construct** toolbox, or select **Translation** from the **Construct** menu.
3. Click the cursor to draw the end point of your translation vector and move the cursor to establish the length and angle of the translation. Click again to finish the vector.

The translated geometry appears. You can adjust the position of the translation by clicking and dragging the tip of the vector.

Notice all points on the translated geometry are written as "prime", *i.e.* A becomes A'. If you translate this geometry again, A' becomes A".

Rotation



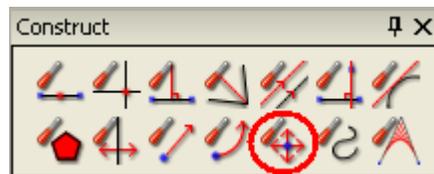
You can rotate any subset of your diagram about a point. Here are the steps:

1. [Select](#)  the geometry to be rotated.
2. Click the **Rotation** tool  in the **Construct** toolbox, or select **Rotation** from the **Construct** menu.
3. Click the screen to place your rotation point.
4. In the data entry box presented, enter the angle of rotation.

The rotation of the selected geometry appears.

Notice all points on the rotated geometry are written as "prime", *i.e.* A becomes A'. If you rotate this geometry again, A' becomes A''.

Dilation



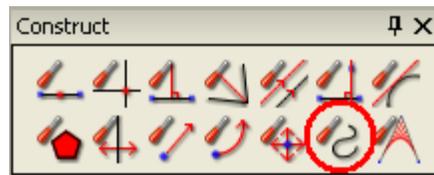
You can dilate any subset of your diagram from a point. Here are the steps:

1. [Select](#)  the geometry to be dilated.
2. Click the **Dilation** tool  in the **Construct** toolbox, or select **Dilation** from the **Construct** menu.
3. Click the cursor on your dilation point.
4. In the data entry box presented, enter the dilation factor.

The dilated geometry appears.

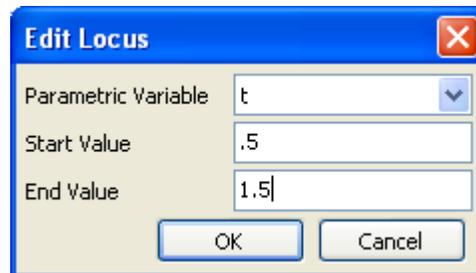
Notice all points on the dilated geometry are written as "prime", *i.e.* A becomes A'. If you dilate this geometry again, A' becomes A''.

Locus of Points / Envelope

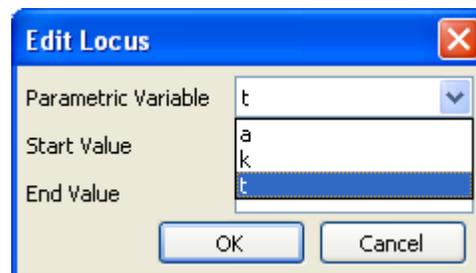


You can construct a locus of points or envelope from a selected point or line, by defining a range for some constraint in the drawing. Just follow these easy steps:

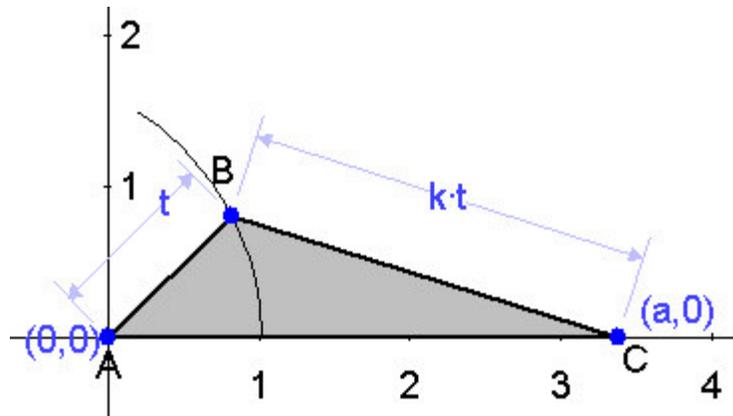
1. **Select**  the point on the drawing that will form the locus (point B in the example below); select a line, line segment, or vector to form an envelope.
2. When you click the **Locus** icon , the **Edit Locus** dialog pops up.



3. You need a parameter to drive the motion to create the locus. Click the arrow key to the right of the **Parametric Variable** window to select from a list of all variables in the drawing. (If you entered the needed constraint in real terms, Cancel the trace and change the constraint to a variable by double-clicking it in the drawing window.)



4. Simply fill in the values for the appropriate variable and click the Ok button.



! Note: The locus only works if the figure's position is fixed i.e. a point in a triangle will not work as a locus unless the location of the other two points are fixed with coordinate constraints.

To adjust the range of the locus, double-click the locus to edit the dialog.

The following example shows an envelope of the line DE. We use the [Point proportional along curve constraint](#) and the parameter t to position the points D and E (D is $(1-t)$ along line AC and E is t along line AB). In the **Edit Locus** dialog, we create the envelope from parameter t as it ranges from 0 to 1.

The screenshot shows the software interface for creating a locus. The main workspace displays a triangle ABC with vertices A, B, and C. A red curve is shown, and a yellow line segment DE is shown. The parameter t is used to position D and E. The software interface includes a toolbar, a Variables panel, and a dialog box for editing the locus.

The Variables panel shows the following table:

Name	Value	Locked
t	0.38	-

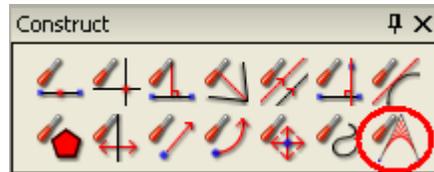
The dialog box for editing the locus shows the following values:

Start: 0, End: 4, Step: 1

The status bar at the bottom shows the current selection: (5.66519, -0.903215) in Radians.

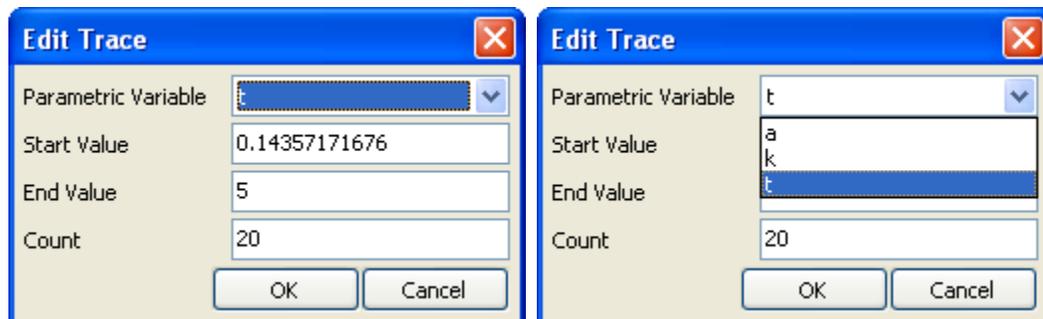
You can replay the creation of the envelope with the [Animation tools](#). Select variable t and click the Play button.

Trace

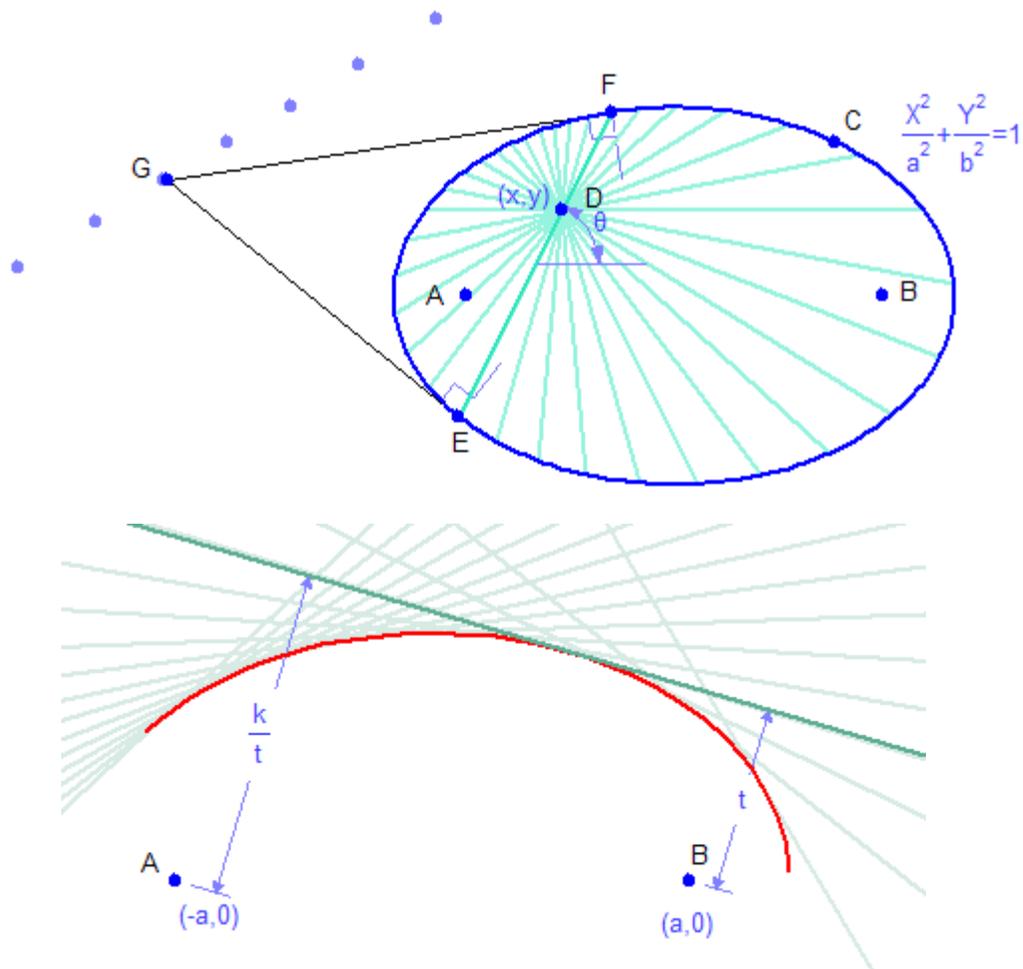


You can **Trace** the movement of one or a group of drawing objects. You can create string art drawings and see how an envelope curve is formed. Here are the steps:

1. [Select](#)  the drawing objects to be traced.
2. Click the **Trace** tool  and the **Edit Trace** dialog pops up.
3. You need a parameter to drive the motion of the trace. Click the arrow key to the right of the **Parametric Variable** window to select from a list of all variables in the drawing. (If you entered the needed constraint in real terms, Cancel the trace and change your constraint to a variable by double-clicking it in the drawing window.)



4. Simply fill in the values for the appropriate variable and click the OK button.



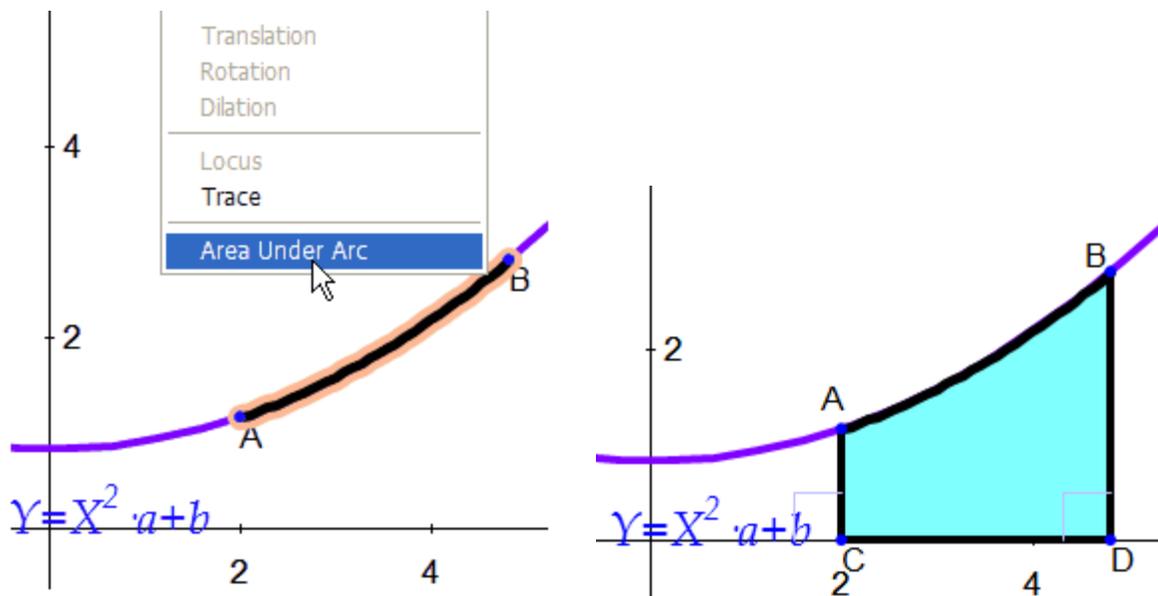
To adjust the range or number of traces, double-click one of the traces to edit the dialog.

Area Under the Arc

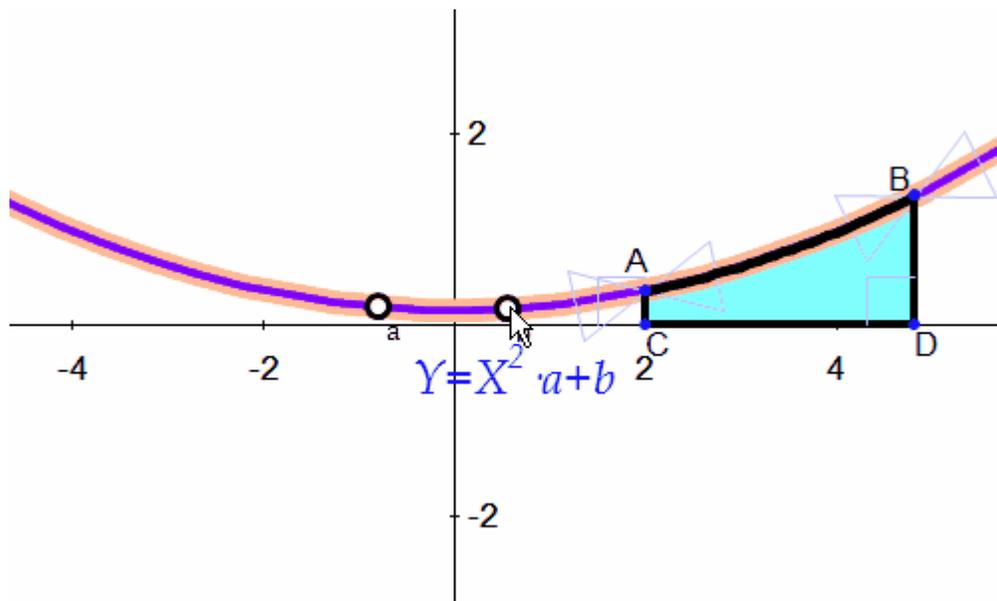
The **Area Under Arc** function is found only in the **Construct** menu at the top of the main window. Here are the steps:

1. Select an [arc](#) drawn over a function.
2. Select **Construct / Area Under Arc**.

A filled area is created between the arc and the X axis. The necessary lines and points containing the area are automatically added.



Drag the handles of the original function and the area under the curve changes accordingly.



This is a great way to illustrate the [definite integral](#).

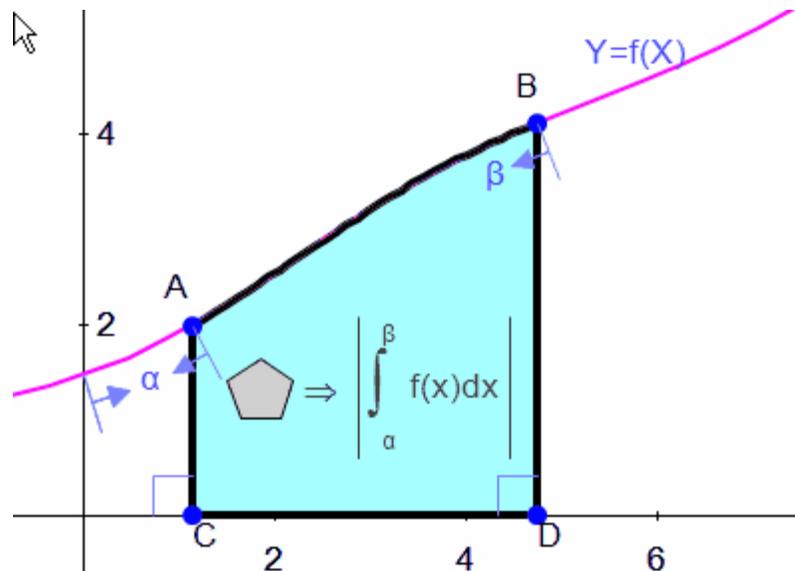
Note: this only works for arcs drawn on functions. For arcs drawn on conics, create the sides with the **Draw / Line Segment**, select all sides and use the [Construct / Polygon](#) tool. See also: instructions for creating [curvilinear polygons](#).

Integral Calculus

The **Area Under Arc** function is a great way to show problems with the definite integral.

Here are the steps for making the integral of the generic function $f(x)$ over the interval α to β :

1. Select the [Draw / Function](#) tool and enter $f(x)$ in the Y= data entry box. Click OK.
2. Use the [Draw / Arc](#) tool to trace over some portion of the function.
3. Select the new arc - be careful not to select the whole function. Just the section of arc should be highlighted.
4. Choose [Area Under Arc](#) from the **Construct** menu. The area between the arc and the X axis will be filled.
5. For each endpoint of the arc, use the [Constrain / Point proportional along curve](#) tool to define the limits of the region, e.g. select α and β from the [Symbols](#) toolbox.
6. Select the area under the arc and click [Calculate / Symbolic / Area](#).



Annotations

Applying Annotations

Annotations allow you to add constraint information to your drawing which isn't needed for its construction. These might be constraints that cause the geometry to be over constrained, but you might want to give the viewer some additional information. This feature can be very helpful for making up texts or worksheets.

Annotate tools are similar to [Text](#) in that they have no influence on the geometry engine, even though they are placed exactly like the [Constrain](#) tools.

Since annotations may look identical to constraints, use the icon from icon

bar  at the top of the window to **Distinguish Constraints / Annotations**. The icon is a toggle; to turn off the marks, click it again.

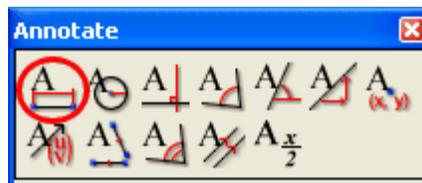
The [Symbols](#) and **Annotation Symbols** toolboxes are both available to the **Annotate** tools.

Here are the **Annotate** tools and the object(s) to preselect:

	Annotation	Preselected Object(s)
	Distance / Length	A line segment, vector, or polygon side, or a point and one of these line types (perpendicular distance), or two points.
	Radius	Circle
	Perpendicular	Two of any line, segment, vector, or polygon side.
	Angle	Two of any line, segment, vector, or polygon side.

	Direction	A line, segment, vector, or polygon side.
	Slope	A line, segment, vector, or polygon side.
	Coordinates	Point
	Coefficients	Vector
	Congruent	A line, segment, vector, or polygon side.
	Congruent Angle	Two of any lines, segments, vectors, or polygon sides
	Parallel	A line, segment, vector, or polygon side.
	Expression	[none]

Distance / Length Annotation

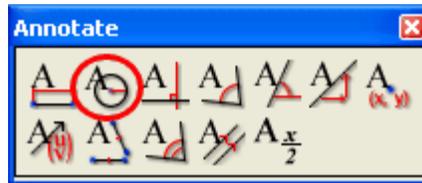


Length annotations may be applied to any line, segment, polygon side or vector. Distance annotations are available between two points, or the perpendicular distance between a point and a line, segment, polygon side, or vector. Use these steps:

1. [Select](#)  the line segment, or point and line, or pair of points as described above. When you make your selection, the drawing objects will be highlighted and the **Distance / Length** icon will light up .
2. Click the icon
3. Enter the distance information. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

You can click the annotation and drag it to adjust its placement in the drawing.

Radius Annotation

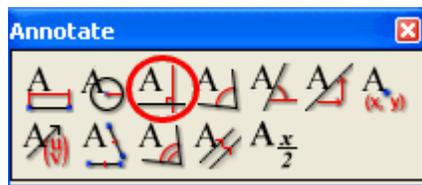


To annotate a circle's radius use these steps:

1. [Select](#)  the circle. The **Annotate / Radius** icon  will light up and the circle will be highlighted.
2. Click the icon
3. Enter the radius information. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

You can click the annotation and drag it to adjust its placement in the drawing.

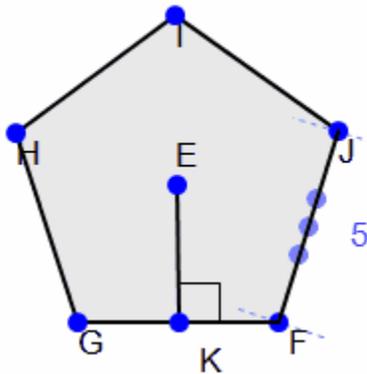
Perpendicular Annotation



The perpendicular annotation inserts the perpendicular mark between any two of these line types: line, segment, polygon side or vector. Use these steps:

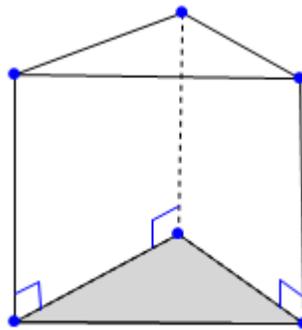
1. [Select](#)  two of any line, segment, vector, or polygon side. The **Annotate / Perpendicular** icon  will light up when both lines are highlighted.

2. Click the icon.

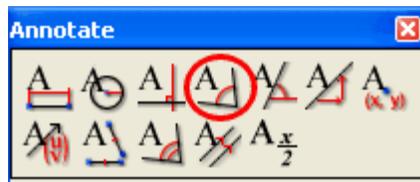


Note: Placing this annotation between two lines does not change the relative position of the lines or prevent the lines from changing their relative position as it does with the **Constrain** tool of the same name.

This annotation is very useful if you are displaying a 3-d object. In this example we imported the Triangular Prism from the **Solids** folder in the Figure Gallery.



Angle Annotation



To annotate an angle use these steps:

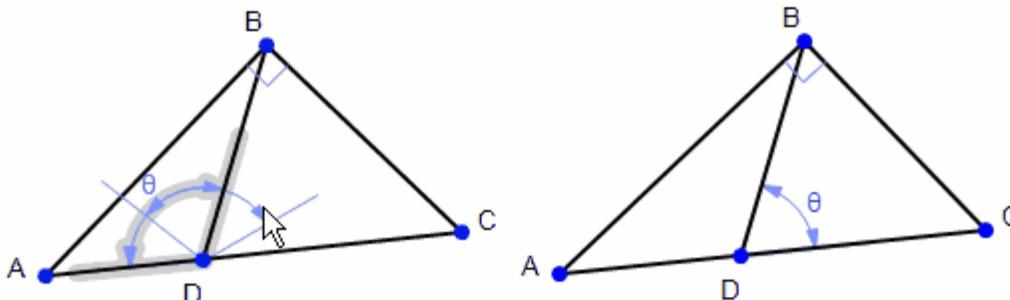
1. Select  two of any line, segment, vector, or polygon side. The

Annotate / Angle icon  will light up and the lines will be highlighted.

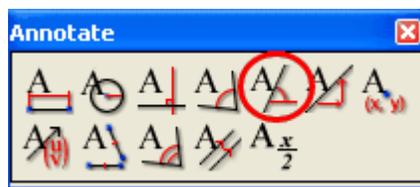
2. Click the icon
3. Enter the angle information. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

Which Side to Annotate?

Sometimes when identifying angles, the annotation falls on the wrong one. In the example below, we wanted BDC, not BDA. Just click the cursor over the annotation arrow and drag it to the other side, then release the mouse button - done!



Direction Annotation

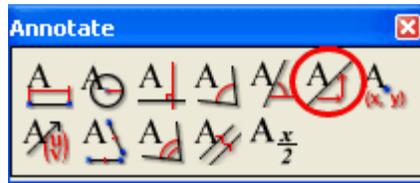


To annotate a line's direction use these steps:

1. [Select](#)  a line, segment, vector, or polygon side. The **Annotate / Direction** icon  will light up and the line will be highlighted.
2. Click the icon
3. Enter the direction information. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

You can click the annotation and drag it to adjust its placement in the drawing.

Slope Annotation

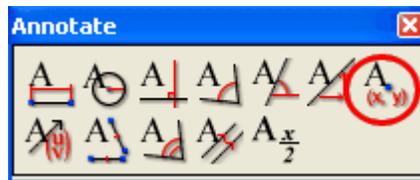


To annotate a line's slope use these steps:

1. [Select](#)  a line, segment, vector, or polygon side. The **Annotate / Slope** icon  will light up and the line will be highlighted.
2. Click the icon
3. Enter the slope information. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

You can click the annotation and drag it to adjust its placement in the drawing.

Coordinate Annotation



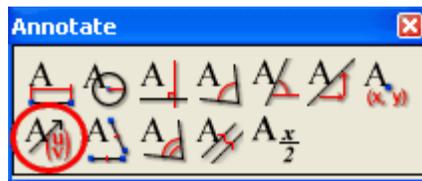
To annotate an point's coordinates use these steps:

1. [Select](#)  point. The **Annotate / Coordinate** icon  will light up and the point will be highlighted.
2. Click the icon
3. Enter the coordinate information. There are no format restrictions.

You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

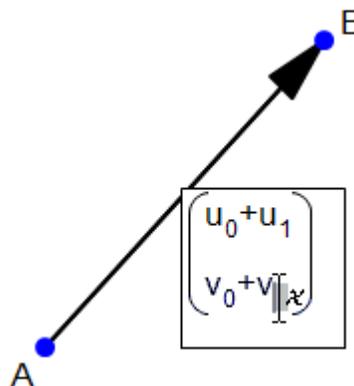
You can click the annotation and drag it to adjust its placement in the drawing.

Coefficients Annotation



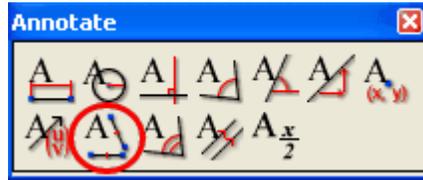
To annotate a vector's coefficients use these steps:

1. [Select](#)  vector. The **Annotate / Coefficients** icon  will light up and the vector will be highlighted.
2. Click the icon
3. Enter the vector's coefficients. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.



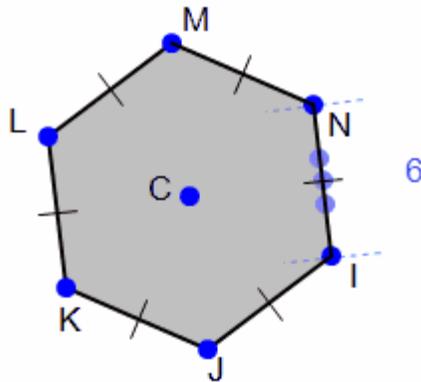
You can click the annotation and drag it to adjust its placement in the drawing.

Congruent Annotation



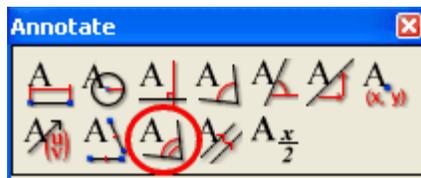
Place a congruent mark on any of the linear drawing elements: lines, segments, vectors, or polygon sides. Use these steps:

1. [Select](#)  any line, segment, vector, or polygon side. The **Annotate / Congruent** icon  will light up when both lines are highlighted.
2. Click the icon.



Note: Placing this annotation on lines does not change the relative lengths of the lines or keep them the same length as it does with the **Constrain** tool of the same name.

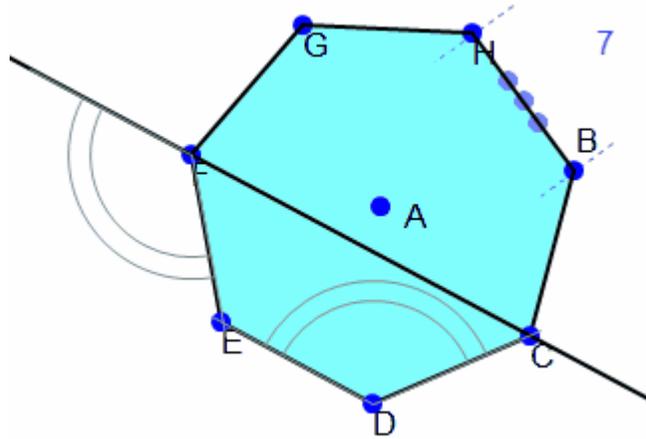
Congruent Angle Annotation



Place a congruent mark between pairs of linear drawing elements: lines,

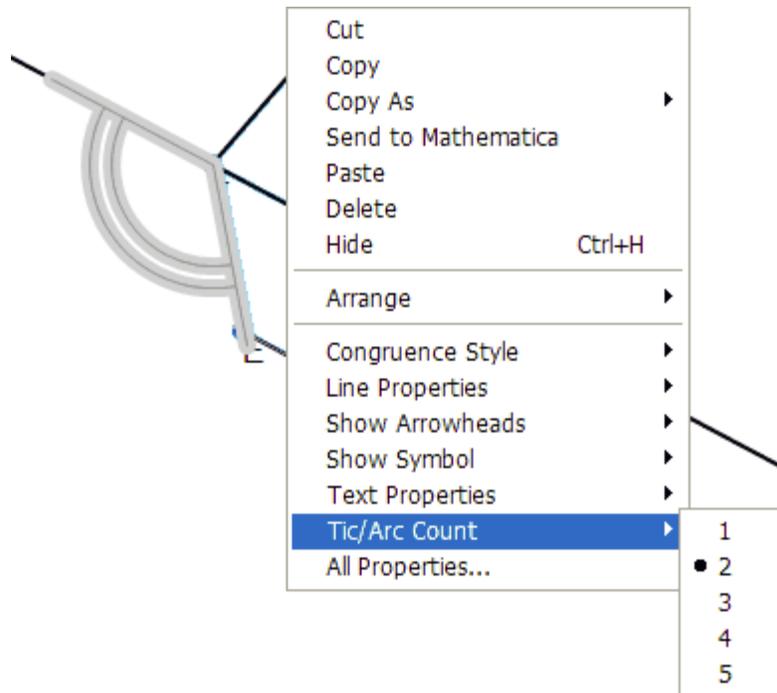
segments, vectors, or polygon sides. Use these steps:

1. [Select](#)  two lines, segments, vectors, or polygon sides. The **Annotate / Congruent Angle** icon  will light up when both lines are highlighted.
2. Click the icon.

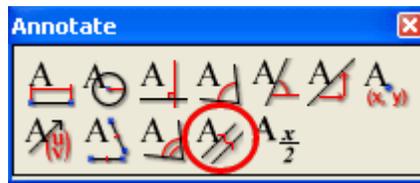


You can change the arc count with these steps:

1. Select the annotation.
2. Right click to invoke the [selection Context menu](#).
3. Select **Tic/Arc Count** from the menu and click the desired number.

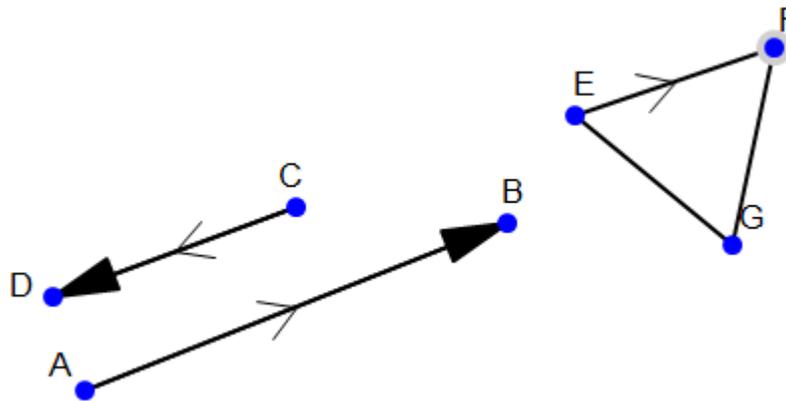


Parallel Annotation



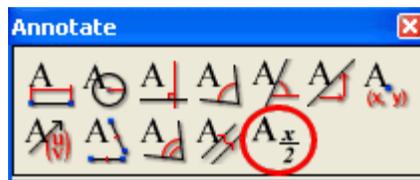
Place a parallel mark on any of the linear drawing elements: lines, segments, vectors, or polygon sides. Use these steps:

1. [Select](#)  any line, segment, vector, or polygon side. The **Annotate / Perpendicular** icon  will light up when both lines are highlighted.
2. Click the icon.



Note: Placing this annotation on lines does not change the relative position of the lines or prevent the lines from changing their relative position as it does with the **Constrain** tool of the same name.

Expression Annotation



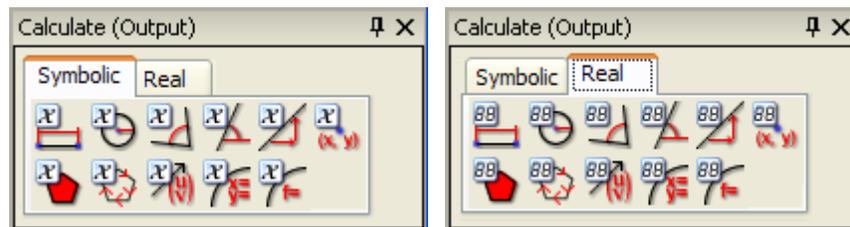
The **Annotate** / **Expression** command is useful for placing a line of mathematics anywhere in your drawing.

1. Click the icon $A_{\frac{x}{2}}$.
2. Move the cursor to the position where you want to place the expression and click.
3. Enter the expression. There are no format restrictions. You can use [Symbols](#) and [Annotation Symbols](#) in the entry. Press enter when you're done.

You can click the annotation box and drag it to adjust its placement in the drawing.

Calculations

Calculating the Output



Mechanical Expressions will make calculations in the geometry based on any constraints or constructions you have specified, or just from the sketch. Calculations can be output in **Real** or **Symbolic** terms by choosing the appropriate tab.

If you haven't supplied all of the necessary input constraints, the system inserts any missing variables automatically or, for real calculations, bases the value on the sketch.

Some calculations may take longer than you expected. If the calculation isn't immediate, you can stop it and restart it with these buttons on the tool bar.



Stop calculations



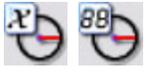
Start calculations.

You may want to reconsider the problem, add constraints, or just let it continue with the calculation.

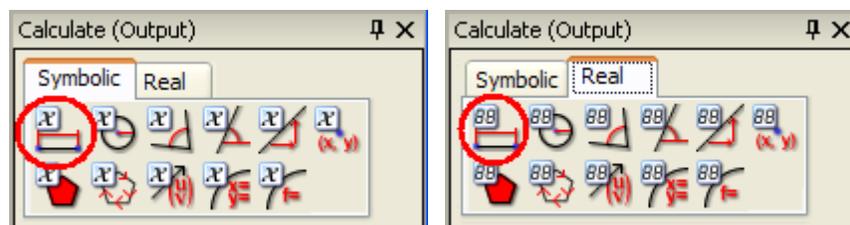
The **Stop calculations** and **Start calculations** can also be found under **Calculate (Output)** menu and under the [general context menu](#).

The table below lists all the available calculations and geometry elements which must be preselected. Be careful when selecting geometry objects, if extra things are selected that are not related to the calculation (like other calculations) the calculations will remain inactive. This can happen by mistake, especially when using the selection rectangle.

	Calculation	Preselected Object(s)
--	-------------	-----------------------

	Distance / Length	A line segment, vector, or polygon side, or a point and one of these line types (perpendicular distance), or two points.
	Radius	Circle
	Angle	Two of any line, segment, vector, or polygon side.
	Direction	A line, segment, vector, or polygon side.
	Slope	A line, segment, vector, or polygon side.
	Coordinates	Point
	Area	Circle or polygon
	Perimeter	Circle or polygon
	Coefficients	Vector
	Parametric Equation	A line, segment, vector, polygon side, circle, or a constructed locus.
	Implicit Equation	A line, segment, vector, polygon side, circle, or a constructed locus.

Distance / Length Calculation



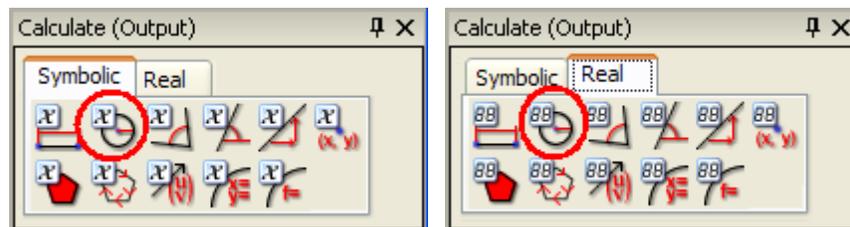
Length calculations may be obtained for any line segment, polygon side or

vector. Distance calculations are available between two points, or the perpendicular distance between a point and a line, segment, polygon side, or vector. Use these steps:

1. [Select](#)  the line segment, or point and line, or pair of points as described above.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Distance / Length** tool in the **Calculate** toolbox or select **Distance / Length** from the **Calculate** menu.

Mechanical Expressions displays the length, using any relevant parameters you may have specified.

Radius Calculation

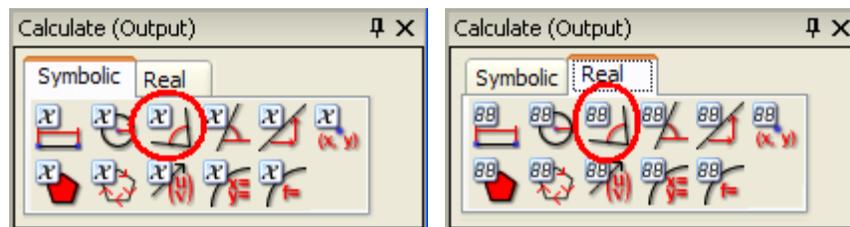


Mechanical Expressions will calculate the radius of any circle. Use these steps to find the radius:

1. [Select](#)  a circle.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Radius** tool in the **Calculate** toolbox or select **Radius** from the **Calculate** menu.

The equation with real or symbolic terms appears in the diagram.

Angle Calculation



Mechanical Expressions will calculate any angle between lines in the geometry. Use these steps to find the angle:

1. [Select](#)  two line types - any line, segment, vector, or polygon side.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Angle** tool in the **Calculate** toolbox or select **Angle** from the **Calculate** menu.

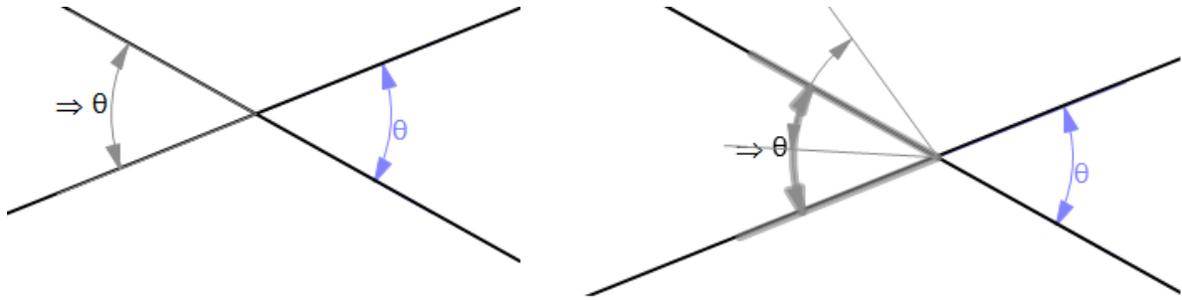
The equation with real or symbolic terms appears in the diagram.

You can obtain [the angle's supplement](#) by dragging the angle symbol.

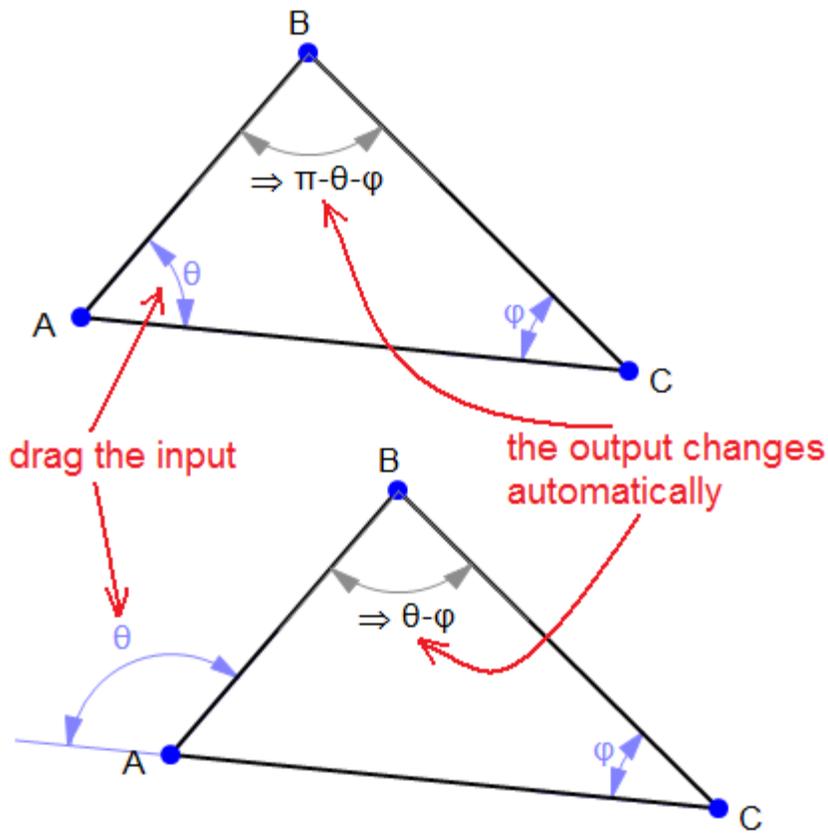
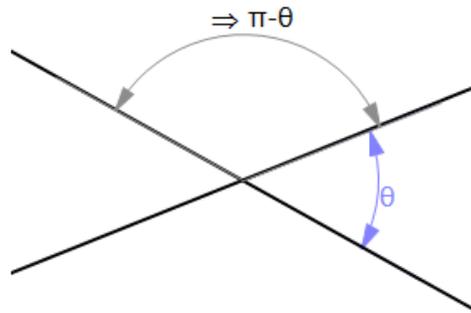
Supplementary Angles

If it's unclear whether a calculation is requested for the angle or its supplement, you can drag the angle symbol to the correct position.

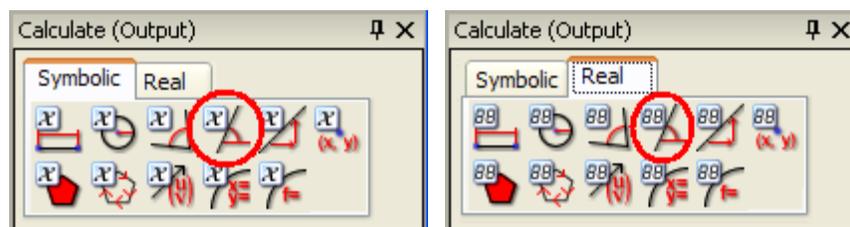
Here are some examples of playing around with supplementary angles (inputs, outputs and angle annotations all have this feature):



Select and drag to get the supplement angle



Direction Calculation

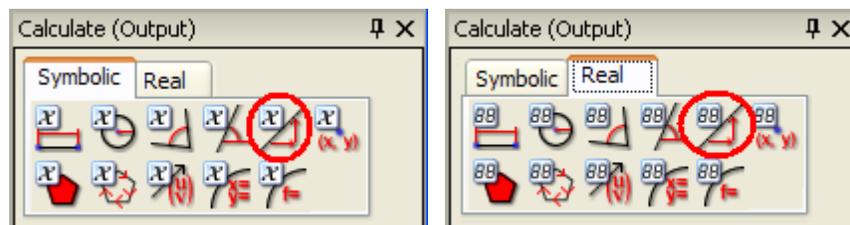


Mechanical Expressions will calculate the direction of lines, segments, polygon sides, or vectors with these steps:

1. [Select](#)  a line type.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Direction** tool in the **Calculate** toolbox or select **Direction** from the **Calculate** menu.

The direction measurement appears in real or symbolic terms.

Slope Calculation

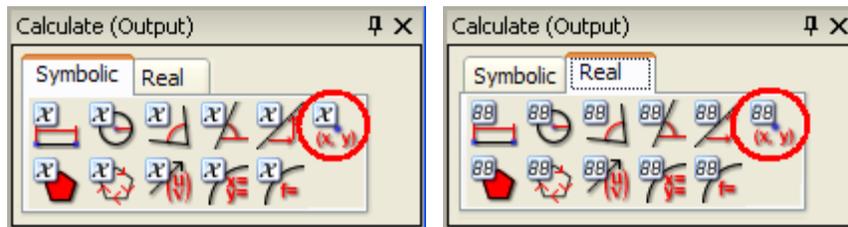


Mechanical Expressions will calculate the slope of lines, segments, polygon sides, or vectors with these steps:

1. [Select](#)  a line type.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Slope** tool in the **Calculate** toolbox or select **Slope** from the **Calculate** menu.

The equation for the slope with real or symbolic terms appears in the diagram.

Coordinates Calculation

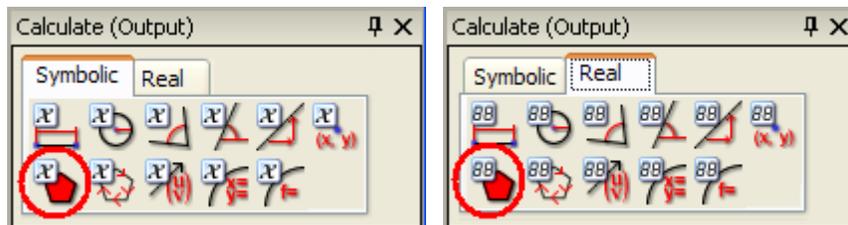


You can calculate the coordinates of any point in your diagram with these steps:

1. [Select](#)  a point.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Coordinates** tool in the **Calculate** toolbox or select **Coordinates** from the **Calculate** menu.

The real or symbolic coordinates appear by the point.

Area Calculation



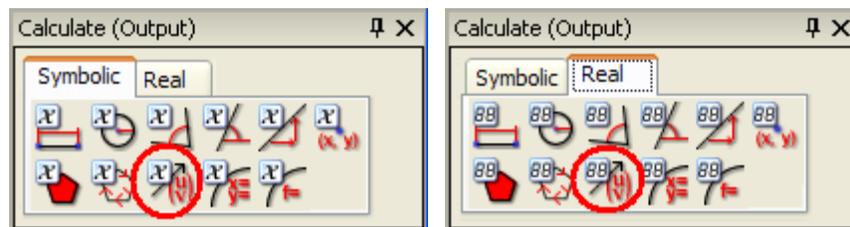
You can obtain the area of any polygon or circle in your diagram.

Note: If your polygon is not filled it is just a group of line segments. To convert them to a polygon, use the [Polygon Construction](#) tool, then proceed with these steps:

1. [Select](#)  a circle or polygon.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Area** tool in the **Calculate** toolbox or select **Area** from the **Calculate** menu.

The area is displayed in real or symbolic terms.

Coefficients Calculation

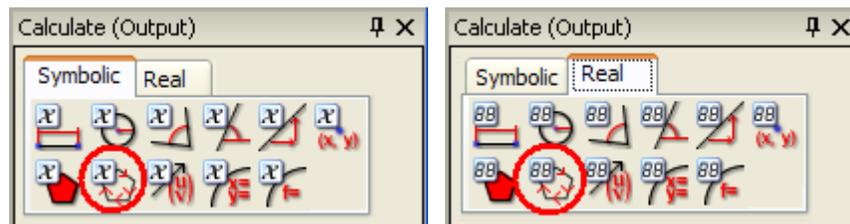


Use this tool to calculate the coefficients of a vector in the diagram with these steps:

1. [Select](#)  a vector.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Coefficients** tool in the **Calculate** toolbox or select **Coefficients** from the **Calculate** menu.

The real or symbolic coefficients appear by the vector.

Perimeter Calculation



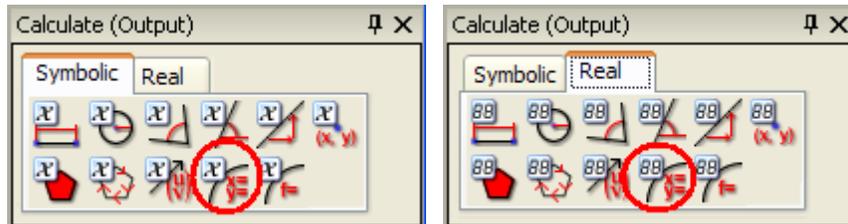
You can obtain the perimeter of any polygon or circle in your diagram.

Note: If your polygon is not filled it is just a group of line segments. To convert them to a polygon, use the [Polygon Construction](#) tool, then proceed with these steps:

1. [Select](#)  a circle or polygon.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Perimeter** tool in the **Calculate** toolbox or select **Perimeter** from the **Calculate** menu.

The perimeter is displayed in real or symbolic terms.

Calculating Parametric Equations



Computes parametric equations for a locus or envelope, based on the parameter defining the curve.

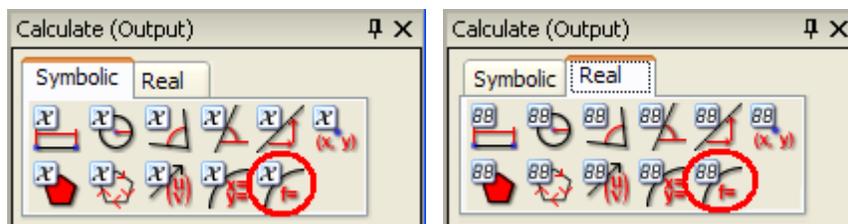
You can also calculate parametric equations for a circle or line.

Use these steps:

1. [Select](#)  any geometry object described above.
2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Parametric Equation** tool in the **Calculate** toolbox or select **Parametric Equation** from the **Calculate** menu.

The real or symbolic equations for x and y appear by the geometry.

Calculating Implicit Equation



Calculates the implicit equation for the selected circle or a line.

Mechanical Expressions will also attempt to calculate the equation of a locus or envelope curve.

1. [Select](#)  any geometry object described above.

2. Click the tab to switch from Real to Symbolic output or *vice versa*.
3. Click the **Implicit Equation** tool in the **Calculate** toolbox or select **Implicit Equation** from the **Calculate** menu.

The real or symbolic equation appears by the geometry.

Mechanics Inputs

Applying Mechanics Inputs



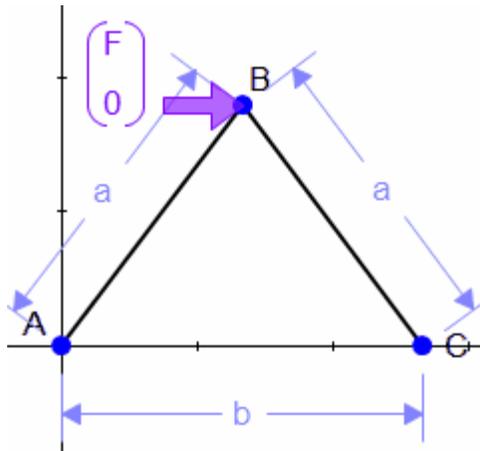
There are a number of Mechanics inputs you can apply to your drawing. Initially, all the inputs in the toolbox are inactive. You must first select the element in your model connected to the desired input. The following table lists all the Mechanics inputs and the elements you must preselect.

	Mechanics Input	Preselected Object
	<u>Applied Force</u>	A point or a vector
	<u>Applied Torque</u>	A line segment
	<u>Mass</u>	A point
	<u>Moment</u>	A line segment
	<u>Spring - Damper - Actuator</u>	A line segment or two points
	<u>Velocity / Acceleration</u>	A <u>Coordinate</u> , <u>Distance / Length</u> , or <u>Angle Constraint</u>

Applied Force

Forces are applied to points or vectors.

- select a point or vector
- click **Mechanics Input / Applied Force**
- enter the x,y value of the force for a point, or the force value for the vector. The direction of the force is taken from the vector.

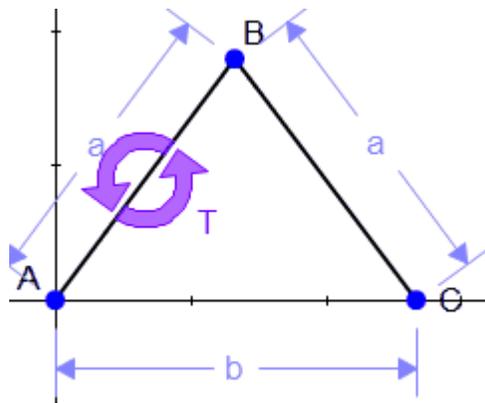


Applied Torque

Input torque is applied to line segments.

- select a line
- click **Mechanics Input / Applied Torque**
- enter the value

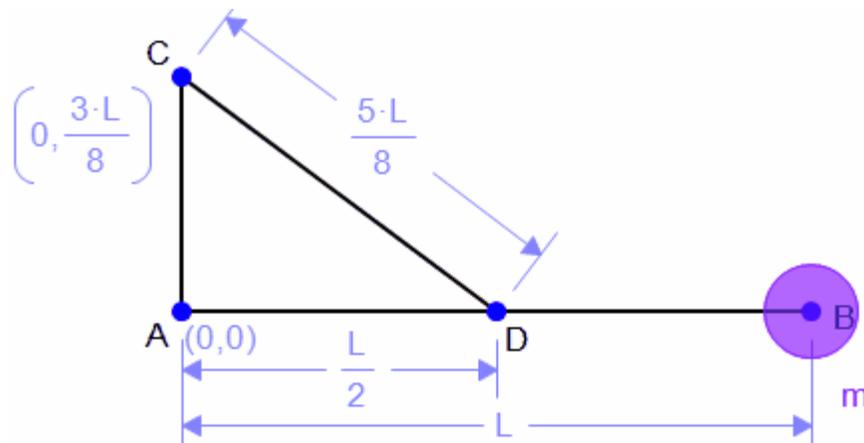
The example below shows a pump model with an input torque T.



Mass

Masses are applied to points.

- select a point
- click Mechanics Input / Mass
- enter the value

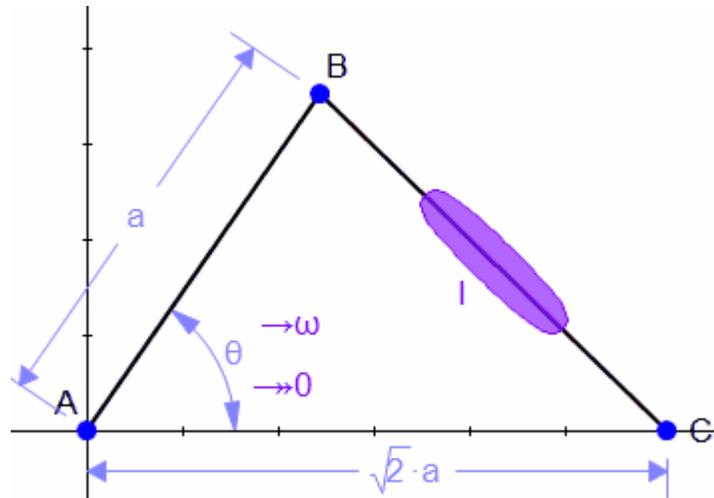


Moment

A moment of inertia is applied to line segments.

- select a line
- click the **Moment** icon from the **Mechanics Input** toolbox
- enter the value

In the model below we give member BC a **Moment** of I.

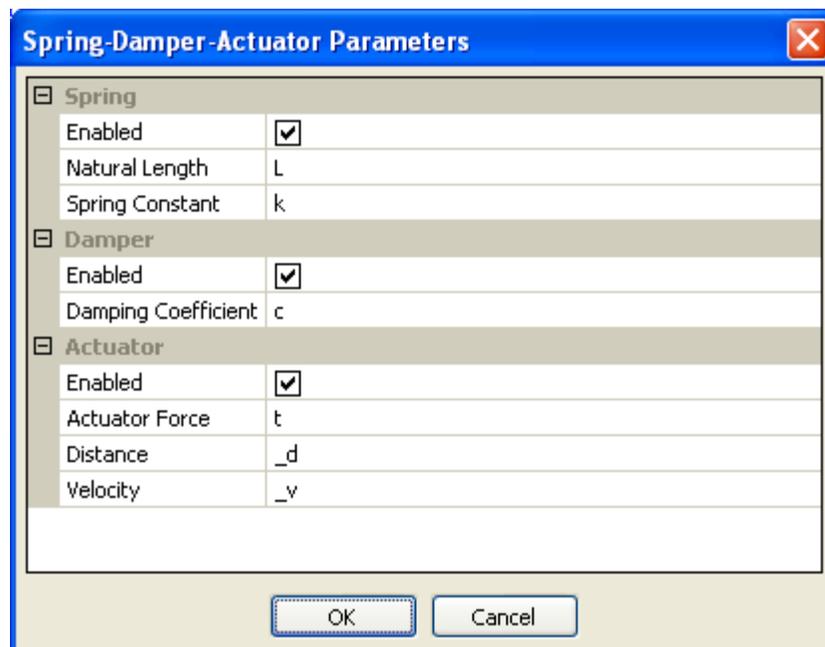


Spring - Damper - Actuator

Springs, dampers and actuators are attached to line segments.

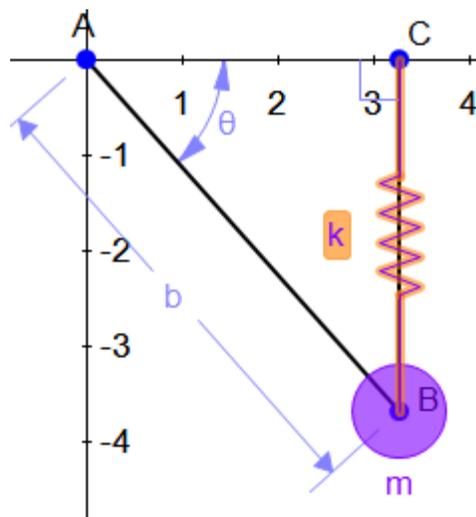
- select a line or two points
- click **Mechanics Input / Spring - Damper - Actuator**

The dialog box appears.



- check Enabled checkbox for the element you want to add
- fill in the values for the element you want to add.
- check that the Enabled checkbox for the elements you don't want to include is unchecked

The example below is a model of a spring with spring constant k , attached to a pendulum.



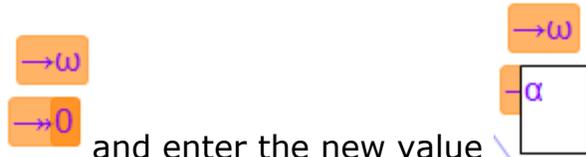
Velocity - Acceleration

Velocities and accelerations are conveyed through constraints.

- select a point's **Coordinates**, a **Distance / Length** constraint, or an **Angle** constraint
- click the **Velocity - Acceleration** icon in the **Mechanics Input** toolbox
- enter the velocity

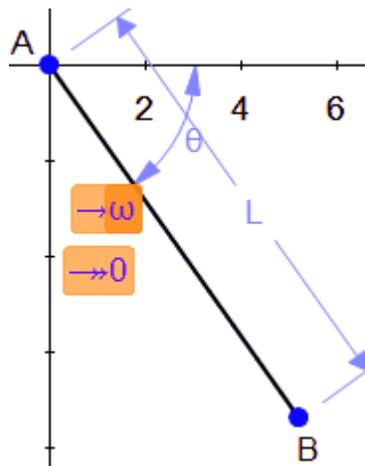
The acceleration is initially set to 0. To change the acceleration

- double-click the acceleration



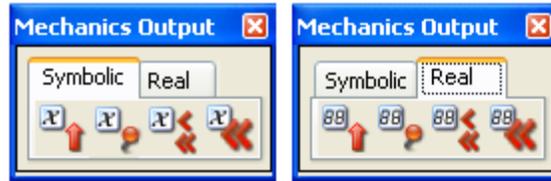
and enter the new value

In the example below we assigned an angular velocity to the pendulum.



Mechanics Output

Viewing Mechanics Outputs



Based on your input specifications, *Mx* will perform a full range of force analyses including static, inverse dynamic, kinematic and tolerance analysis. You can obtain numeric values by selecting the **Real** tab, or symbolic expressions by selecting the **Symbolic** tab. Initially, all the outputs in the toolbox are inactive. You must first select the element in your model which carries desired output. The following table lists all the Mechanics outputs and the elements you must preselect.

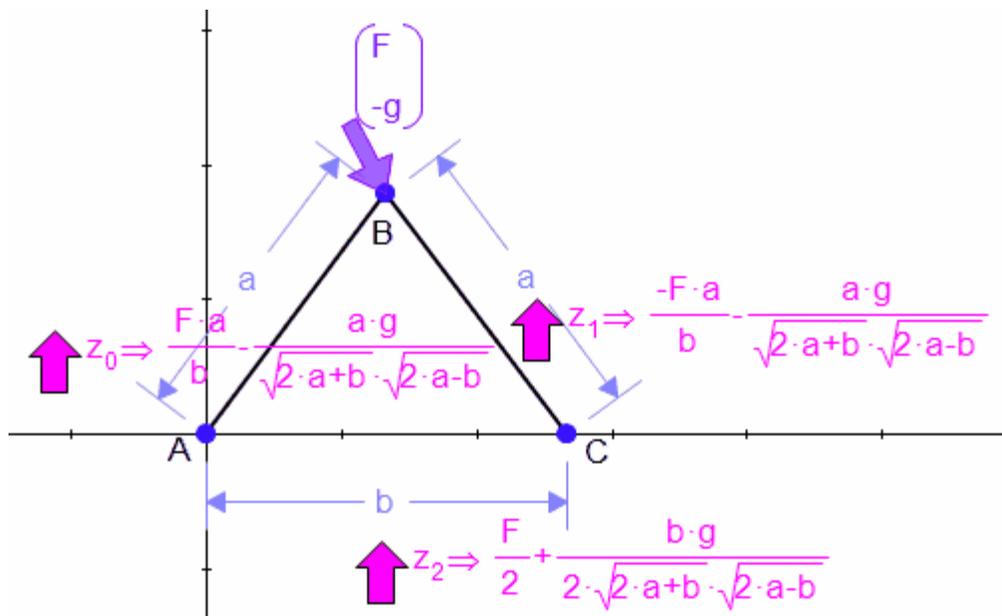
Icon	Mechanics Output	Preselected Object(s)
	<u>Reaction Force</u>	A point, line segment or polygon side
	<u>Pin Reaction</u>	A line segment and one of its endpoints
	<u>Velocity / Acceleration</u>	A line segment or polygon side
	<u>Resultant Acceleration</u>	A <u>Coordinate</u> or <u>Distance / Length Constraint</u>
	<u>Differential Equations</u>	A Resultant Acceleration

Reaction Force

Forces are carried by constraints.

- select a point's **Coordinates**, a **Distance / Length** constraint, or an **Angle** constraint
- select the **Reaction Force** icon in the **Mechanics Output** toolbox

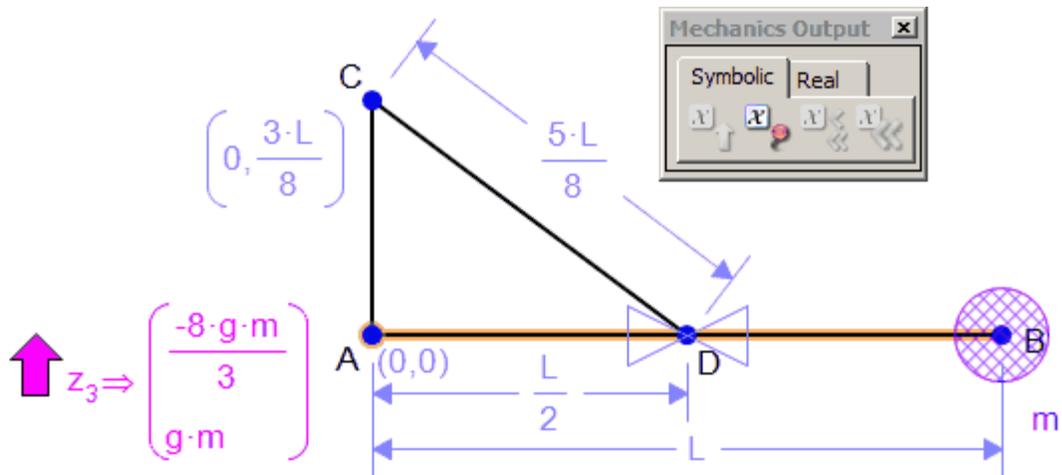
The model below has an applied force at the apex. We measure the reaction force in members AB and BC and the force holding the whole thing together (z_2)



Pin Reaction

To see the reaction force on a pin, select the pin and its line segment - the member it attaches. In the example below, we calculate the reaction force on pin A viewed as part of the member AB:

- Holding down the *shift* key, select point A and line AB
- Select **Mechanics Output / Pin Reaction**

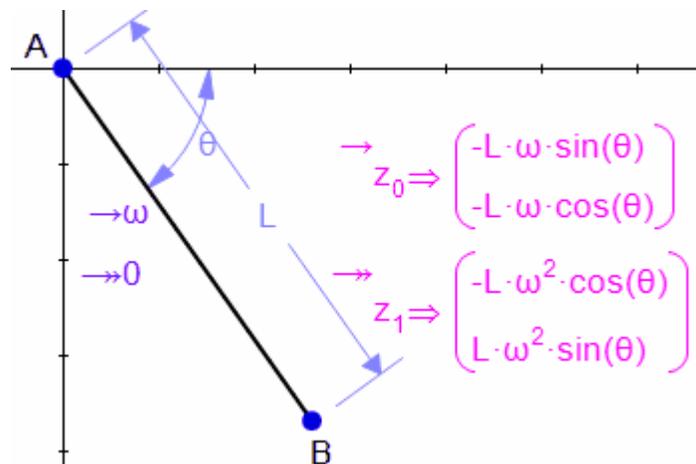


Velocity - Acceleration

Measure the velocity and acceleration of points and lines.

- select a point or line or the measurement of a distance or angle to get the relative velocity
- click the **Velocity - Acceleration** icon in the **Mechanics Output** toolbox

The pendulum in the example below has an angular input velocity, ω . The resultant velocity and acceleration of point B is displayed.

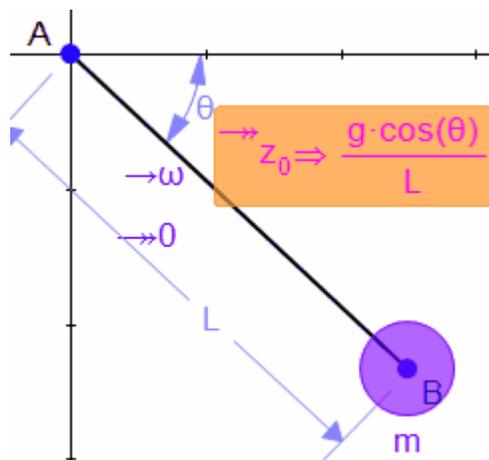


Resultant Acceleration

Output accelerations are taken from constraints which are considered free to accelerate.

- select a **Distance / Length** constraint, or an **Angle** constraint
- select the **Resultant Acceleration** icon in the **Mechanics Output** toolbox

In the example below we calculate the acceleration of the pendulum in angle θ .



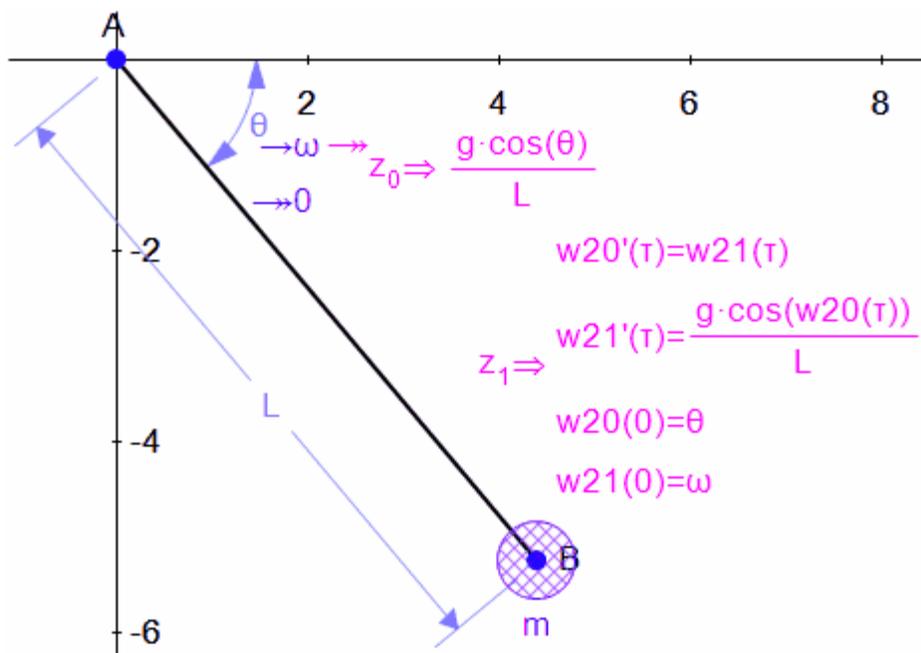
Differential Equations

For Dynamics models, you can get the equations of motion for any **Resultant Accelerations**. The equations of motion are expressed as a system of first order ODE's, the appropriate form for copying directly into your CAS.

If you have n free accelerations, you will get a set of $2n$ first order differential equations, along with $2n$ initial conditions.

The equations are functions provided by the system. The prefix for the function names may be set in **Edit/ [Mechanics Environment](#) /Differential Equation Prefix**.

Here is a simple pendulum example.



Output

Output	
Use Assumptions	<input type="checkbox"/>
Use Intermediate Variables	<input type="checkbox"/>
Show Intermediate Variables	<input checked="" type="checkbox"/>
Show Name	<input checked="" type="checkbox"/>
Show System Variables	<input checked="" type="checkbox"/>
Maximum Size Allowed On Diagram	4
Use Approximation	<input type="checkbox"/>
Approximation Order	Linear

Viewing the Output

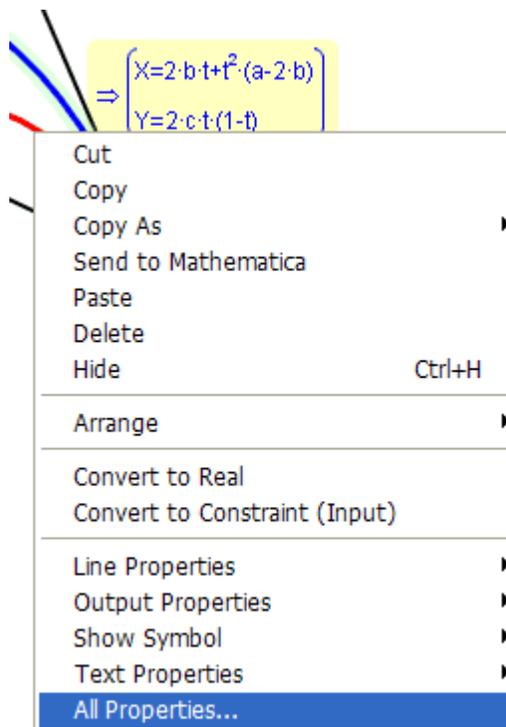
The Output settings apply to [Symbolic Calculations](#). The general default Output settings are found in the **Edit / Preferences** menu selection,



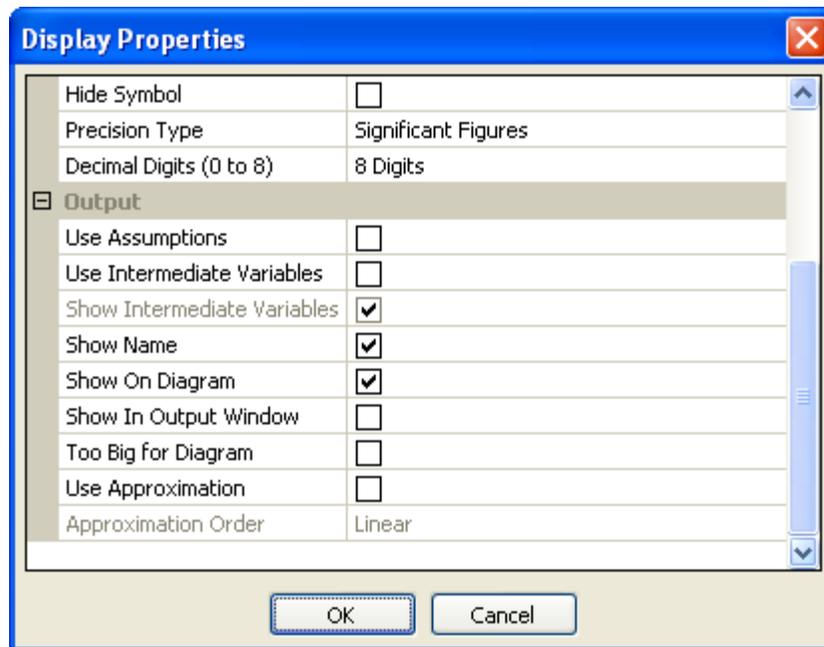
Math tab - **Math** .

Individual outputs can be adjusted in the **Display Properties** dialog. Select the output(s), then invoke the dialog in one of two ways:

- right click the mouse and select **All Properties** from the **Selection** context menu



- from the menu bar, select **Edit / Properties**



The **Output** selections specify how the calculations are made and how the output is displayed.

[Use Assumptions](#) - applies to equations containing absolute values.

[Use Intermediate Variables](#) - can sometimes simplify the output.

The "[Show](#)" check boxes control where the output is displayed.

The check boxes are toggles; when the box is checked the property is true, when it is clear the property is false.

Assumptions

With the [Use Assumptions](#) selection, *Mechanical Expressions* eliminates the absolute value from expressions and determines from the diagram whether the value is positive or negative. Try it with these steps:

1. [select](#)  one or more output calculations
2. right click the mouse and select **All Properties** from the **Selection** context menu
3. check the [Use Assumptions](#) check box

Obviously, this tool only has an effect when the expression selected

contains an absolute value.

Intermediate Variables

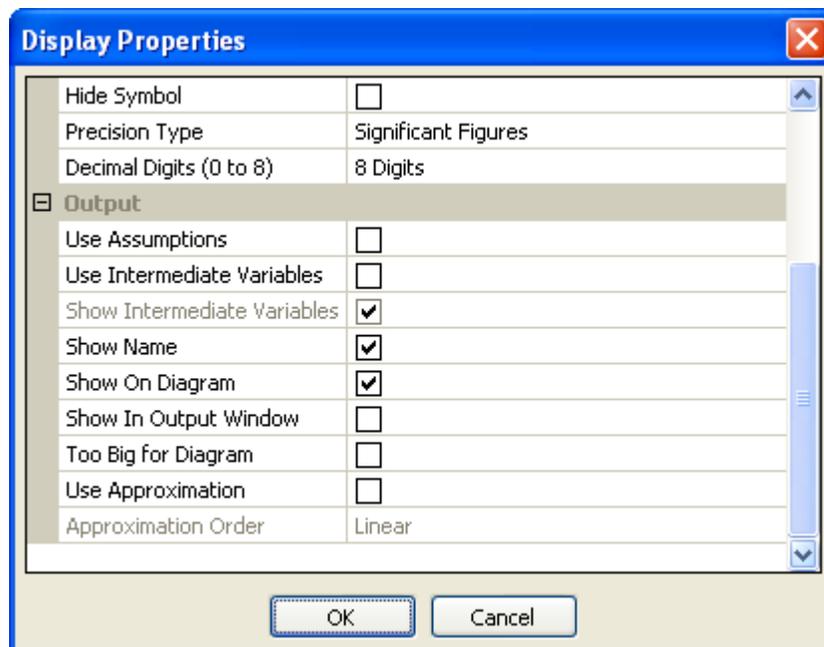
Substituting intermediate variables can sometimes simplify expressions calculated by the program. Try this option to see how it affects your output:

1. [select](#)  one or more output calculations
2. right click the mouse and select **All Properties** from the **Selection** context menu
3. check the Use Intermediate Variables check box

If Use Intermediate Variables is unchecked, the Show Intermediate Variables is inactive.

Note: Intermediate variables are not always used in calculations, in which case this box will have no effect.

Show Output Check Boxes

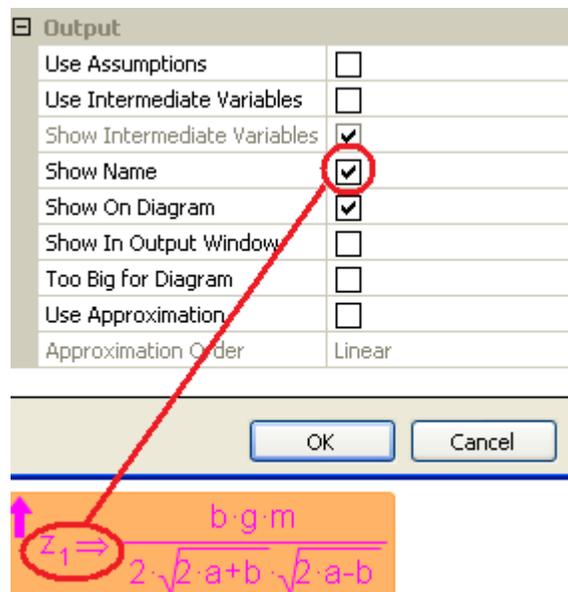


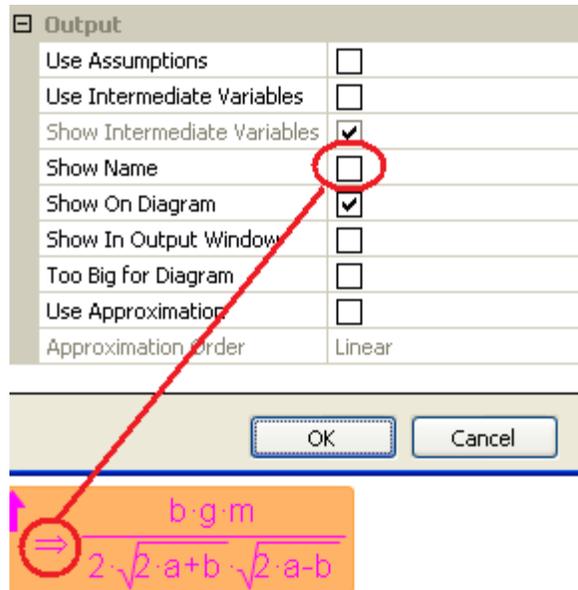
After you generate an output expression:

1. click the output
2. right click the mouse and select **All Properties** from the **Selection Context** menu.
3. when checked, the corresponding output is displayed

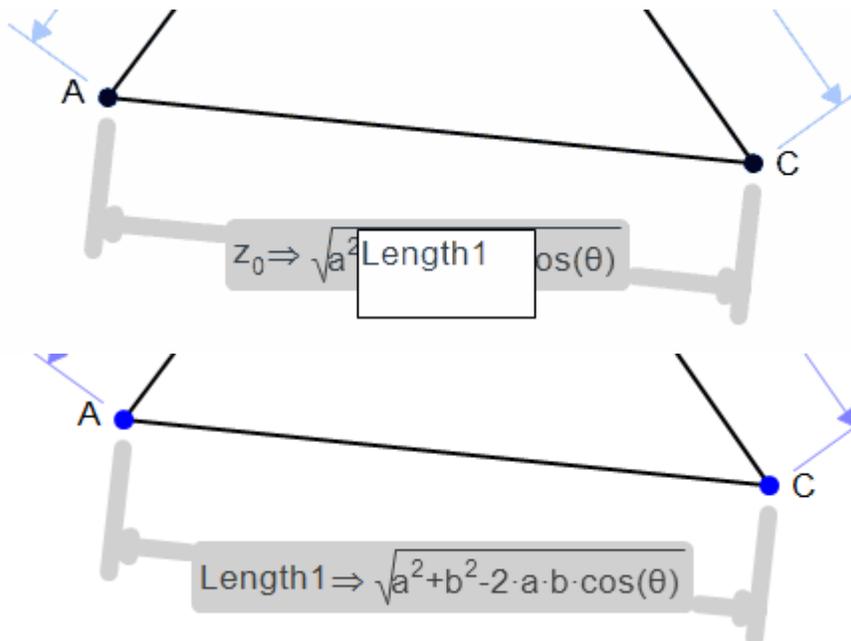
Show Intermediate Variables - if the system uses intermediate variables, their definitions are displayed in the output window.

Show Name - is a term assigned by the system to the output. This name is z_n where n is the sequential number of the output .





You can change the output name by double clicking the output and entering a new name in the box.



Show On Diagram - puts the output expression on the diagram when checked.

Show in Output Window - puts the output expression in the output window when checked. If this value is checked, then Show Name becomes active.

Too Big for Diagram - the output expression is moved to the output window when checked (Show in Output Window is checked, Show On Diagram becomes inactive).

Approximation

Converting an output to a numerical **Approximation** lets you investigate tolerance sensitivity. The resulting expression is a Taylor series of 1st or 2nd order expanded about the current numerical values of the variables. Here are the steps.

1. select the symbolic output
2. from the [Selection Context](#) menu (right-click) choose **All Properties**
3. scroll to the bottom of the window and check the Use Approximation box
4. click the Approximation Order line and the  button to chose between *Linear* and *Quadratic*.

Diagram illustrating the Law of Cosines for a triangle with vertices A and B, side length a , and angle θ . The distance z_0 is calculated as:

$$z_0 \Rightarrow \sqrt{a^2 + b^2 - 2 \cdot a \cdot b \cdot \cos(\theta)}$$

The **Display Properties** dialog box shows the following settings:

Hide Symbol	<input type="checkbox"/>
Precision Type	Significant Figures
Decimal Digits (0 to 8)	8 Digits
Output	
Use Assumptions	<input type="checkbox"/>
Use Intermediate Variables	<input type="checkbox"/>
Show Intermediate Variables	<input checked="" type="checkbox"/>
Show Name	<input checked="" type="checkbox"/>
Show On Diagram	<input checked="" type="checkbox"/>
Show In Output Window	<input type="checkbox"/>
Too Big for Diagram	<input type="checkbox"/>
Use Approximation	<input checked="" type="checkbox"/>
Approximation Order	Linear

The resulting linear approximation of z_0 is:

$$z_0 \Rightarrow -4.0078877 + 0.58475914 \cdot a + 0.76080293 \cdot b + 2.6914244 \cdot \theta$$

If you have many outputs for using **Approximation**, you can change the default setting in **Edit / Preferences / Math / Output** before you make your output calculations.

Symbols

Using Symbols



The **Symbols** toolbox lets you easily [insert Greek letters](#) into your expressions and constraints. Click the tab to choose from lower case or upper case Greek letters. Use the buttons or type the name of the Greek letter and the symbol will be inserted after you press *enter*.

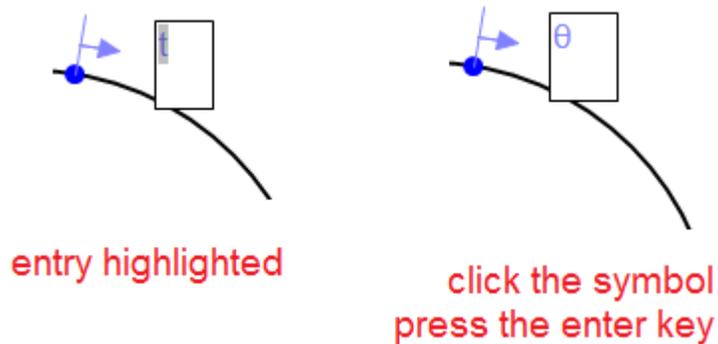
The bottom row of buttons in the toolbox lets you insert commonly used math operations. You can either use the icons, or you type them from your keyboard:

Symbol Icon	Function Call / Reserved Word
	<code>sqrt(value)</code>
	<code>abs(value)</code>
	<code>piecewise({expression1, domain1},{expression2, domain2}...,{last expression, otherwise})</code>
	<code>pi</code>

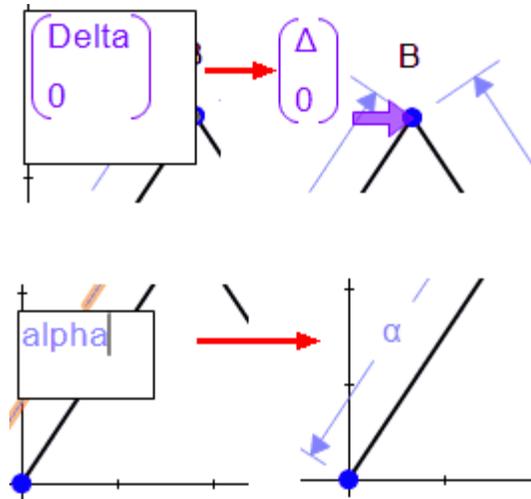
A complete list of [built-in functions](#) is detailed below.

Inserting Greek Letters

To insert Greek letters into any variable name or expression, click the appropriate tab, **Greek Upper** (upper case letters) or **Greek Lower** (lower case letters) in the **Symbols** toolbox, and click the letters to be inserted into the data entry box.



If your **Symbols** toolbox is hidden, you might want to just type the name of the Greek letter into your expression. The symbol will be inserted after you press *enter*. To get an uppercase Greek symbol, capitalize the first letter of its name.

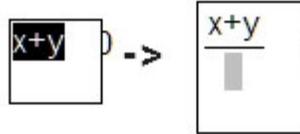


Multiplication & Division Editing Tools

 The **Multiplication** button inserts a multiplication symbol into the expression.

 The **Division** button makes expressions easier to enter and read.

- From the data entry box, enter the numerator of the expression, highlight it, and then click **Division**.



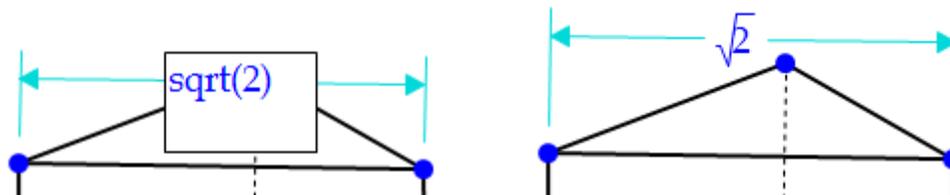
The cursor is then positioned in the denominator.

- If you click the **Division** button first, be sure to place the cursor in the appropriate place before typing the expression.

Square Root Editing Tool

 You can enter square roots in one of these ways:

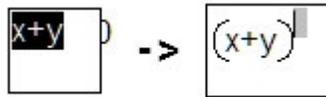
- From the data entry box, enter the expression you want inside the square root, highlight the terms, and click the **Square Root** button.
- From the data entry box, click the **Square Root** button, then highlight the 0 and type the terms.
- Use the *sqrt()* function in the data entry box.



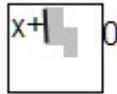
Subscript / Superscript Editor

You can enter superscripts or subscripts for variables in one of these ways:

- From the data entry box, enter the expression you want sub/superscripted, highlight the terms and click the **Subscript**  or **Superscript**  button.



- From the data entry box, click the **Sub/Superscript** button and type the values into the grey boxes.



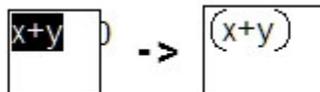
Note: Make sure the cursor is positioned at the left side of the gray box before typing the sub/superscript.

- Another way to make a subscript is to use square brackets - $A[1] = A_1$

Parentheses and Absolute Value Notation

You can add parentheses or an absolute value sign to a term in one of two ways:

- From the data input box, type the term(s), highlight the term(s), then click the **Parentheses**  or **Absolute Value**  button.



- From the data entry box, click the **Parentheses**  or **Absolute Value**  button first and enter the terms.

Using the Piecewise Function

 A piecewise function or expression can be created using the **Piecewise** symbol or the [built-in function](#) - $piecewise(\{expression1, domain1\}, \{expression2, domain2\}, \dots, \{last\ expression, otherwise\})$. The reserved word, "otherwise" is an option available for the last condition.

For details see [Piecewise Function](#) and [Piecewise Parametric Example](#) in the [Creating Functions](#) section.

Built-In Functions

For including in any expression or constraint, *MX* has the following common functions available:

Trig

• <code>sin()</code>	• <code>arcsin()</code>	• <code>sinh()</code>
• <code>cos()</code>	• <code>arccos()</code>	• <code>cosh()</code>
• <code>tan()</code>	• <code>arctan()</code>	• <code>tanh()</code>

Math

• <code>sqrt()</code> - same as 	• <code>abs()</code> - same as 
• <code>signum(x)</code> - finds the sign of a number: = -1 if $x < 0$ 0 if $x = 0$ 1 if $x > 0$	• <code>exp(x)</code> - the exponential function; you must use <i>exp</i> , <u>not</u> <i>e</i> , <i>e</i> is just a variable name
• <code>log()</code> or <code>ln()</code> - both mean the natural log	• <code>piecewise</code> ({expression1, domain1},{expression2, domain2}...) - the function is evaluated in the order written
• <code>diff(expression, variable)</code>	• <code>integrate(expression, variable)</code>
• <code>sum(expression, variable = start, end)</code>	• <code>pi</code> - same as  in the Symbols toolbox
• <code>ceil()</code> - rounds up	• <code>floor()</code> - rounds down

Boolean

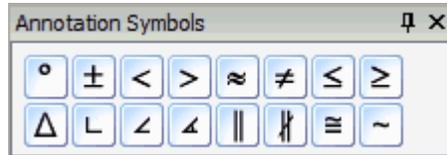
AND	<
OR	<=

NOT

>

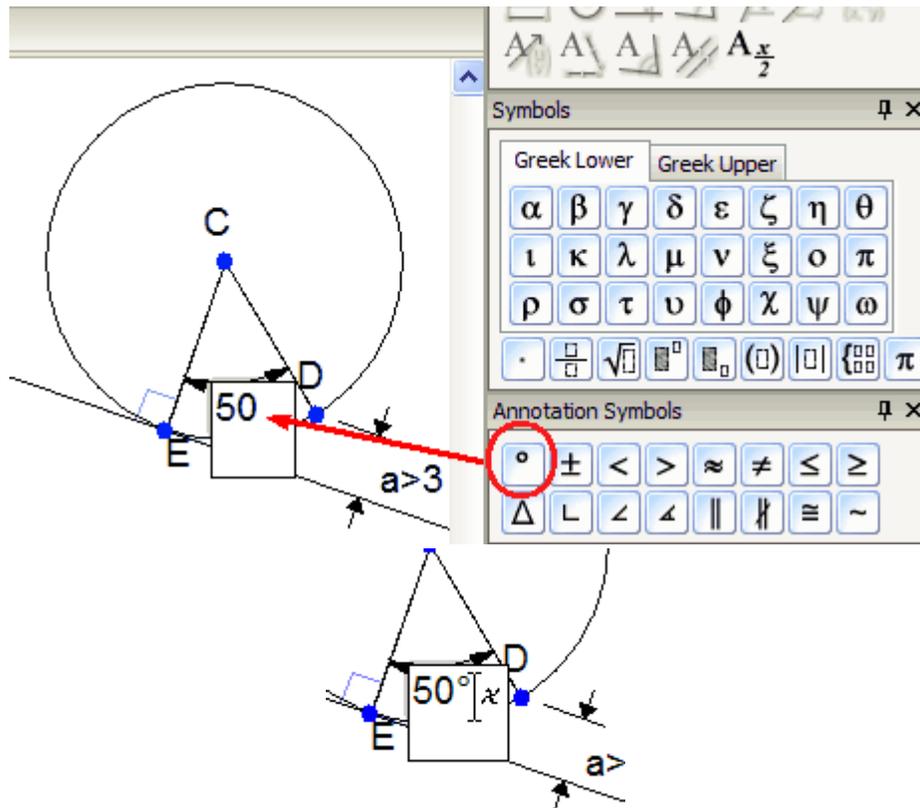
>=

Using Annotation Symbols

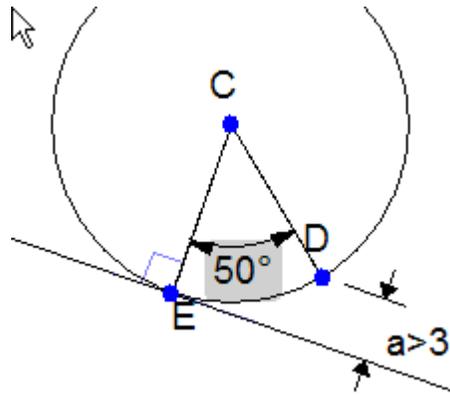


Annotation Symbols are available for use with any of the [Annotate](#) tools. These symbols are not used in *Mechanical Expressions'* algebra engine, but may be useful in creating worksheets and tests.

Use the symbols from the data entry window of the **Annotate** tools. Simply click the symbol you need as you type.

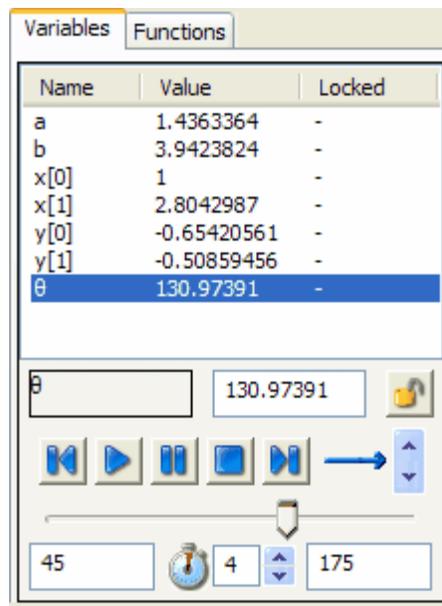


When you are finished with the annotation, press enter.

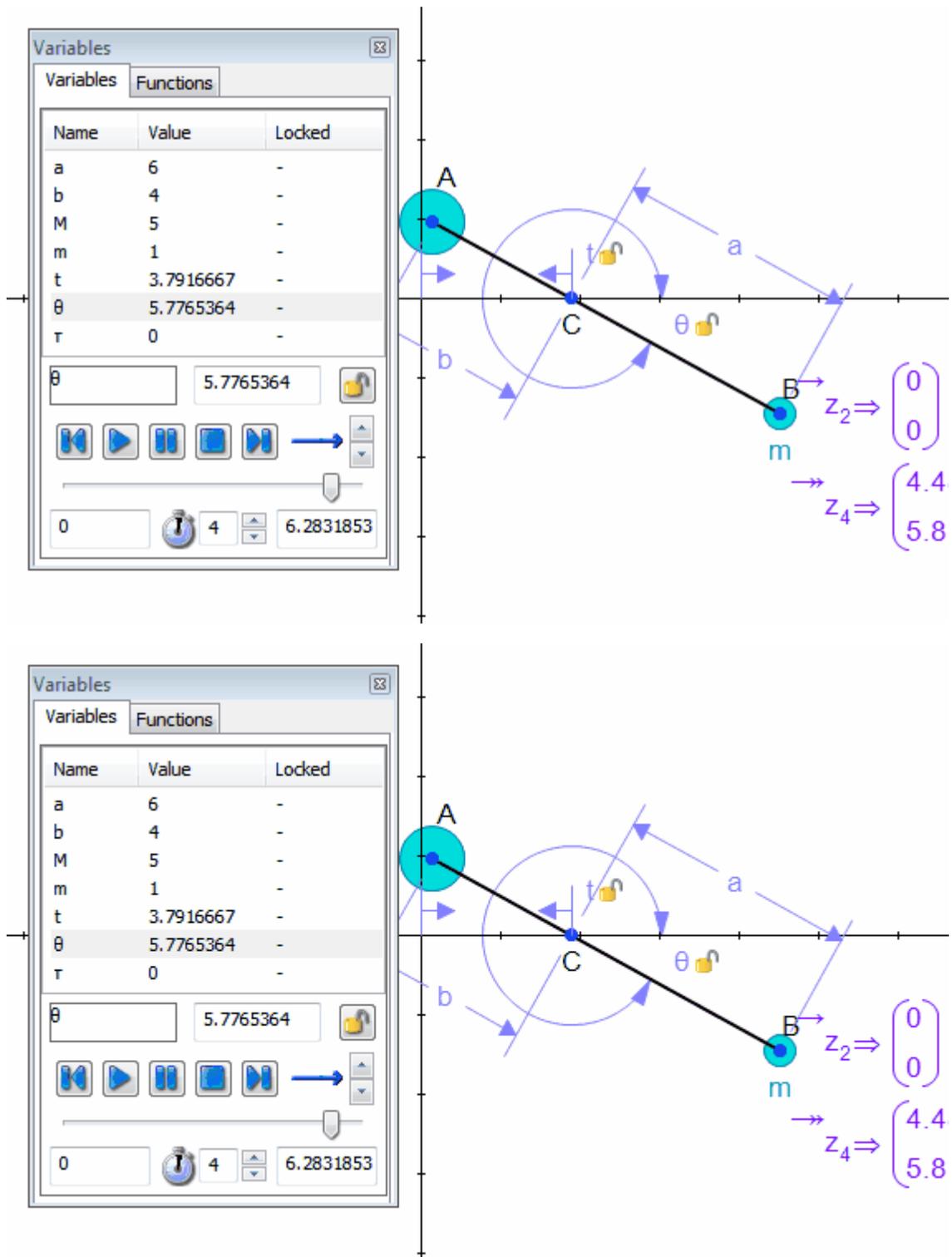


Font trouble - some of the **Annotation Symbols** may not show up in your drawing, depending on your OS and the default font setting. (Windows 7 users have no worries.) If you don't see an **Annotation Symbol**, change the **Edit / Preferences / Math / Annotation / Font / Face Name**. Try one of the Unicode fonts, e.g. *Lucida Sans Unicode*. If you are [exporting a Metafile](#), you may have to change the default font in the program to which you are exporting.

System Variables and Animation



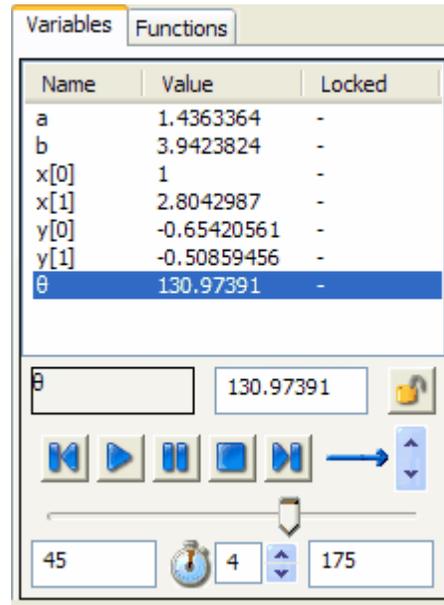
Investigating Variables



The **Variables** toolbox reports all the variables you have used in the

diagram and lets you manipulate their values.

Variables List



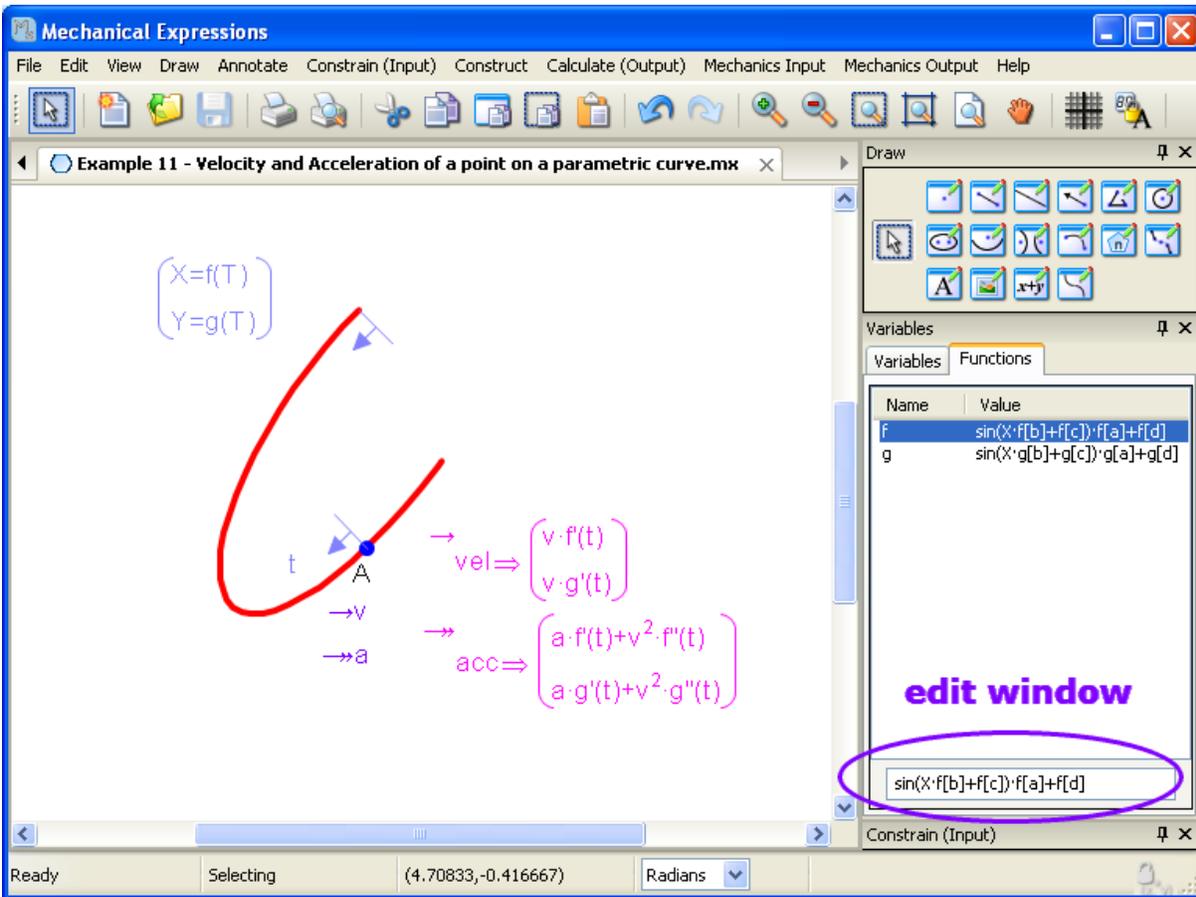
This list contains the names of all variables used in your diagram.

For every variable name, the system shows:

- **the current value** - these values can be ones that you have explicitly specified, or just taken from the way you sketched the geometry.
- **lock status** - if the variable is locked (+) its value will not change if you move the geometry or add additional constraints; the unlocked (-) variable is free to change as the geometry moves or changes.

Functions List

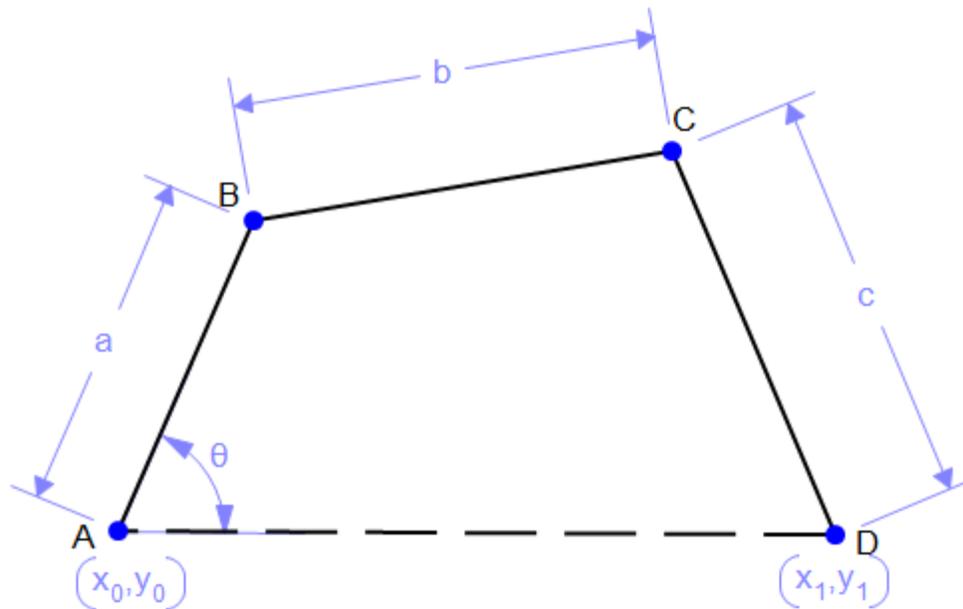
When using the [Function](#) command to draw a function of the form $Y=f(X) + g(X)$, the **Functions** tab in the **Variables** toolbox lists the functions f and g and their values. Use the edit line at the bottom of the box to modify the functions.



Using the Lock Tool

By default, when you drag points in a *Mechanical Expressions* model, it will adjust the numerical sample values used in the various parameters of the model to accommodate the drag, as best it can.

For example, in the model of a 4 bar linkage below, dragging point B will cause lengths a and b and angle θ to be adjusted appropriately.



However, you may want the drag to act as if the members AB and BC were rigid, and only angle theta adjustable. To do this you can [lock the parameters](#):

Name	Value	Locked
a	2.5	+
b	3.1509052	+
c	3.091761	+
x[0]	-2.4299065	+
x[1]	2.7476636	+
y[0]	-1.0654206	+
y[1]	-1.0841121	+
θ	1.1230514	-

The value of a , for example, can still be set from the Variables panel, but it will not change when the model is dragged.

Changing and Locking the Variable Value



To make a change to the variable list, first click anyplace in the row of the variable you want to change. That row will be highlighted.

To change the value: highlight the value in the edit window and type the new value.

To change the lock status: just click the button -

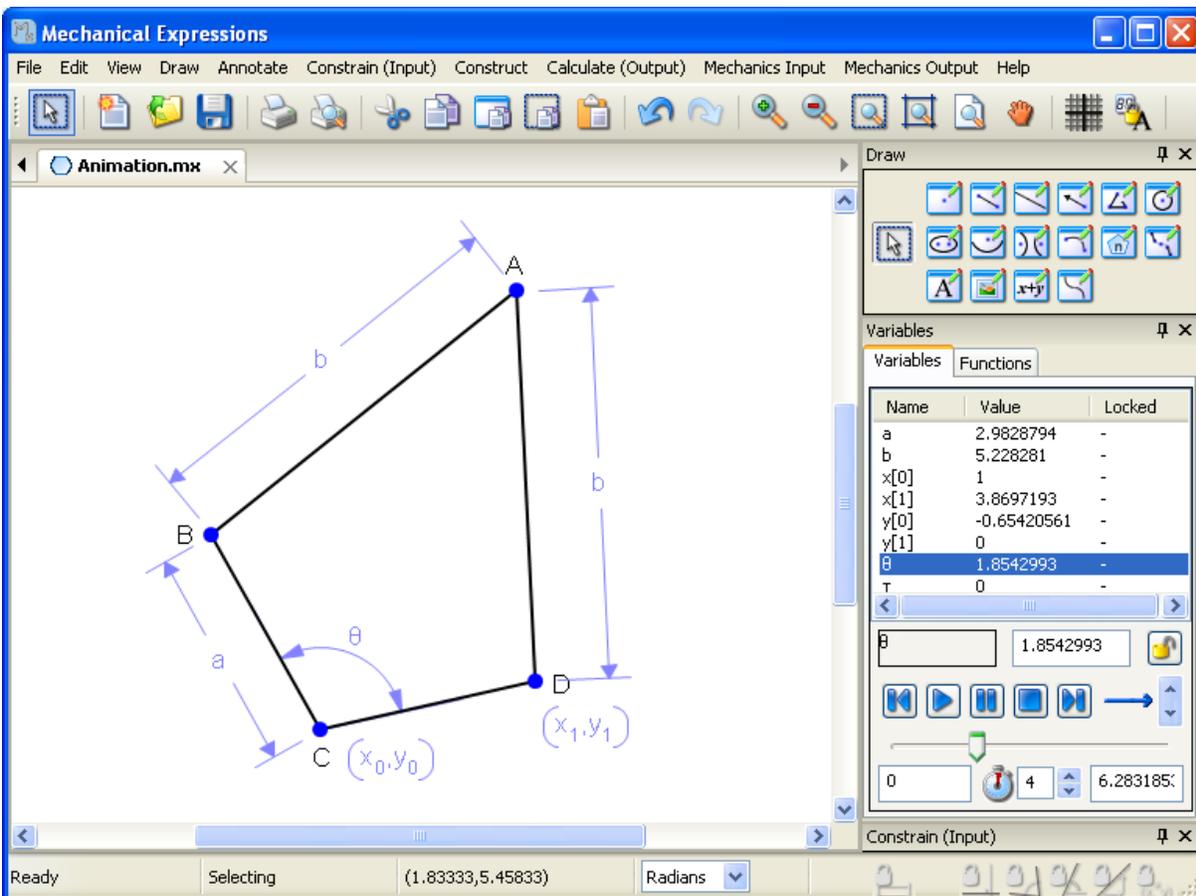
 to unlock a locked variable

 to lock an open variable

Animation

Your geometry comes to life with the Animation tools. You simply need to select the parameter that drives the animation, give it a range, then Play.

In the diagram below we select θ for the crank of this linkage.



Click the headings below for details on the animation buttons and windows:

- [Animation console](#) - works like a video player.
- [Animation modes](#) - indicates how the range for the animation is stepped through.
- [Animation values and duration](#) - where you specify the speed and the range for the driving parameter.

Users of numeric interactive geometry systems may be familiar with the concept of animation based on points animated along line segments or curves. This type of animation can be conveniently modeled in **Mechanical Expressions** using the [point proportional along a curve](#) constraint along with parameter based animation.

Animation Console



The Animation console works like a standard video console with the **Play**, **Pause**, and **Stop** buttons as well as advance to the **Beginning** and **End** buttons.

Animation Modes



The animation modes can be changed with the up/down arrow buttons. The modes are:

-  Runs the animation one time through the specified range.
-  Runs the animation continuously from the beginning to the end of the range.
-  Runs the animation one time forward and then backward through the specified range.
-  Runs the animation continuously forward and then backward through the specified range.

Animation Values and Duration



These animation buttons help you adjust the range and speed of the animation.

- Click and drag the slider along the bar to manually animate the drawing.
- In the two data entry windows at the bottom right and left of the toolbox, specify the range of the animation.
- The **Duration** box in the center lets you specify how long the animation takes to play one time through. Values are between 1 and

60 seconds.

Animation and the Locus Tool

Both the construction of the [locus and envelope curves](#), and the [animation](#) of the diagram in *Mechanical Expressions* can be defined in terms of any variable. For example in the model below, we can create a locus over values of the variable t (other variables will be kept constant).

Mechanical Expressions

File Edit View Draw Annotate Constrain (Input) Construct Calculate (Output) Mechanics Input Mechanics Output Help

Animation.mlx Oval of Cassini.mlx

Oval of Cassini

A $(-a,0)$ B C $(a,0)$

t $\frac{k}{t}$

Name	Value	Locked
a	3.4166667	-
k	13.375647	-
t	3.8161412	-
τ	0	-

3.8161412

0 4 10

Ready Selecting (0.958333,1.27083) Radians



Menus and Icons

Many of the menus and icons across the top of the screen duplicate the commands and functions found in the toolboxes.

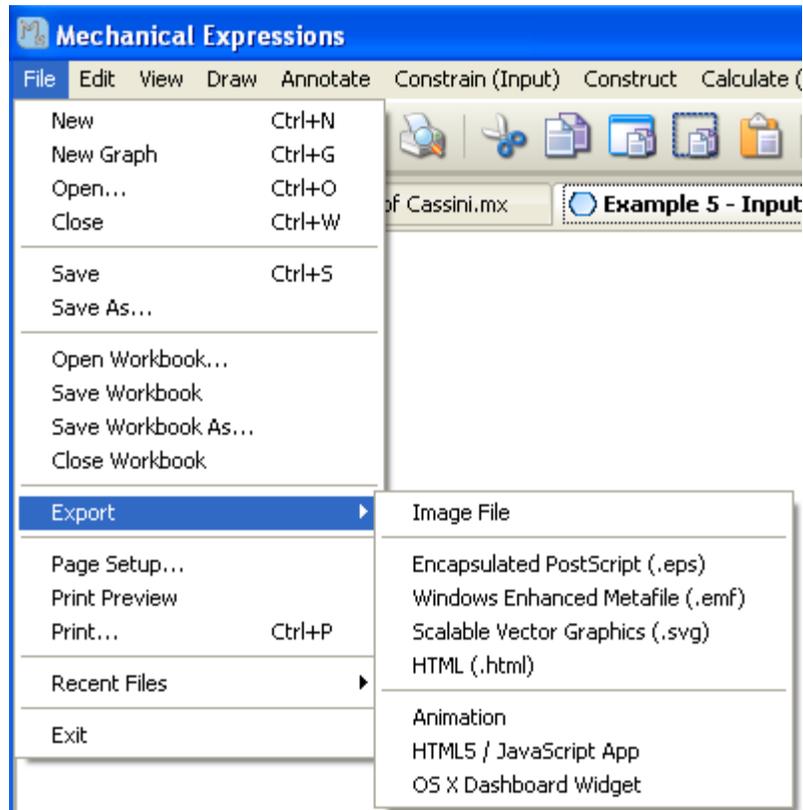
File Menu

The **File** menu contains the standard Windows file handling operations with options for copying and exporting to other programs. Several of the options are also available from the icon bar.

Menu Option	Function
 New	Creates a new project.
New Graph	Graph mode allows scaling of axes.
 Open. . .	Brings up the Select a File dialog box so you can open a project.
Close	Closes the current file or, if multiple files are open, the file on top.
 Save	Saves the file. If you have not yet saved the current work to a file, the Save File As dialog box lets you specify where to save the project file.
Save As . . .	Brings up the Save File As dialog box to enter a new or different path / file name. Useful for making a backup.
Open Workbook	Brings up the Open Workbook dialog box. If any other files are open, they will be closed when you select the workbook.
Save Workbook	Saves all tabbed pages as a single workspace (.mxw), so you can open them all at once.
Save Workbook as	Saves all tabbed pages as a single workbook

	(.mxw) and lets you specify a new or different path / file name for the workbook.
Close Workbook	Closes the current workbook. If you have made changes to pages, you will be asked if you want to save them individually (.mx files).
Export	Export the file as Windows Metafile (.emf) (Windows version only), image file, an Encapsulated PostScript (.eps), Scalable Vector Graphics (.svg), HTML file (.html), animated <i>gif</i> , <i>JavaScript</i> file, or OS X Dashboard Widget.
Page Setup. . .	Displays the page setup dialog box for choosing a printer and print options.
 Print Preview	Displays the printout by pages.
 Print. . .	Displays the standard system Print dialog.
Recent files	Click to display a list of the most recently used files. Selecting one opens it.
Exit	Exits the program, after prompting for save.

Exporting a Drawing



To export your drawing to another program, choose **File / Export**. You can export the drawing in the following formats:

Static File Formats

- *Image - BMP, JPEG, TIFF, PNG, XMP*
- *Encapsulated Postscript*
- *Windows Enhanced Metafile*
- Scalable Vector Graphics
- [HTML](#)

Dynamic File Formats

- [Animated GIF](#)
- [HTML5 / JavaScript App](#)
- [OS X Dashboard Widget](#)

 Please note that neither EMF, nor EPS support semi-transparency or transparent images of any kind, thus you will get a warning message if you try to export to either of these formats and you have such an item in the document.

Here are the steps for the export as an Image file, EPS, EMF, SVG or HTML:

1. For all file types enter the Filename or click the folder icon to select the appropriate folder and file.
2. [Image files](#) and [HTML files](#) have an extra step at this point as detailed below.

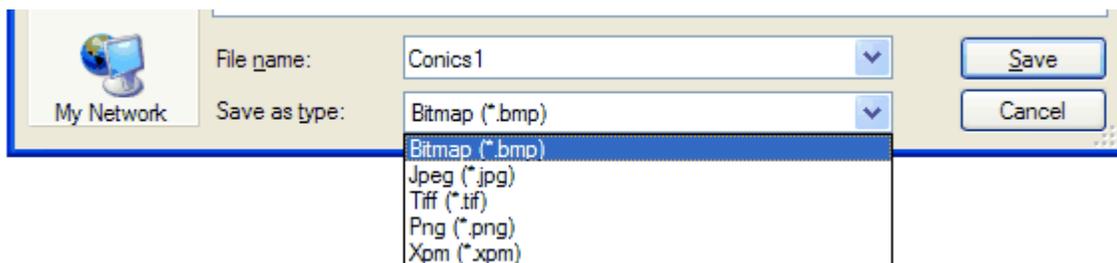
3. Select the region of the drawing with the displayed cursor (click-and-drag opposite corners of the region).



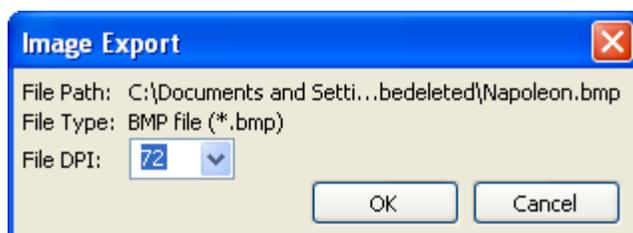
[Animation Files](#) and [JavaScript Files](#) have a few more details to consider as explained below.

Exporting Image Files

When exporting image files, click the down arrow in the Save as type line to select your desired image format.



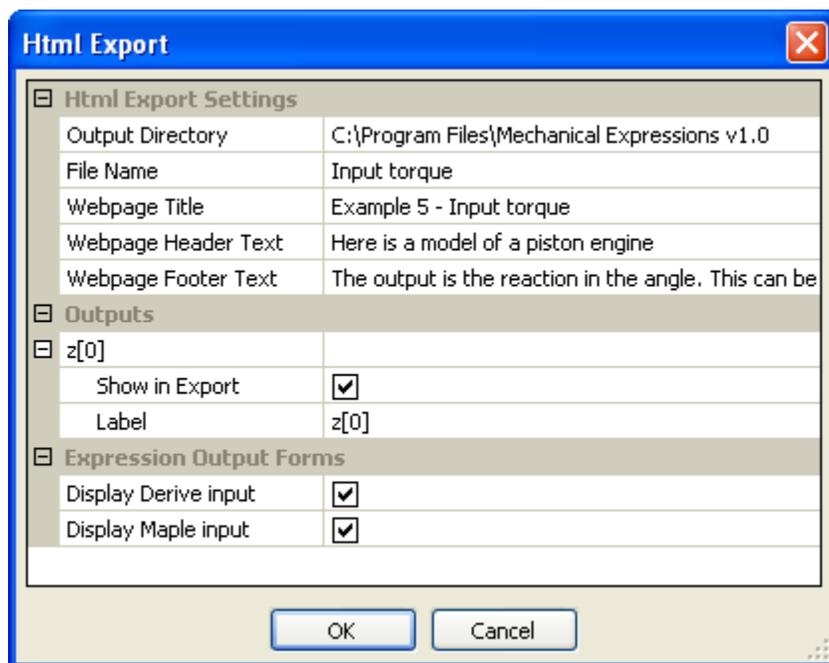
Next, set the resolution in the File DPI box. Click the down arrow and select the appropriate setting or enter a number in the window.



Exporting HTML Files

When you select **File / Export / HTML**, the **HTML Export** dialog appears.

Fill in the Html Export Settings with optional Title, Header and Footer text. The Outputs can be renamed to something less obscure than letters with subscripts. You can give them actual labels using real words. You can also display your output expressions in many popular CAS input formats including *Content* and *Presentation MathML*.



[-] Html Export Settings	
Output Directory	C:\Program Files\Mechanical Expressions v1.0
File Name	Input torque
Webpage Title	Example 5 - Input torque
Webpage Header Text	Here is a model of a piston engine
Webpage Footer Text	The output is the reaction in the angle. This can be
[-] Outputs	
[-] z[0]	
Show in Export	<input checked="" type="checkbox"/>
Label	z[0]
[-] Expression Output Forms	

Exporting Animation Files

Select **File / Export / Animation File** to produce an animated *gif*. This format is supported by many applications and will enable you to embed animations in, for example, *PowerPoint* slides and *Wikipedia* pages.

Select the directory and file name of your *gif*, and you will be presented with a dialog to choose the parameter on which the animation is based, along with various technical aspects of the animation.

Animation Export

File Path: C:\GeometryExpressions\reflection.gif

File Type: Animated GIF

File DPI: Use screen DPI

Frames Per Second: 10

Number of iterations: 0 Enter "0" for unlimited iterations.

Variable: t

File DPI - specify the resolution of the output. The higher number you use, the slower will be the process of creating and loading the animation.

Frames Per Second - if you multiply this number by the animation duration specified in the **Variables** toolbox, you will get the number of frames captured. For example if you are set at 10 frames per second,

and the **Variables** toolbox specifies the duration of the animation to be 4 seconds, then 40 frames will be captured. The more frames you capture, the slower will be the animation creation process, and the longer the animation will take to load.

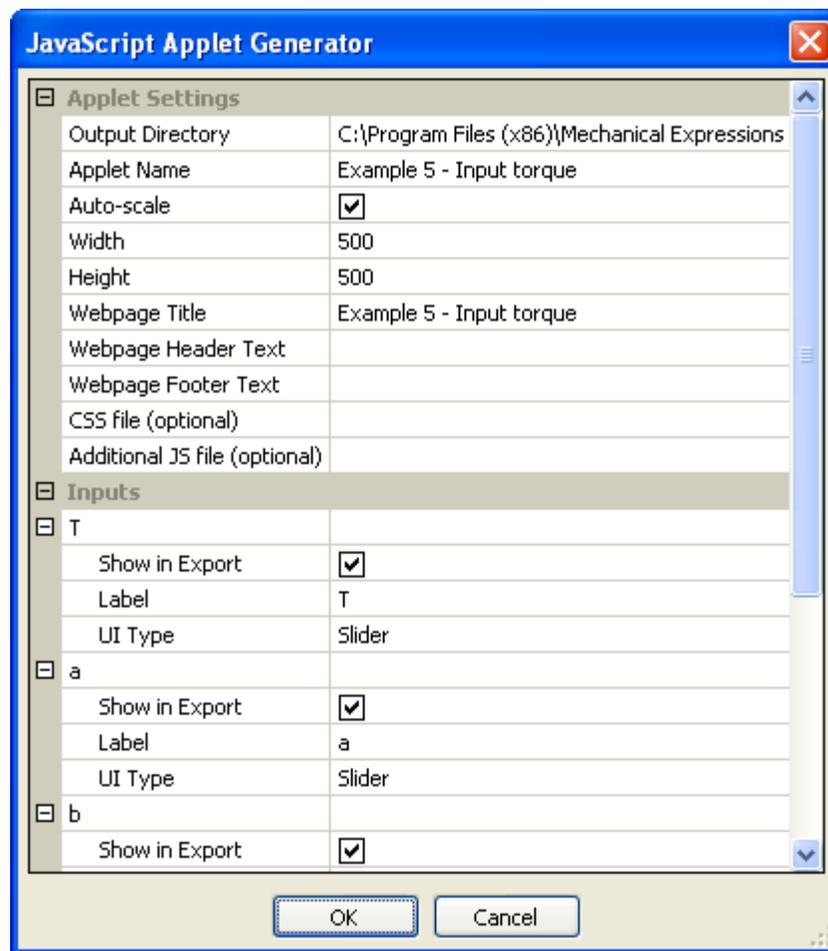
Number of iterations - when an animation is played (e.g. when a *PowerPoint* slide containing the animation is displayed), enter a number to play the animation a specific number of times, or enter 0 to play it continuously.

Variable - choose the variable that controls the animation. (All the variables in the **Variables** toolbox should be available). The limits of the variable defining the range of the animation should be set in the **Variables** toolbox.

Exporting JavaScript Files

Select **File / Export / [HTML5 / JavaScript App]** - to export a *Mechanical Expressions* model as a *JavaScript* application (.html file), within an html page. This can then run within any web browser that supports HTML 5.

Fill out the details in the **JavaScript Applet Generator** dialog.



Output directory - tells *MX* where to put the files. It will create a file: *name.html* in the specified directory. You should be able to bring *name.html* up in a browser to see the applet.

Applet Name - is the name of the html file.

Auto-scale - when check, the JavaScript applet automatically rescales the drawing when the user changes the value of one of the inputs; when uncheck, you click-and-drag a rectangle around the drawing after you click Ok.

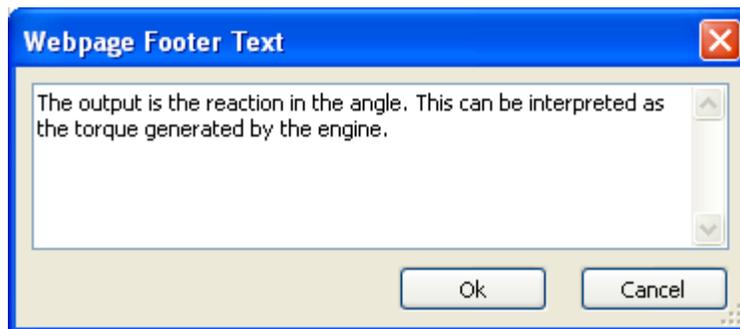
Width and Height specify the size of the drawing on the html page.

Webpage Title, Webpage Header Text, and Webpage Footer Text - enter your text for these sections of the applet.

Since header and footer text may be several lines long, You can go back and change these text boxes before you close the dialog:

- select the text entry box
- click the  to display the dialog
- enter or edit text, then click Ok.

Note: you can insert html code into the header and footer text, e.g. to make a word in the footer text bold:



CSS file - lets you add special formatting to your app with your own *Cascading Style Sheet*.

Enable Dynamic Simulation - view models with constraints that are free to move, like a pendulum or a trebuchet. You can insert UI to start and stop the simulation and set the simulation speed by checking the desired boxes. If you leave them blank, the simulation starts automatically and the speed is set by the system.

Inputs - lets you choose which variables the user will be able to change, what text Label identifies variable and what type of control to use.

Any variables in your *MX* model may be selected as input variables in the *JavaScript* model. See the topic detailing UI Types below.

Outputs - lets you choose which outputs will appear in the applet, and their text Label.

See the [examples](#) below.

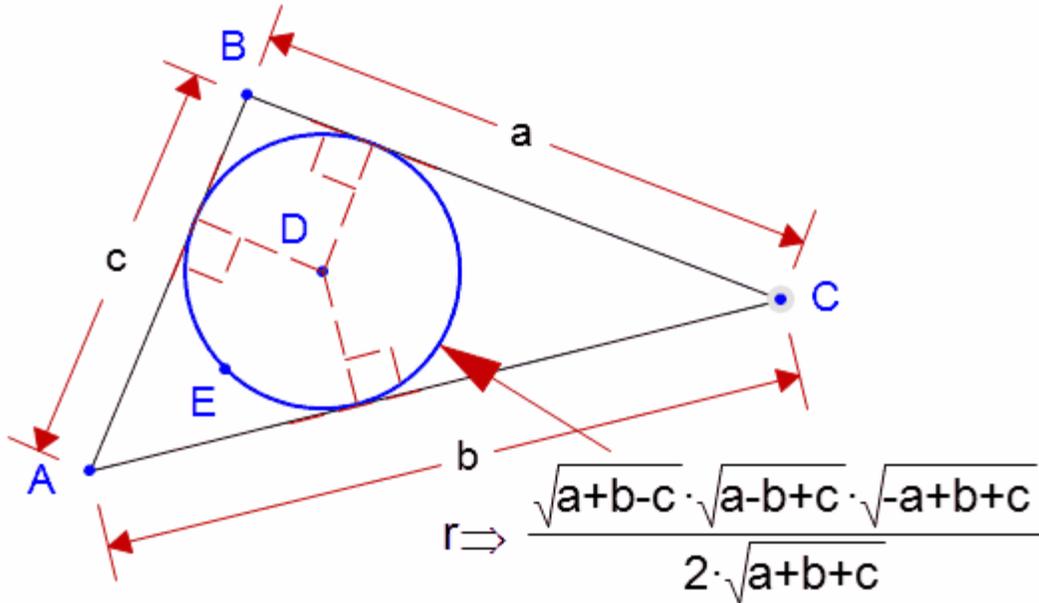
Scaling the App

The Auto-scale checkbox in the **JavaScript Applet Generator** dialog lets *Mx* decide the size of the drawing in the app window. It does this without knowing how the drawing might move in a simulation, so only check this box if there is no movement in the app, or if the movement doesn't change the bounds of the drawing, as in the [Brachistochrone](#) example below.

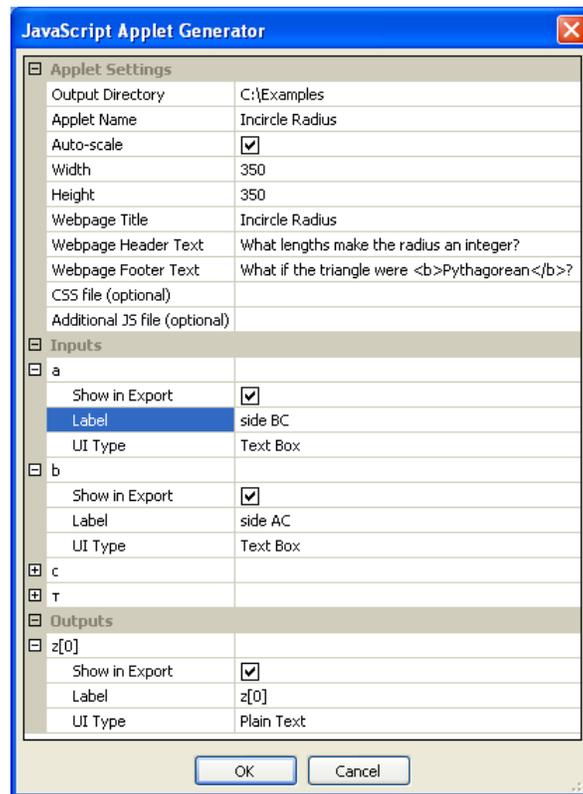
In the Trebuchet example is one that should not use the Auto-scale function, we leave the box unchecked. When you finish entering all the applet details, *Mx* prompts you to select the drawing area. Remember to leave enough space around the drawing to account for movement. If you need to adjust it after the export, just go back to the *Mx* file. All the details are saved, so you don't have to reenter them, just do another export and redraw the boundaries of the model.

JavaScript Applet Example

We'll use this *MX* model, displaying the radius of an incircle to create a JavaScript Applet.



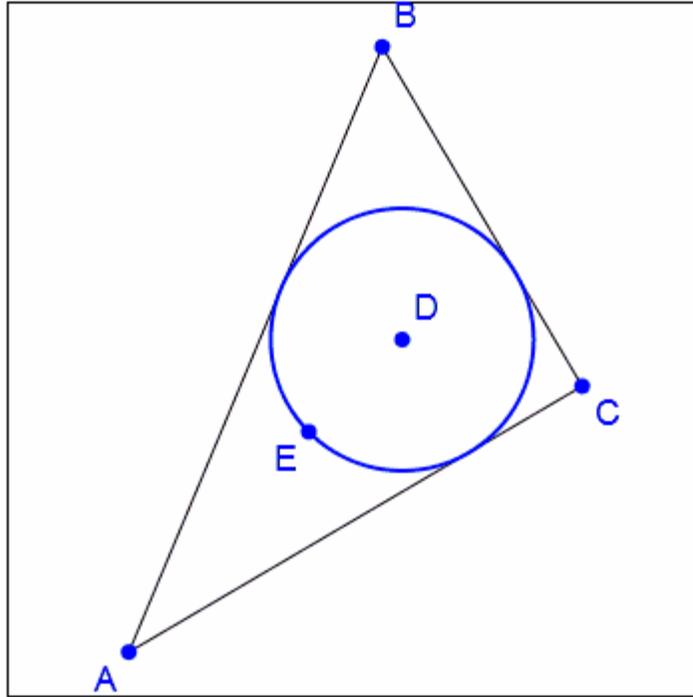
Here are the parameters we entered in the JavaScript Applet Generator dialog:



Here is the result:

Incircle Radius

What lengths make the radius an integer?



side BC

side AC

side AB

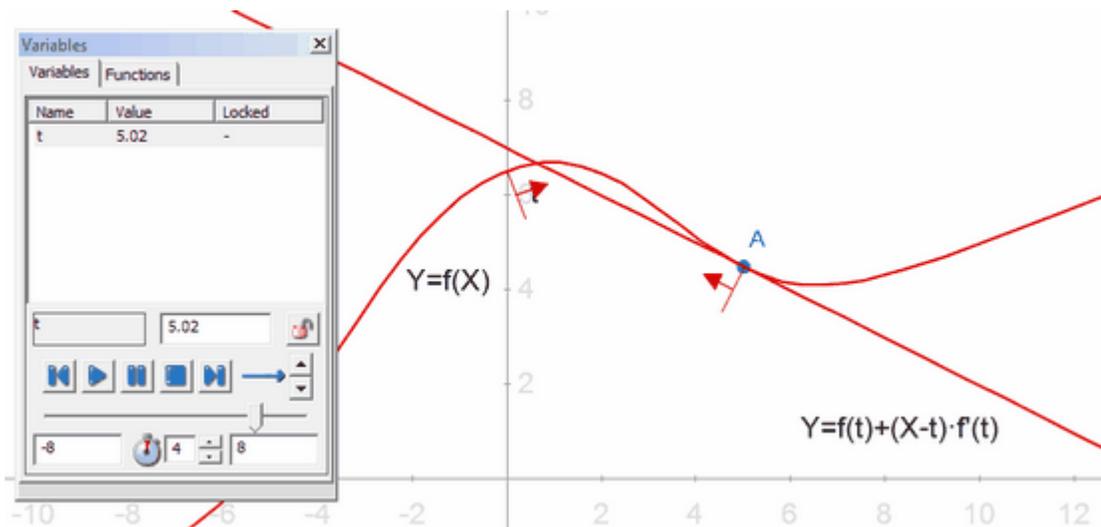
radius 2

What if the triangle is **Pythagorean**?

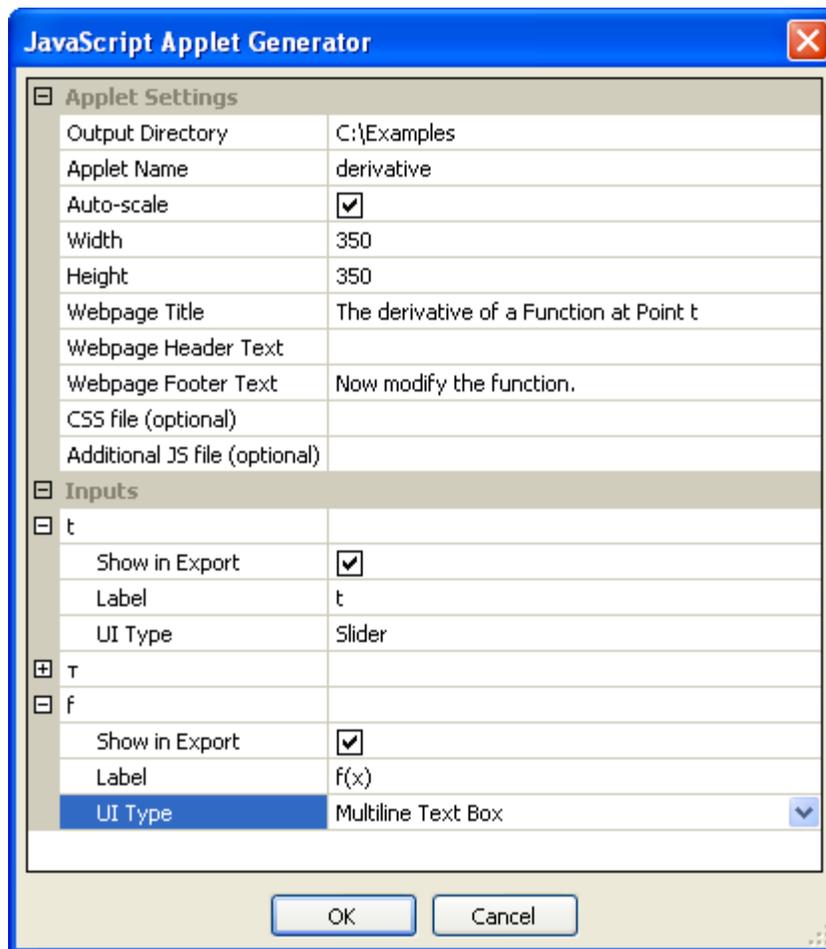
The exported image can be zoomed in and out using the - and + keys on the keyboard or panned around using the arrow keys. If displayed on a touch sensitive device, the app supports multi-touch features.

JavaScript Animated Applet

In this applet, we'll draw a general function, $f(x)$ and then create its derivative at t (using the Point proportional  constraint). Here is the *MX* drawing:

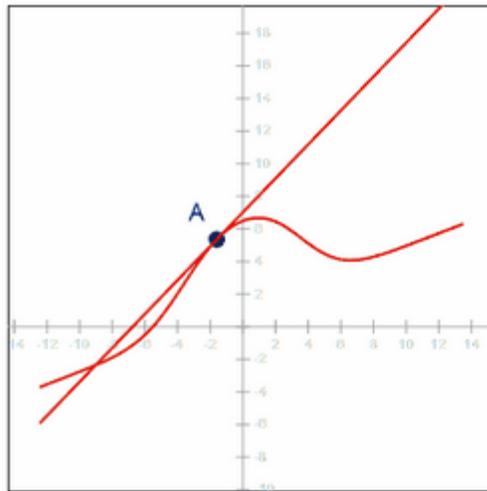


Here are the parameters we entered in the **JavaScript Applet Generator** dialog:



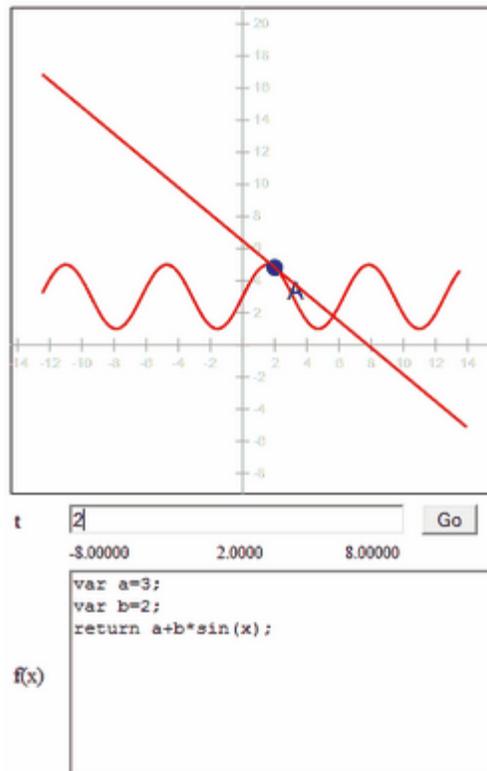
Selecting *slider* for the UI Type of variable t we now have the Go/Stop button to control the animation of t between the ranges defined in the **Variables** panel above.

The Derivative of a Function at Point t



t
-8.00000 5.0227 8.00000
f(x) $\sqrt{((0.38593343068696*x)+1.05$

Now modify the function.



To modify the function, simply type a new one in the edit field. A multi-line function allows more options.

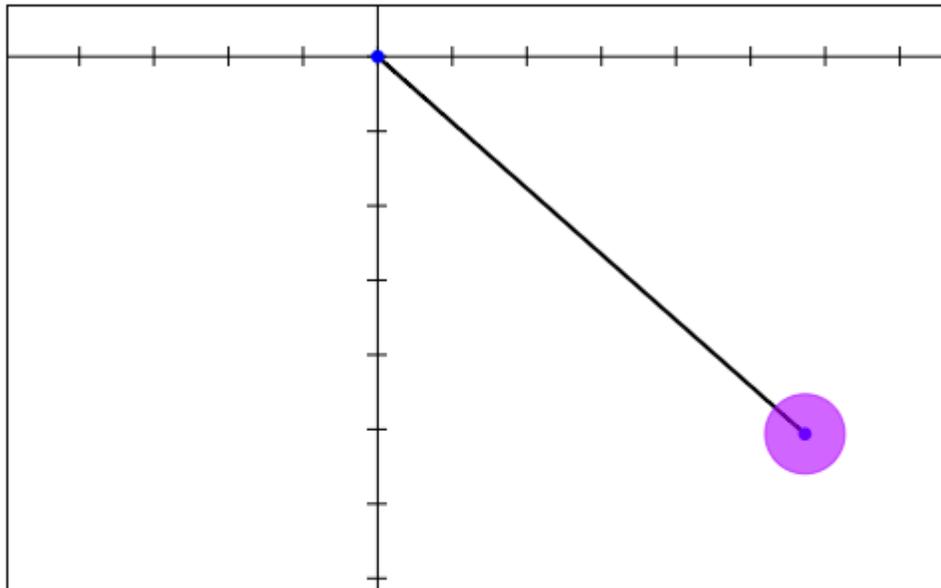
Dynamic Simulations

When you create a dynamic model with constraints which are [Free to Accelerate](#), you can make an app of the Dynamic Simulation.

- Make sure your constraint(s) is a single variable, not an expression.
- Optionally, attach an input [Velocity - Acceleration](#) to your free constraint(s). If you do, it will be taken as the initial condition for the velocity (the acceleration will be ignored, as it is computed from the diagram). If you don't specify an input velocity, an initial condition of 0 velocity will be assumed. Be sure to output the [Resultant Acceleration](#) of your free constraint(s).
- Check that the [Dynamic Simulation](#) checkbox in the JavaScript Applet Generator dialog is checked.
- Other check boxes:

Start/Stop button - if you do not check this box, the simulation starts automatically.

Simulation Speed - you can insert a data entry box to adjust the speed or let it run automatically (as explained below).

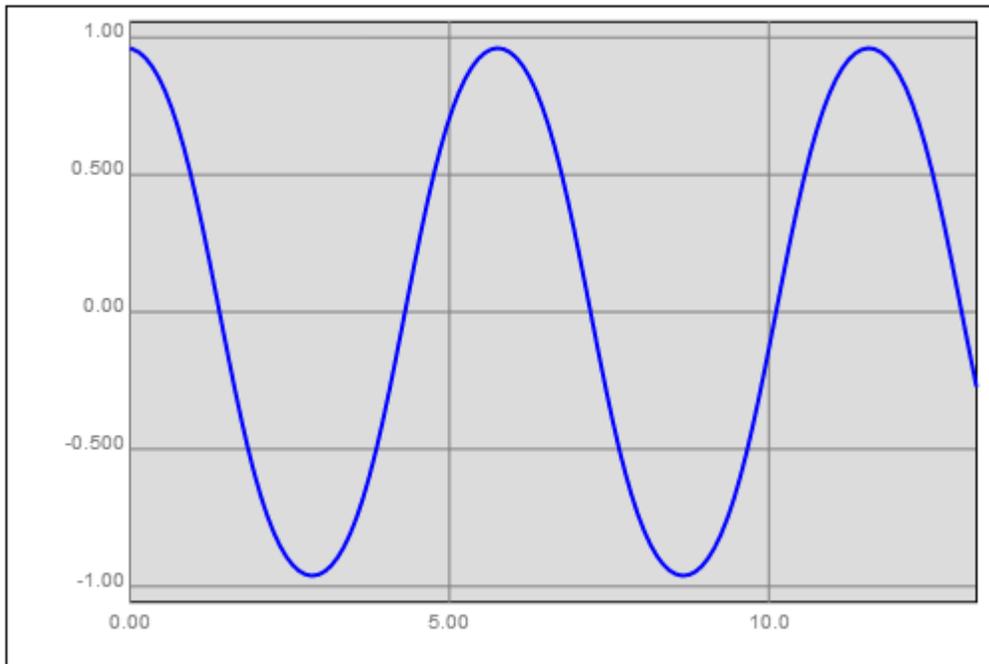


length	<input type="text" value="7.6454"/>	<input type="button" value="▲▼"/>
mass	<input type="text" value="1"/>	<input type="button" value="▲▼"/>
θ	<input type="text" value="41.465"/>	<input type="button" value="▲▼"/>
Simulation Speed	<input type="text" value="1.0"/>	<input type="button" value="▶"/>
Acc:	<input type="text" value="0.96119"/>	<input type="button" value="▼"/>

Below the drawing we can list:

- the inputs
- a Start/Stop button
- the Simulation Speed - this value is relative to model speed. The initial value, 1.0, means that the simulation will go at the same real-time speed as the dynamic model. *E.g.* a 32 foot long pendulum, will take 6.28 seconds to complete its cycle. Increase the speed to 10 and it takes .628 seconds.
- The **Resultant Acceleration**, labeled Acc, updates dynamically.

- To see a graph of the acceleration values, click .



- Click the icon again and you get a table of values which you can copy and paste into another program for further analysis:

time	Acc:
0.0000000	0.96119427
0.0500000	0.95710416
0.1500000	0.94473731
0.2500000	0.92381627
0.3500000	0.89391867
0.4500000	0.85453613
0.5500000	0.80515383
0.6500000	0.74534635
0.7500000	0.67488292
0.8500000	0.59383189
0.9500000	0.50265188
1.0500000	0.40225538
1.1500000	0.29403192
1.2500000	0.17982141
1.3500000	0.06183507
1.4500000	-0.05747011
1.5500000	-0.17554920
1.6500000	-0.28993907
1.7500000	-0.39841700
1.8500000	-0.49912780

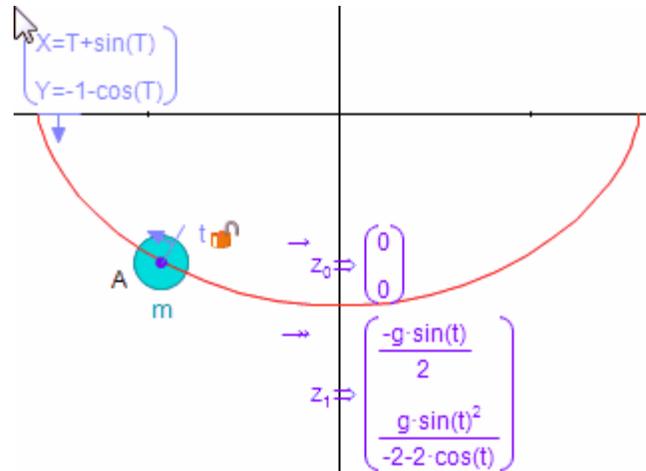
The Brachistochrone Example

An inverted cycloid curve is the solution to the brachistochrone problem: providing the quickest path between two points for a ball rolling under gravity, or a bead sliding on a wire. You can find this model and run the app (Example 23) in the *Examples* subdirectory of your *Mx* installation.

Here are the steps to create the model:

1. Select **Draw / Function**  and choose **Parametric** from the Type window.
2. Enter: $X = T + \sin(T)$, $Y = -1 - \cos(T)$ with T varying from -3.14 to 3.14 .
3. **Draw / Point**  on the curve.
4. Select the point and the curve and choose **Point Proportional** from the **Constrain** toolbox  with a value of t .
5. Select the parameter t and right-click to get the **Context** menu and choose [Free Constraint to Accelerate](#).
6. To see the acceleration of the point over time, τ , select the point and click **Velocity / Acceleration** from the **Mechanics Output** toolbox .

Your model should appear like this:



Now you are ready to **Export / HTML5 / Javascript App**, found in the **File** menu.

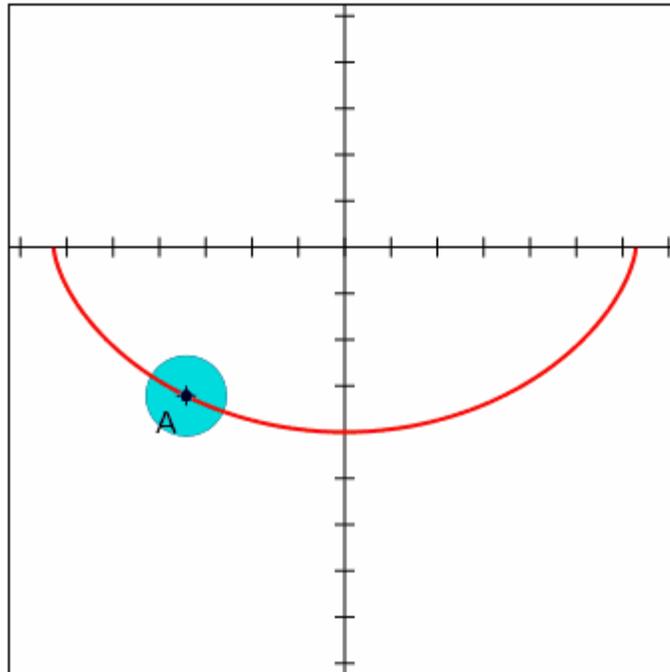
- Specify that the app should contain a simulation, give it a start button (the default has these checked), and set t to be draggable. In the dialog below, we also clarify the labels.

Applet Settings	
Output Directory	C:\SG\SG\Install Source\MechanicalExpressions
Applet Name	Dynamic Simulation 1 - Brachistochrone
Auto-scale	<input checked="" type="checkbox"/>
Width	350
Height	350
Webpage Title	Example 1- The Brachistochrone Problem
Webpage Header Text	
Webpage Footer Text	
CSS file (optional)	
Additional JS file (optional)	
Enable Dynamic Simulation	<input checked="" type="checkbox"/>
Start/Stop Button	<input checked="" type="checkbox"/>
Simulation Speed	<input checked="" type="checkbox"/>
Inputs	
m	
Show in Export	<input checked="" type="checkbox"/>
Label	mass
UI Type	Text Box
t	
Show in Export	<input checked="" type="checkbox"/>
Label	Point position
UI Type	Draggable
τ	
Show in Export	<input type="checkbox"/>
Label	τ
UI Type	Text Box

Outputs	
z[0]	
Show in Export	<input type="checkbox"/>
Label	z[0]
UI Type	Plain Text
z[1]	
Show in Export	<input checked="" type="checkbox"/>
Label	Acc Point A

You can drag the point along the curve and see its change in acceleration. Click the down arrow in the acceleration line to see a graph Click the arrow again to see the table of the output. The App looks like this:

Example 1- Brachistochrone Problem



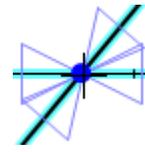
mass
 Simulation Speed
 Acc Point A (3.8918063, -1.9206349)

Trebuchet on Wheels Example

The *Mx Examples* collection contains a stationary trebuchet example (Example 19). We modify this example by adding another degree of freedom to show the recoil of the trebuchet. You can find this model and run the app (Example 24) in the *Examples* subdirectory of your *Mx* installation.

Here are the steps to creating the model:

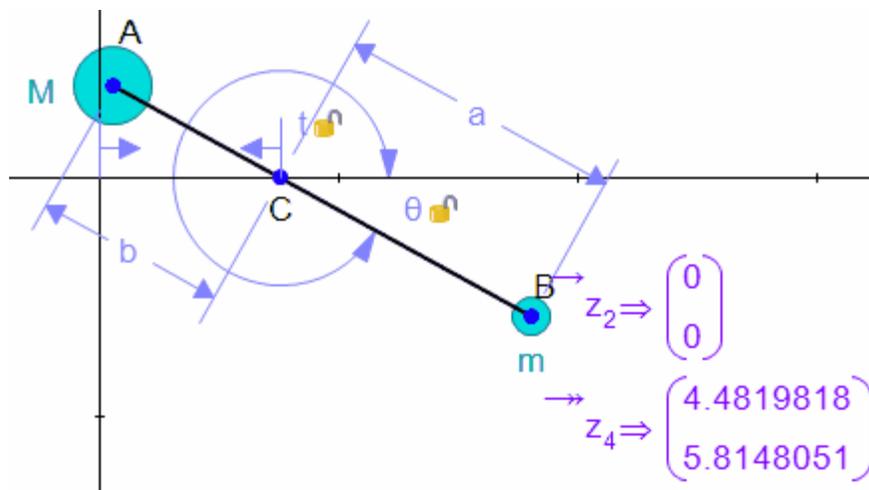
1. Draw a line segment over the x axis, but not through the origin.
2. Draw a point at the intersection of the line with the x axis. (You



should see the double bow tie before you click.)

3. Constrain the distances from each end of the line to the new point (a and b).
4. Select the point and the x axis and click **Point Proportional**  in the **Constrain** toolbox. Hit *enter* to accept the default parameter, t .
5. Select an endpoint and click **Mechanics Input / Mass** , to apply masses M and m to the line's endpoints.
6. Select the arm and the x axis to constrain the angle between the two with the default parameter, θ .
7. Select θ and t , right click, and select **Free Constraint to Accelerate**.
8. To see the acceleration of the point over time, τ , select the point B and click **Mechanics Output/ Velocity / Acceleration** in the **Real** tab (the symbolic expression is rather involved) .

Your model should appear like this:



Now you are ready to **Export / HTML5 / Javascript App**, found in the **File** menu.

9. Specify that the app should contain a simulation, give it a start button (the default has these checked).
10. Uncheck the Auto-scale box in the Applet Settings section. When you finish entering all the applet details, *Mx* prompts you to select the drawing area. Remember to leave enough space around the trebuchet in order to see its entire movement.

Here are the app specifications:

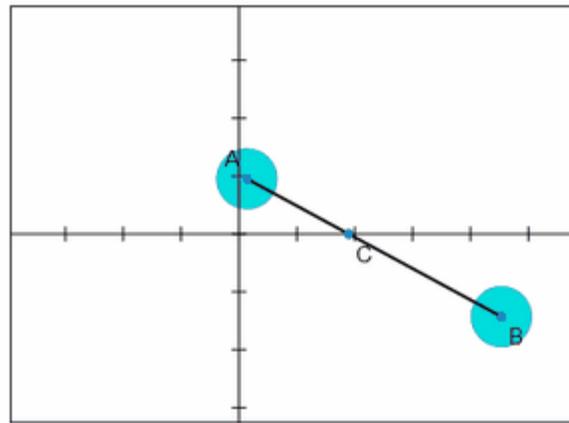
Auto-scale	<input type="checkbox"/>
Width	400
Height	400
Webpage Title	Trebuchet on Wheels
Webpage Header Text	The length of the arm from the fulcrum to A is
Webpage Footer Text	
CSS file (optional)	
Additional JS file (optional)	
<input type="checkbox"/> Enable Dynamic Simulation	<input checked="" type="checkbox"/>
Start/Stop Button	<input checked="" type="checkbox"/>
Simulation Speed	<input checked="" type="checkbox"/>
<input type="checkbox"/> Inputs	
<input type="checkbox"/> M	
Show in Export	<input checked="" type="checkbox"/>
Label	M
UI Type	Text Box
<input type="checkbox"/> a	
Show in Export	<input checked="" type="checkbox"/>
Label	a
UI Type	Text Box
<input type="checkbox"/> b	
Show in Export	<input checked="" type="checkbox"/>
Label	b
UI Type	Text Box
<input type="checkbox"/> m	
Show in Export	<input checked="" type="checkbox"/>
Label	m
UI Type	Text Box
<input type="checkbox"/> t	
Show in Export	<input checked="" type="checkbox"/>
Label	t
UI Type	Text Box
<input type="checkbox"/> θ	
Show in Export	<input checked="" type="checkbox"/>
Label	θ
UI Type	Slider

Outputs	
z[2]	
Show in Export	<input type="checkbox"/>
Label	Vel_B
UI Type	Plain Text
z[4]	
Show in Export	<input checked="" type="checkbox"/>
Label	Acc_B
UI Type	Plain Text

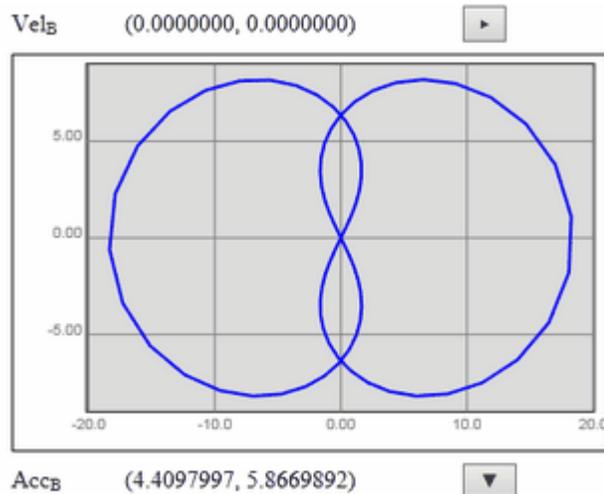
Click the down arrow in the Velocity or Acceleration line to see a graph. Click the arrow again to see the table of the output. Here's the app:

Trebuchet on Wheels

The length of the arm from the fulcrum to A is b ; from fulcrum to B is a . The counterweight of mass M is at A and the missile of mass m is at B. We model the recoil with parameter t , the position of the fulcrum on the x axis. θ is the angle of the arm to the horizontal. With t and θ free to accelerate, we examine the acceleration of point B.



M
 a
 b
 m
 θ
 0 5.7871444 6.2831853
 Simulation Speed

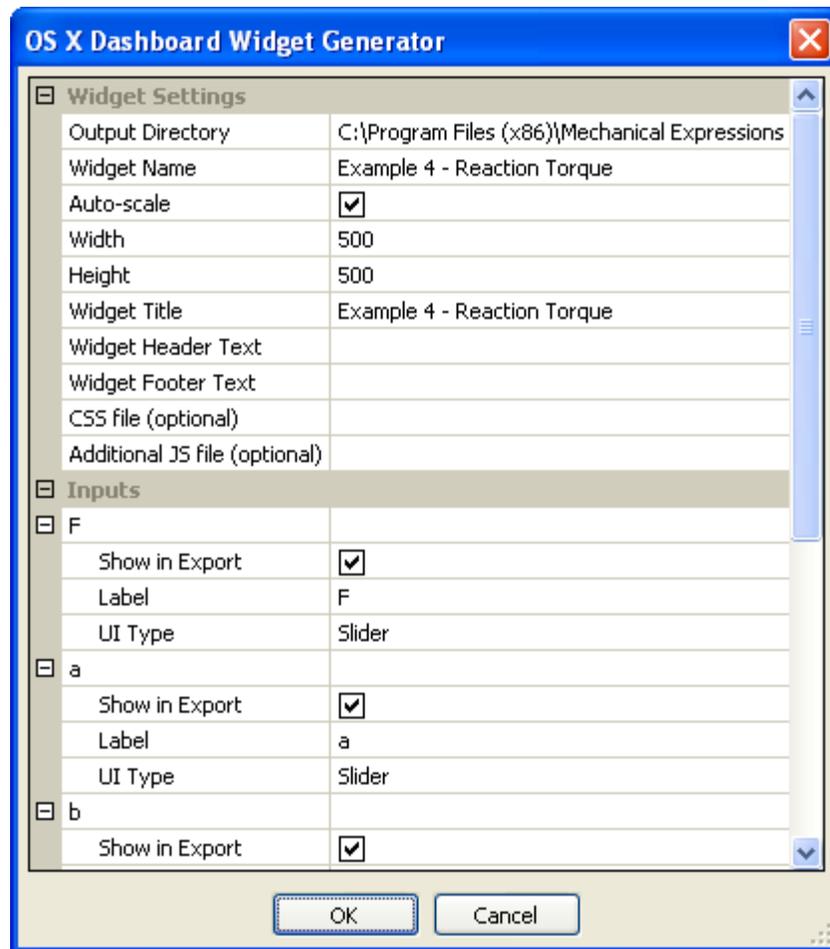


To get a smoother graph, decrease the Simulation Speed.

Creating OS X Dashboard Widgets

Dashboard Widgets are very similar to *JavaScript Applets*, but they sit on The *Mac Dashboard*. Select **File / Export / OS X Dashboard Widgets**.

Fill out the details in the **OS X Dashboard Widget Generator** dialog.



Output directory - tells *MX* where to put the files. It will create a folder: *name.wdgt* containing all the components of the widget.

Widget Name - is the name of the folder and the main .html file.

Auto-scale - when check, the Widget automatically rescales the drawing when the user changes the value of one of the inputs; when unchecked, you click-and-drag a rectangle around the drawing after you click Ok.

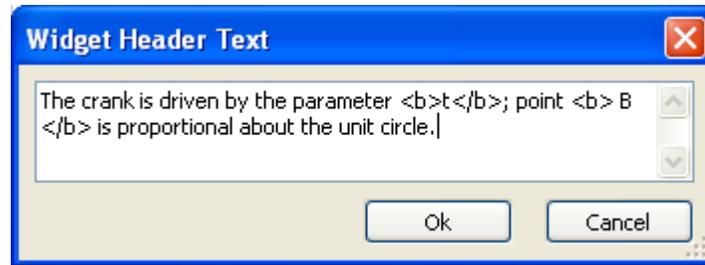
Width and Height specify the size of the drawing in the Widget box.

Widget Title, Widget Header Text, and Widget Footer Text - enter your text for these sections.

Since header and footer text may be several lines long, You can go back and change these text boxes before you close the dialog:

- select the text entry box
- click the  to display the dialog
- enter or edit text, then click Ok.

Note: you can insert html code into the header and footer text, e.g. to make a word in the footer text bold:



CSS file (optional) - you can attach your favorite Cascading Style Sheet, without having to reproduce it every time.

Inputs - lets you choose which variables the user will be able to change, what text Label identifies the variable and what type of control to use.

Any variables in your *MX* model may be selected as input variables in the Widget. See the topic detailing [UI Types](#) below.

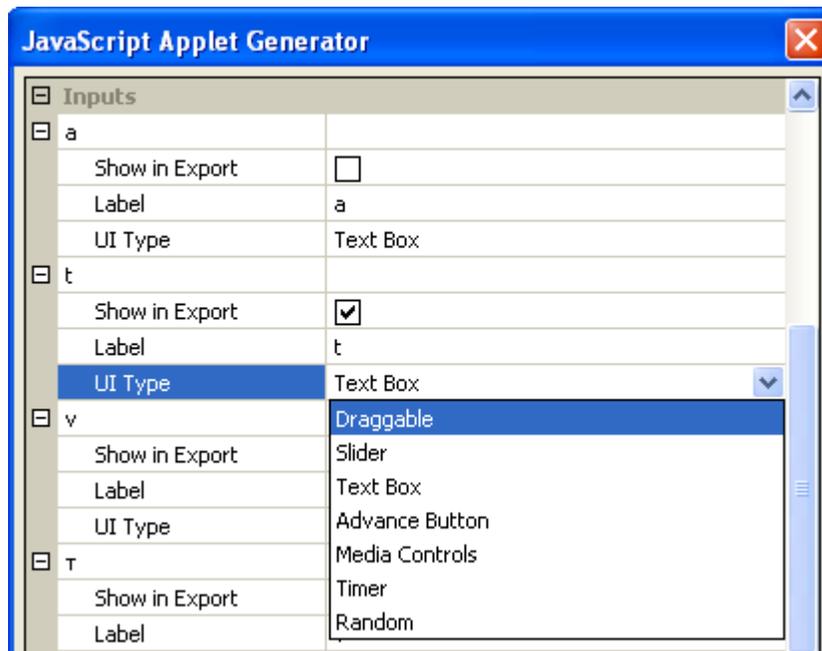
Outputs - lets you choose which outputs will appear in the applet, and their text Label.

Any measurements which are present in the *Mechanical Expressions* model may be chosen as outputs for the widget.

UI Types for Applets

JavaScript, Lua Apps and Widgets use identical Input and Output types. Here are the selections.

Inputs



Draggable - any points in the *Mechanical Expressions* model constrained by variable **Coordinates** or a variable parameter for the **Point Proportional** constraint can be set as **Draggable** points in the *JavaScript, Lua* app or *Widget*. The point's constraint variables, however, cannot be functions or negative; only positive variables are allowed for defining draggable points. *I.e.*, the value of the variable may very well be negative, but using $-t$ as the point proportional parameter or $(x, 3*x)$ as a point's coordinates prevents the point from being draggable.

Slider - takes it's range from the values specified in the *MX Animation* in the **Variables** panel.  Please note - not all browsers support sliders.

Text Box - lets you enter any numeric value for the variable.

For a function, you have the choice of a single line **Text Box** or a [Multiline Text Box](#). Remember to use the *JavaScript return* statement in multi-line statements in *JavaScript Apps* or *Widgets*.

Inputs	
t	
Show in Export	True
Label	t
UI Type	Text Box
f	
Show in Export	True
Label	f(x)
UI Type	Text Box
	Text Box
	Multiline Text Box

 Note: when defining variables or functions in the edit field of *JavaScript Apps* or *Widgets*, remember that *JavaScript* does not use "^" to denote a power. X^2 must be written: `pow(X,2)`.

Advance Button - displays the variable **Label** on a button and increments the variable when clicked. Uses the [range](#) and [direction](#) from the *MX* animation settings. If you used decimal values in *MX*, the values are reduced to integers.

Media Controls - works like the **Advance Button** but gives you some additional options. For values within the specified range, you can:

- increment or decrement regardless of the mode setting
- jump to a specific integer value by typing (as in the **Text Box** mode)
- jump to the beginning or end of the range

Timer - this is great for making [Clock Applets](#) and smooth animations. Here are the **Timer Styles**:

⊖ θ	
Show in Export	<input checked="" type="checkbox"/>
Label	θ
UI Type	Timer
Timer Style	Animation period, continuous
⊖ τ	Animation period, continuous
Show in Export	1 minute period, continuous
Label	1 minute period in 1 second increments
UI Type	1 hour period, continuous
⊖ ω	1 hour period in 1 minute increments
Show in Export	12 hour period, continuous
Label	24 hour period, continuous

The hour, minutes and seconds are taken from your computer's clock.

Random - gives the specified variable a single random value within the [range](#) set in the *MX Variables* tool panel. To change the variable's value to another random number click the **Reload** button .

Outputs

Any measurements which are present in the *Mechanical Expressions* model may be chosen as outputs for the *JavaScript*, *Lua Apps* or *Widgets*. Check the **Show in Export** checkbox and modify the **Label** if needed.

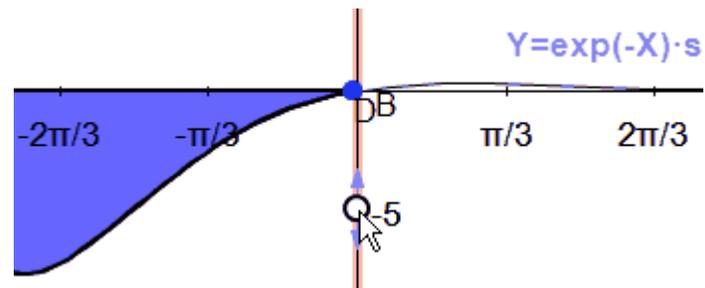
⊖ Outputs	
⊖ z[1]	
Show in Export	<input checked="" type="checkbox"/>
Label	z[1]
UI Type	Plain Text
⊖ z[2]	Plain Text
Show in Export	Show/Hide Button

UI Type - Plain Text or Show / Hide Button which is a toggle.

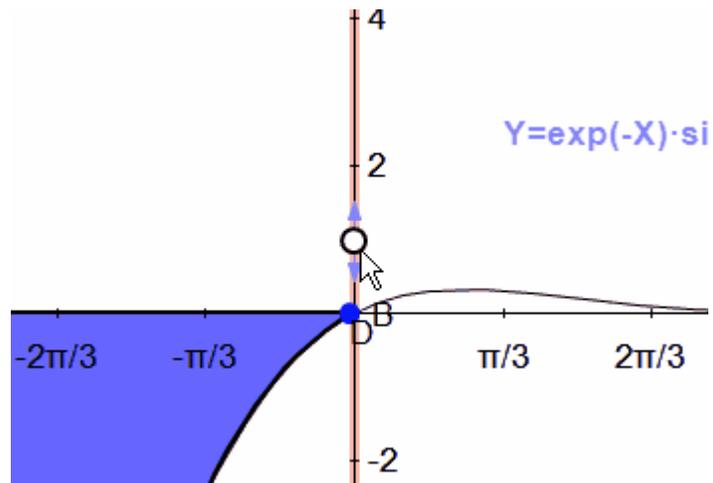
Graphing Mode

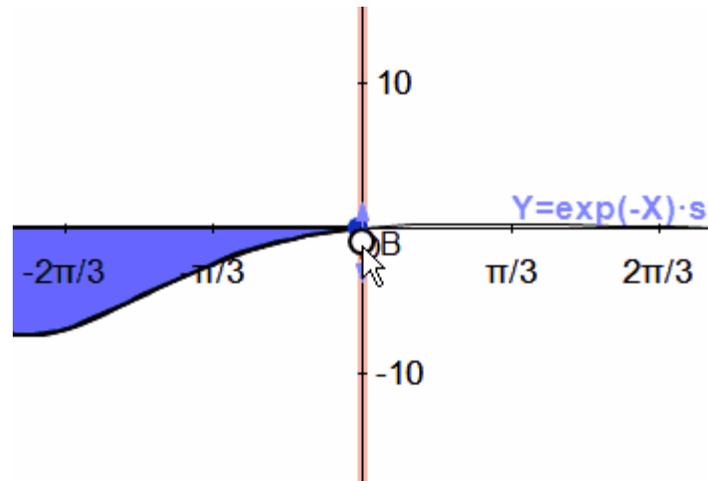
When you need to draw a graph requiring independent scaling of the axes, select **File / New Graph**.

- Draw your graph.
- Click an axis - the axis will be highlighted and a circular handle appears.



- Slide the handle up and down the axis with your mouse.





Note: Many of the geometry drawing, constraint and construction tools are unavailable (grayed out) in the Graphing mode for obvious reasons related to the independent scaling of the axes.

Edit Menu

The **Edit** menu contains the standard Windows editing operations as well as ways of dealing with constraint conflicts and all of the program settings. Several of the options are also available from the icon bar.

Menu Option	Function	When Available
 Undo	Reverses actions starting with the last one.	After any action has been taken.
 Redo	Reinstates actions starting with the last one that was undone.	After using Undo
 Select	When checked, the select mode is active.	Select mode is always active except when using a Drawing tool or moving or panning the drawing .
Select All	Selects everything in the drawing window.	Always
Select All Type	Presents a submenu of	Always -- most useful

	object types to select.	when the object type is in the window.
Clear Selection	Unselects any objects that are selected.	Always
 Cut	Deletes an object, but saves it so it can be pasted somewhere else.	An object is selected
 Copy	Does not delete the object, but saves it so it can be pasted somewhere else.	An object is selected
Copy As	Displays a submenu of choices for copying mathematics into other programs.	An expression or formula is selected
 Copy Drawing	Copies everything in the drawing window as an Enhanced Metafile (.emf)	Always
 Copy Region	Copies a section of the drawing window inside a rectangle made by dragging the cursor.	Always
 Paste	Puts whatever has been cut or copied into the current drawing	Object(s) cut or copied
Delete	Deletes whatever is selected, without saving it.	One or more objects selected
Arrange	For placing selected objects on top of (bring forward) or underneath (send backward) other objects for easier selection and viewing.	One or more objects selected

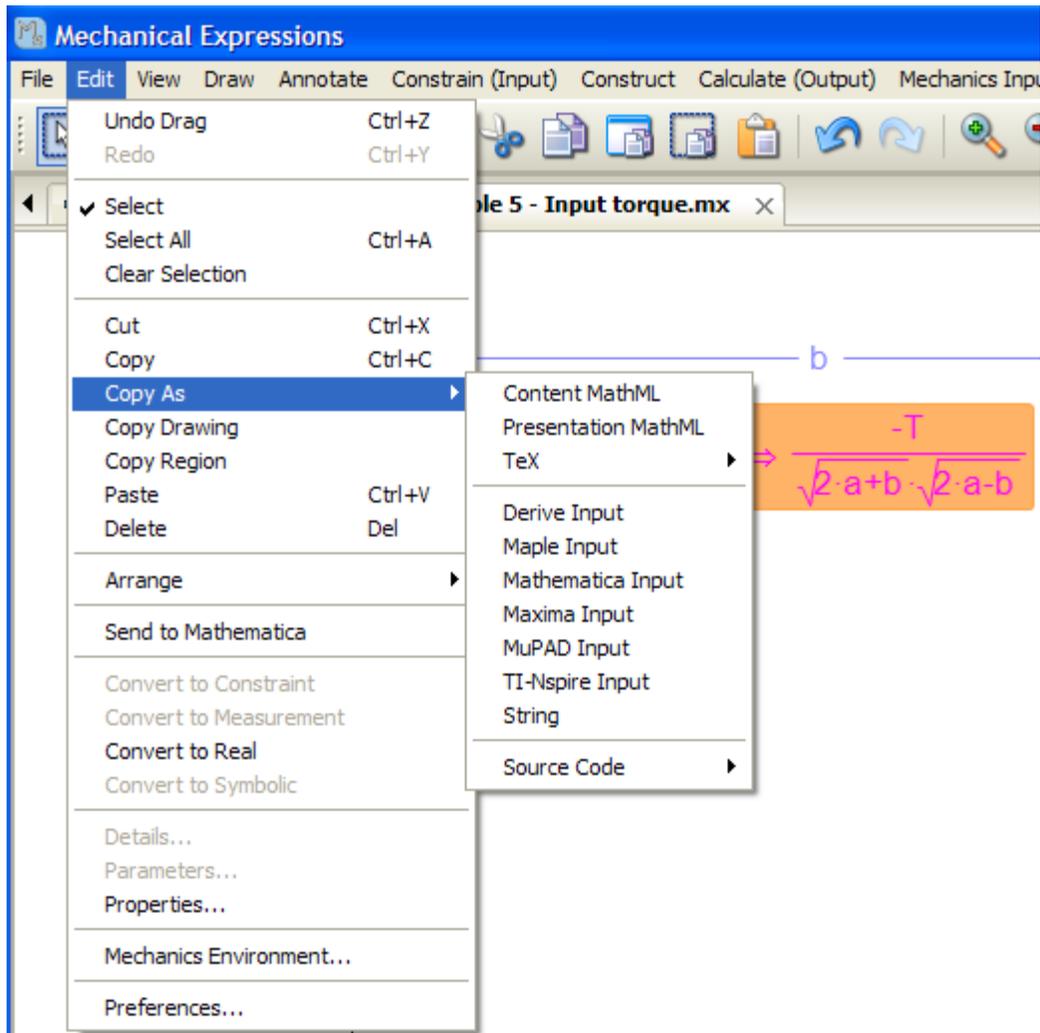
Send to <i>Mathematica</i>	Inputs the math to <i>Mathematica</i> when the algebra system is running in another window.	Windows version only An output expression or formula is selected
Convert to Constraint	Tries to convert a selected output [=2θ] to an input constraint if there is no conflict with other constraints	An output expression is selected
Convert to Measurement	Converts the selected constraint into a measurement (output)	An input constraint is selected
Convert to Real	Converts a symbolic calculation to a real one	A symbolic output is selected
Convert to Symbolic	Converts a real calculation to a symbolic one	A real output is selected
Free Constraint to Accelerate	Frees constraint to create a dynamic model	An constraint is selected
Details. . .	Displays the Edit Text dialog to edit a block of text	A block of text is selected
Parameters. . .	Lets you edit the parameters of functions, loci and traces.	A function, locus or trace is selected
Properties. . .	Lets you edit the display properties of the selected object(s)	One or more objects of the same type are selected
Mechanics Environment	Sets the default Mechanics properties.	Always
Preferences . . .	Sets the default appearance and properties for the project's drawing, text and mathematics	Always

NOTE: For the Mac version, **Preferences** are found under the **Mechanical Expressions** menu.

Copying Mathematics

To copy expressions or functions into an Algebra system or another program:

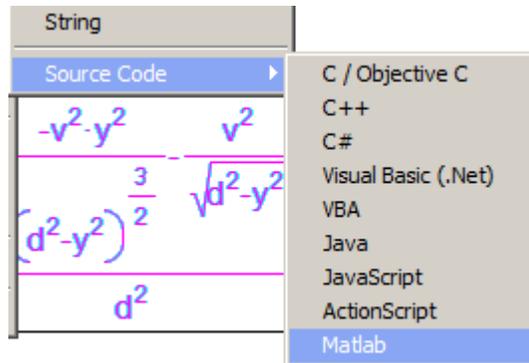
- Select the math from the Diagram or the Output window.
- Select **Edit / Copy As** or [right-click the selected expression](#) to display the submenu of choices for copying expressions or functions from *Mechanical Expressions* to another program.



- The 2 general types of MathML are available, Content and Presentation MathML, as well as formats meeting the specific quirks of several popular Computer Algebra programs.
- The TeX typesetting output gives you 3 choices in the submenu: Inline, Display, and Wikipedia. The actual TeX produced is identical, except for the delimiters which mark the start and finish of the TeX code.
- There is also a general purpose String output which converts the selected math into a text string containing no special characters:

$\Rightarrow \sqrt{a^2+b^2-2\cdot a\cdot b\cdot \cos(\theta)}$ is copied as `> (((a)^(2)+(b)^(2)+(cos(theta)*b*a*(-2))))^(1/2).`

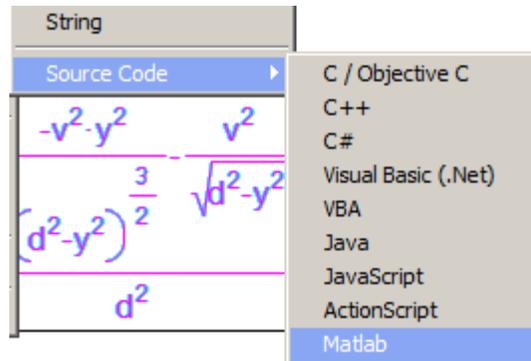
- Generate [Source Code](#) from *Mechanical Expressions* in a number of different languages:



When you make a submenu selection, the selected math is copied to the *Windows* clipboard, ready to be pasted into the appropriate application (Ctrl+V).

Generating Source Code

You can generate computer source code from *Mechanical Expressions* in a number of different languages.



There are two types of expression in *Mechanical Expressions*:

- Scalar
- Vector

The source code will be in a different form depending on whether there are [intermediate variables](#) present or not.

Note that there is not much difference between the languages in the mathematical expressions they generate. The main differences are:

- C#, Java, Javascript, ActionScript, Visual Basic (.net), and Lua prefixes math functions with "Math."
- C / C++ and VBA do not use any prefix for the math functions

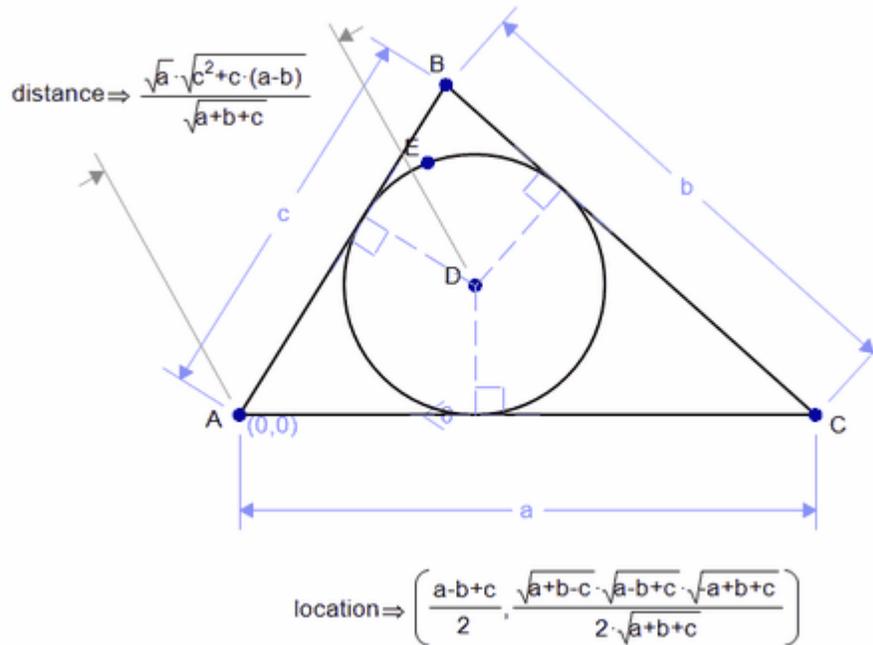
Each language has its own way of invoking functions. In the cases where a vector is returned from the function, the different languages work in different ways.

- In C pointers to doubles representing the x and y coordinates of the vector are passed into the function.
- In C++, Visual Basic and VBA, references to doubles representing the x and y coordinates of the vector are passed into the function.
- In C# double out parameters for the x and y coordinates of the vector are used.
- In Java, JavaScript and ActionScript, an array is passed into the

function, the 0th and 1st elements of the array will acquire the x and y coordinates of the vector.

Source Code Examples

From the following example we'll copy the expressions for the location of point D (a vector) and distance AD (a scalar) in our code generation.



Scalar / No Intermediate Variables

- Select the *distance* expression.
- Right-click and select **Copy As / Source Code / C/Objective C**

In this case the code generates a single expression (here we are generating C):

```
(pow((pow(c,2)+((a+(b*-1))*c)),0.5)*pow((a+b+c),-0.5)*pow(a,0.5)).
```

Scalar / Intermediate Variables

With intermediate variables showing we get the following for the distance expression:

```
double distance(
```

```
double a ,
double b ,
double c )
{
double d_1;
double v_1;
double phi_0;
double d_2;
double d_0;
double u_1;
d_1 =
(pow(((a*-1)+b+c),0.5)*pow((a+(b*-1)+c),0.5)*pow((a+b+(c*-1)),0.5)
*pow((a+b+c),0.5));
v_1 = (d_1*pow(a,-1)*0.5);
phi_0 = ((a+b+c)*v_1*pow(c,-1)*pow(b,-1));
d_2 = (v_1*pow(b,-1)*a*-1);
d_0 = (pow(a,2)+(pow(b,2)*-1)+pow(c,2));
u_1 = (d_0*pow(a,-1)*0.5);
return
(pow(fabs(phi_0),-1)*fabs(d_2)*pow((pow(c,2)+(u_1*c*2)+pow(u_1,2)+
pow(v_1,2)),0.5)*pow(c,-1));
}
```

We see that the name of the function is the name of the expression in Mechanical Expressions, its parameters are the input variables, and its return value is the value of the expression.

Vector / Intermediate Variables

Select the *location* expression, a vector value, and our function returns two quantities. This is done in different ways for different languages:

C / Objective C

Pointers to doubles are passed into the function:

```
void location(  
    double a ,  
    double b ,  
    double c ,  
    double *location_x_ ,  
    double *location_y_ )  
{  
    double location_x;  
    double location_y;  
    double d_1;  
    double v_1;  
    double d_2;  
    double d_0;  
    double u_1;  
    double phi_0;  
    d_1 =  
(pow(((a*-1)+b+c),0.5)*pow((a+(b*-1)+c),0.5)*pow((a+b+(c*-1)),0.  
5)*pow((a+b+c),0.5));  
    v_1 = (d_1*pow(a,-1)*0.5);  
    d_2 = (v_1*pow(b,-1)*a*-1);  
    d_0 = (pow(a,2)+(pow(b,2)*-1)+pow(c,2));  
    u_1 = (d_0*pow(a,-1)*0.5);  
    phi_0 = ((a+b+c)*v_1*pow(c,-1)*pow(b,-1));  
    location_x = (((d_2*-1)+(u_1*d_2*pow(c,-1)*-1))*pow(phi_0,-1));  
    location_y = (pow(phi_0,-1)*v_1*d_2*pow(c,-1)*-1);  
    *location_x_ = location_x;  
    *location_y_ = location_y;  
}
```

C++

References are passed into the function:

```
void location(  
    double a ,  
    double b ,  
    double c ,  
    double &location_x_ ,  
    double &location_y_ )  
{  
    double location_x;  
    double location_y;  
    ...  
    location_x_ = location_x;  
    location_y_ = location_y;  
}
```

C Sharp

Out parameters are passed into the function:

```
void location(  
    double a ,  
    double b ,  
    double c ,  
    out double location_x_ ,  
    out double location_y_ )  
{  
    double location_x;  
    double location_y;  
    ...  
    location_x_ = location_x;  
    location_y_ = location_y;
```

}

Visual Basic / VBA

References are passed into the function:

```
Sub z_0(ByVal a As Double , ByVal b As Double , ByVal c As Double ,  
ByRef z_0_x_ As Double ,ByRef z_0_y_ As Double )
```

```
    Dim z_0_x As Double
```

```
    Dim z_0_y As Double
```

```
    ...
```

```
    z_0_x_ = z_0_x
```

```
    z_0_y_ = z_0_y
```

```
End Sub
```

Java

An array of doubles of size 2 is passed in and populated by the function:

```
double location(  
    double a ,  
    double b ,  
    double c ,  
    double[] location_v )
```

```
{
```

```
double location(  
    double a ,  
    double b ,  
    double c ,  
    double[] location_v )
```

```
{
```

```
    double location_x = 0;
```

```
    double location_y = 0;
```

```
    ...
```

```
    location_v[0] = location_x;
    location_v[1] = location_y;
}
```

JavaScript

An array is passed in and populated by the function:

```
function location(
    a ,
    b ,
    c ,
    location_v )
{
    var location_x = 0;
    var location_y = 0;
    ...
    location_v[0] = location_x;
    location_v[1] = location_y;
}
```

Action Script

An array is passed in and populated by the function:

```
public function location(
    a:Number ,
    b:Number ,
    c:Number ,
    location_v:Array) )
:void
{
    var location_x:Number;
    var location_y:Number;
```

...

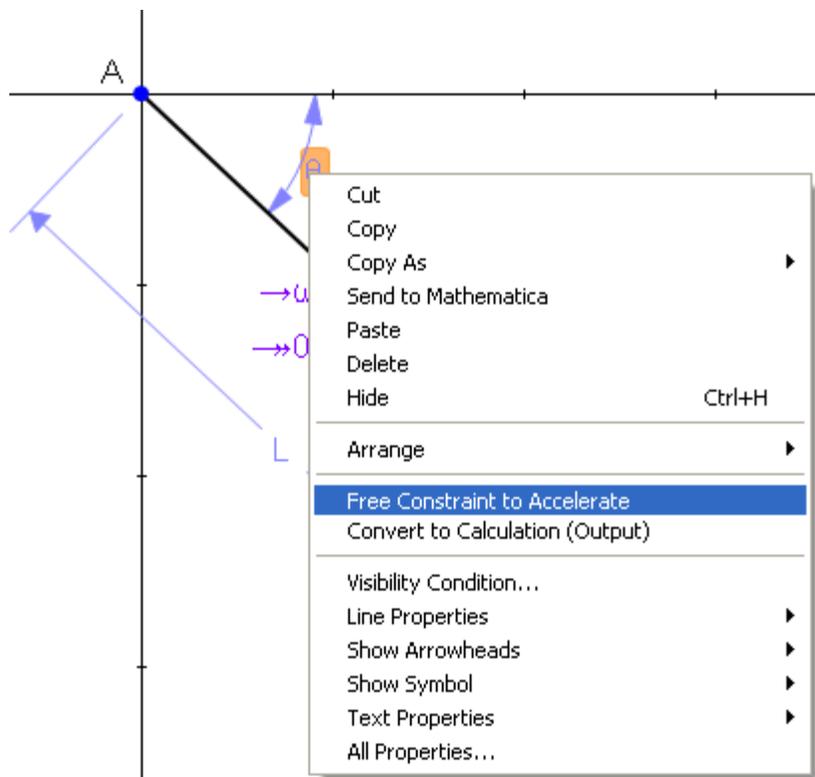
```
location_v[0] = location_x;
```

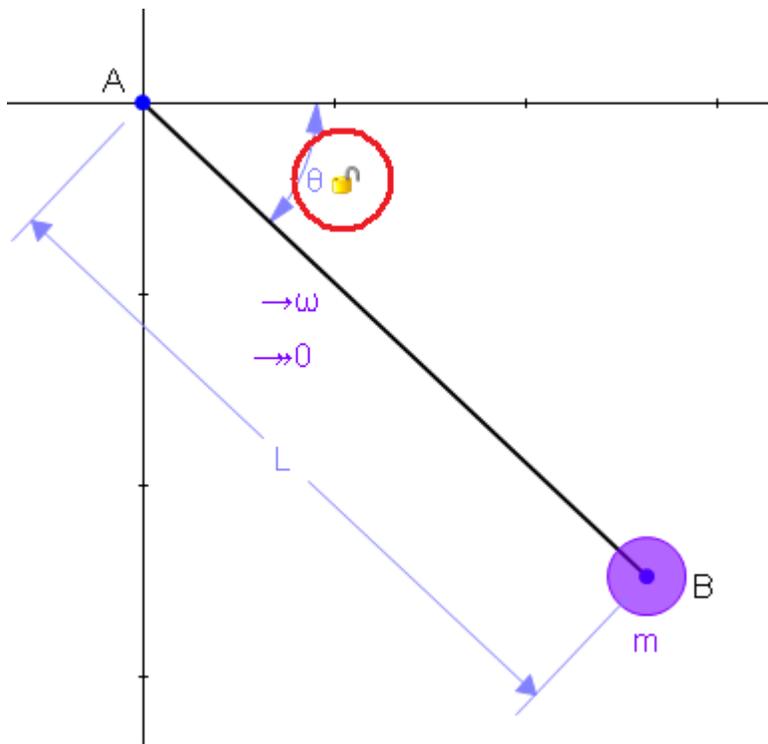
```
location_v[1] = location_y;
```

```
}
```

Free Constraint to Accelerate

To create a dynamic model in *Mechanical Expressions*, you need to first create a static model, specifying constraints which will bear the load of any unbalanced forces. You then need to specify which of these constraints are in fact free to accelerate. You do this by selecting the constraints then using the [right click menu option](#) or the **Edit** menu option. When the constraint is free to accelerate you will see a small unlocked icon.





If a constraint has an input velocity and acceleration, and is made free to accelerate, then the input acceleration is not used. Instead an acceleration is computed for the constraint based on the existing force elements and mass elements. This computed acceleration is used in calculating other mechanics outputs, such as reaction forces, velocities and accelerations.

If you measure the resultant acceleration of a constraint, the system automatically frees that constraint. If you then delete the resultant acceleration, the constraint is still left free to accelerate. To stop the constraint being free to accelerate, you need to toggle it off using the right click or the **Edit** menu.

View Menu

The table below lists the complete summary of **View** functions.

Menu Option	Function	When Available
-------------	----------	----------------

Hide	Hides a selection	One or more elements are selected.
Show all	Displays any entities that were hidden	One or more elements are hidden.
 Toggle Hidden	Lets you toggle hidden / visible for any object in the drawing	Always (if the drawing window isn't empty)
Zoom In	Makes the drawing details larger without affecting the size on the printed page. (The text gets larger on the screen.)	Always available - (most useful when there is something in the drawing window).
Zoom Out	Makes the drawing details smaller without affecting the size on the printed page. (The text gets smaller on the screen.)	Always available - (most useful when there is something in the drawing window).
Zoom To Selection	Lets you make a selection and adjusts it to fit the drawing window. (The text gets larger on the screen.)	Always available - (most useful when there is something in the drawing window).
Zoom To Fit	The entire diagram is displayed in the drawing window. (The text size changes with the geometry.)	Always available - (most useful when there is something in the drawing window).
Zoom To Page	The whole page is displayed in the drawing window. (The text size changes with the geometry.)	Always available - (most useful when there is something in the drawing window).
 Pan View	Allows you to move the contents of the drawing window without changing its position on the page.	Always available - either Pan View or Move Geometry will be in effect (checked).

 Scale Geometry Up	Enlarges only the geometry. (The text size on the screen doesn't change.)	Always
 Scale Geometry Down	Shrinks only the geometry. (The text size on the screen doesn't change.)	Always
 Scale Geometry To Selection	Lets you select a portion of the geometry and adjusts it to fit the drawing window (The text size on the screen doesn't change.)	Always
 Scale Geometry To Fit	Adjusts all geometry to fit in the drawing window. (The text size on the screen doesn't change.)	Always
 Scale Geometry To Page	Adjusts all geometry to fit inside the specified page boundaries. (The text size doesn't change relative to the page.)	Always
 Move Geometry	When checked, click and drag to move the drawing contents with respect to the page boundaries.	Always. Make sure Page Boundaries is checked (below) to see the results.
 Axes	When checked, the axes are displayed. They have the properties of Infinite Lines .	Always
 Grid	When checked, the grid is displayed.	Always
Page Boundaries	When checked, the page boundaries are displayed.	Always
Tool Panels	Lists all the toolboxes.	Always

	When checked, the toolboxes are displayed on the screen.	
Tool Panel Configurations	Gives you options for arranging the toolboxes to your preference.	
Output	When checked, the output window is displayed.	Always
Language	The current version of <i>Mechanical Expressions</i> can be displayed in English, French, German, Spanish, Polish , or Russian . Choose one and restart the program.	Always

Checked menu options are toggles:

- Checked indicates the option / mode is active or displayed.
- Unchecked indicates the option / mode is inactive or hidden.
- Except **Pan View** and **Move Geometry** where one or the other is checked.

Click the selection to change its state.

Some menu items have icon shortcuts found on the icon bar at the top of the screen.

Zooming and Scaling

The **View** menu has **Zoom** operations pertaining to the screen view, and **Scale** operations pertaining to the page view.

- Zooming makes the drawing details smaller without affecting the size on the printed page. The text (constraints, output and annotation) changes size with the rest of the drawing.
- Scaling adjusts the size of the geometry relative to the page, but the

text doesn't change size in the drawing window. Check **View / Page Boundaries** to see this work.

The **Scale** functions used from the icon bar at the top of the screen can be changed to **Zoom** functions by holding the ctrl key while clicking the icon. This is handy if you need to change the size of the text on the screen:

- A **Scale down**  followed by a **Zoom in** [ctrl]  has the effect of enlarging the text.
- A **Zoom out** [ctrl]  followed by a **Scale up**  has the effect of shrinking the text on the screen.

Toolbox Menus

The menus with the same name as the toolboxes at the side of the screen just give another way of accessing the same functions.

Menu Option	Selection		
<u>Draw</u>	<u>Point</u>	<u>Line Segment</u>	<u>Infinite Line</u>
	<u>Vector</u>	<u>Polygon</u>	<u>Circle</u>
	<u>Ellipse</u>	<u>Parabola</u>	<u>Hyperbola</u>
	<u>Arc</u>	<u>N-gon</u>	<u>Curve</u> <u>Approximation</u>
	<u>Text</u>	<u>Picture</u>	<u>Expression</u>
	<u>Function</u>		
<u>Annotate</u>	<u>Angle</u>	<u>Distance /</u> <u>Length</u>	<u>Coefficients</u>
	<u>Coordinate</u>	<u>Radius</u>	<u>Expression</u>
	<u>Direction</u>	<u>Slope</u>	
<u>Constrain</u>	<u>Distance /</u> <u>Length</u>	<u>Radius</u>	<u>Perpendicular</u>

	Angle	Direction	Slope
	Coordinate	Coefficients	Tangent
	Incident	Congruent	Parallel
	Equation	Proportional	
Construct	Midpoint	Intersection	Perpendicular Bisector
	Angle Bisector	Parallel	Perpendicular
	Tangent to Curve	Polygon	Reflection
	Translation	Rotation	Dilation
	Locus	Trace	Area Under Arc
Calculate	Distance / Length	Radius	Angle
	Direction	Slope	Coordinates
	Area	Perimeter	Coefficients
	Parametric Equation	Implicit Equation	
	Stop Calculations	Start Calculations	

Help Menu

The **Help** menu lets you access this help system, check for updates, change the program's language, and gives you information about the program's license and version.

The menu selections are always available.

Menu Option	Function
Dynamic Help	Invokes the Help system

Contents. . .	Look in the Table of Contents; add new or refer to saved bookmarks.
Index. . .	Look in the Help index. There is also a facility to <u>Search</u> index headings.
Search. . .	Search the Help topics for keywords.
License. . .	Displays information about your license.
Check for Updates. . .	Prompts you to save your work, checks for new versions of <i>Mechanical Expressions</i> , then restarts the program.
About. . .	Contains the current version of the program, the copyright notice, and the link to <i>Mechanical Expressions</i> ' website.

NOTE: For the Mac version, **About...** is listed under ***Mechanical Expressions*** menu.

Context Menus

Context Menus pop up when you right-click with the cursor positioned anywhere in the drawing window.

- The [general context menu](#) - appears when you right click and nothing is selected.
- The [selection context menu](#) - appears when one or more elements in the drawing window are selected. Some menu entries may be inactive, depending on which elements are selected.

The General Context Menu

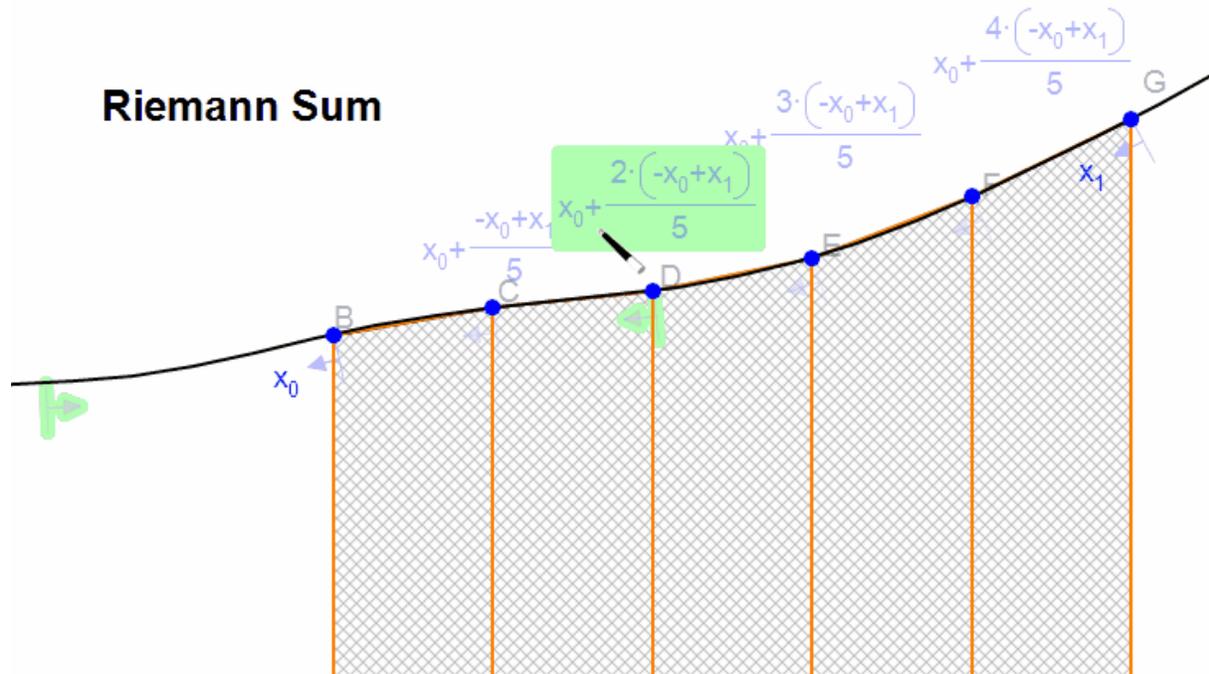
Right-click anywhere in the drawing window to display a context menu. If nothing in the window is selected, the menu choices are the following:

Menu Option	Function	When Available
Close	Closes the current file	Always

Save	Updates a file that already exists	The file has been saved
Save As. . .	Saves a file for the first time and prompt for the filename and path	Always
Select All	Selects everything in the drawing window	Always
Select All Type	Presents a submenu of object types to select.	Always -- most useful when the object type is in the window.
 Copy Drawing	Copies everything in the drawing window as an Enhanced Metafile (.emf)	Always
 Copy Region	Copies a section of the drawing window inside a rectangle made by dragging the cursor.	Always
 Paste	Puts whatever has been cut or copied into the current document	Object(s) cut or copied
Show All	Displays any entities that were hidden	One or more element (s) are hidden
 Toggle Hidden	Lets you toggle hidden / visible for any object in the drawing	Always
 Stop Calculations	Stop current calculations	A calculation isn't finished
 Start Calculations	Restart any stopped calculations	A calculation is stopped by user
Display Properties	Allows you to change the Grid and Background Display Properties	Always

Toggling - Hide / Show Elements

From the general context menu select **Toggle Hidden**. The magic wand cursor appears, and any hidden objects appear faintly in the drawing window.



Click faint items to display them. Click any displayed items to hide them. When you are finished toggling, click the select arrow .

Selection Context Menu

Select one or more model elements and right-click anywhere in the drawing window to display a context menu. Selection context menus contain some subset of the following list.

Menu Option	Function	When Available
-------------	----------	----------------

 Cut	Deletes an object, but saves it so it can be pasted somewhere else	One or more objects selected
 Copy	Does not delete the object, but saves it so it can be pasted somewhere else	One or more objects selected
Copy As	Displays a submenu of choices for copying mathematics into other programs	An expression or formula is selected
Send to <i>Mathematica</i>	Inputs the selected expression to <i>Mathematica</i> when the algebra system is running in another window	An output expression or formula is selected
 Paste	Puts whatever has been cut or copied into the current document	Object(s) cut or copied
Delete	Deletes whatever is selected, without saving it.	One or more objects selected
Hide	Makes the selected objects invisible	One or more objects selected
Edit Parameters...	Lets you edit the domain of a polar or parametric function or the parameters of a locus or trace.	A function, locus, or trace is selected
Arrange	For placing selected objects on top of (bring forward) or underneath (send backward) other objects for easier selection and viewing	One or more objects selected
Constrain (Input)	Displays a submenu identical to the one in the same drop-down menu on the Menu Bar	Geometry selected
Free Constraint to Accelerate	Frees constraint to create a dynamic model	An input constraint is

		selected
Construct	Displays a submenu identical to the one in the same drop-down menu on the Menu Bar	Geometry selected
Calculate (Output)	Displays a submenu identical to the one in the same drop-down menu on the Menu Bar	Geometry selected
Visibility Condition	Lets you enter an equation specifying when the selected object(s) are visible.	One or more objects selected
Point Properties	Lets you change the selected point's color and size	One or more points selected
Arrow Head	Lets you turn off or change the arrow head style of the selected segment(s)	One or more segments selected
Line Properties	Lets you change the selected line's color, style, and thickness	One or more objects created with lines or segments
Fill Properties	Lets you change the color, style, and transparency level of the selected object(s)	Polygon, N-gon, filled circle, filled ellipse, picture or trace selected
Pinned	Lets you pin / unpin the selected object(s)	Text, picture, or expression selected
Text Properties	Lets you change the selected text's color, size, and style	Text, label, expression, constraint, or measurement selected
Show Symbol	A toggle to display or hide the selected object(s)	Constraints, annotations, or measurement

		lines selected
Output Properties	Lets you turn on or off the selected output's name, assumption or intermediate variables	One or more outputs selected
Show Arrowheads	Lets you turn on or off the selected angle symbol's arrowheads	One or more angle symbols selected
Congruence Style	Lets you change the angle style from arcs to tics and vice versa	One or more angle or congruent angle annotations selected
Tic / Arc Count	Lets you change the number of tic/arc counts of selected annotations	One or more congruent, congruent angle, or parallel annotations selected
Axes Properties	Lets you turn the labels on the axes on/off or change the number of subdivisions or units to display	One or both axes selected
All Properties. . .	Lets you edit the display properties of the selected object(s)	One or several similar objects are selected
[Convert to Calculation (Output)]	Deletes the selected constraint and calculates the equivalent output	A constraint is selected
[Convert to Constraint (Input)]	Changes the calculation to an input constraint	An output expression is selected
[Convert to Real]	Changes a symbolic output to a real output value	A symbolic output expression is selected

[Convert to Symbolic]

Changes a real output value to a symbolic output expression

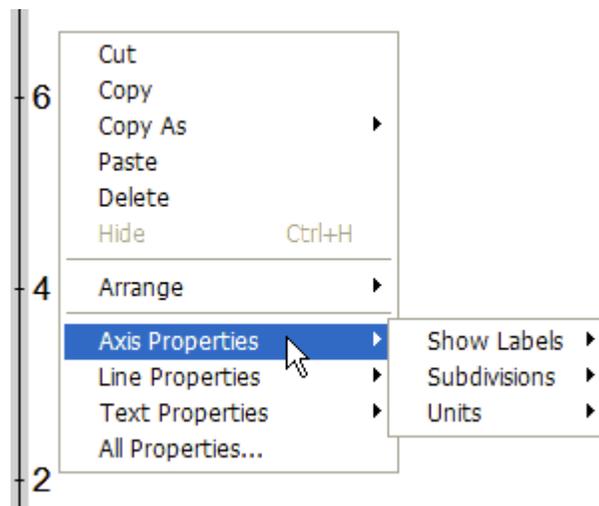
A real output value is selected

Axes Display Properties

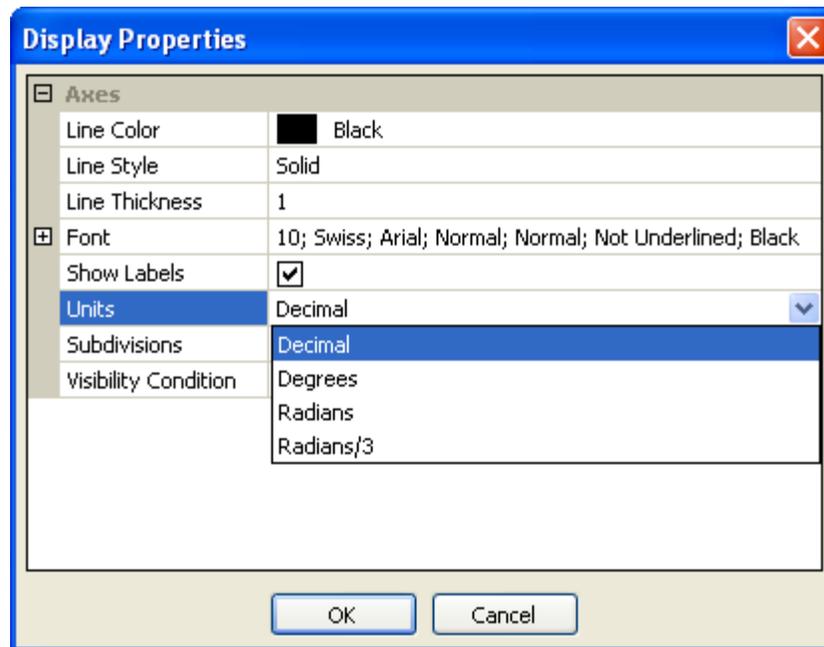
The Axes Display can be set in the default settings, [Edit / Preferences](#) under the **Grid, Axis, Page** tab, or you can change them for an individual drawing from the [Selection Context menu](#).

To invoke the **Selection Context** menu:

1. Select one or both axes
2. Right click the mouse



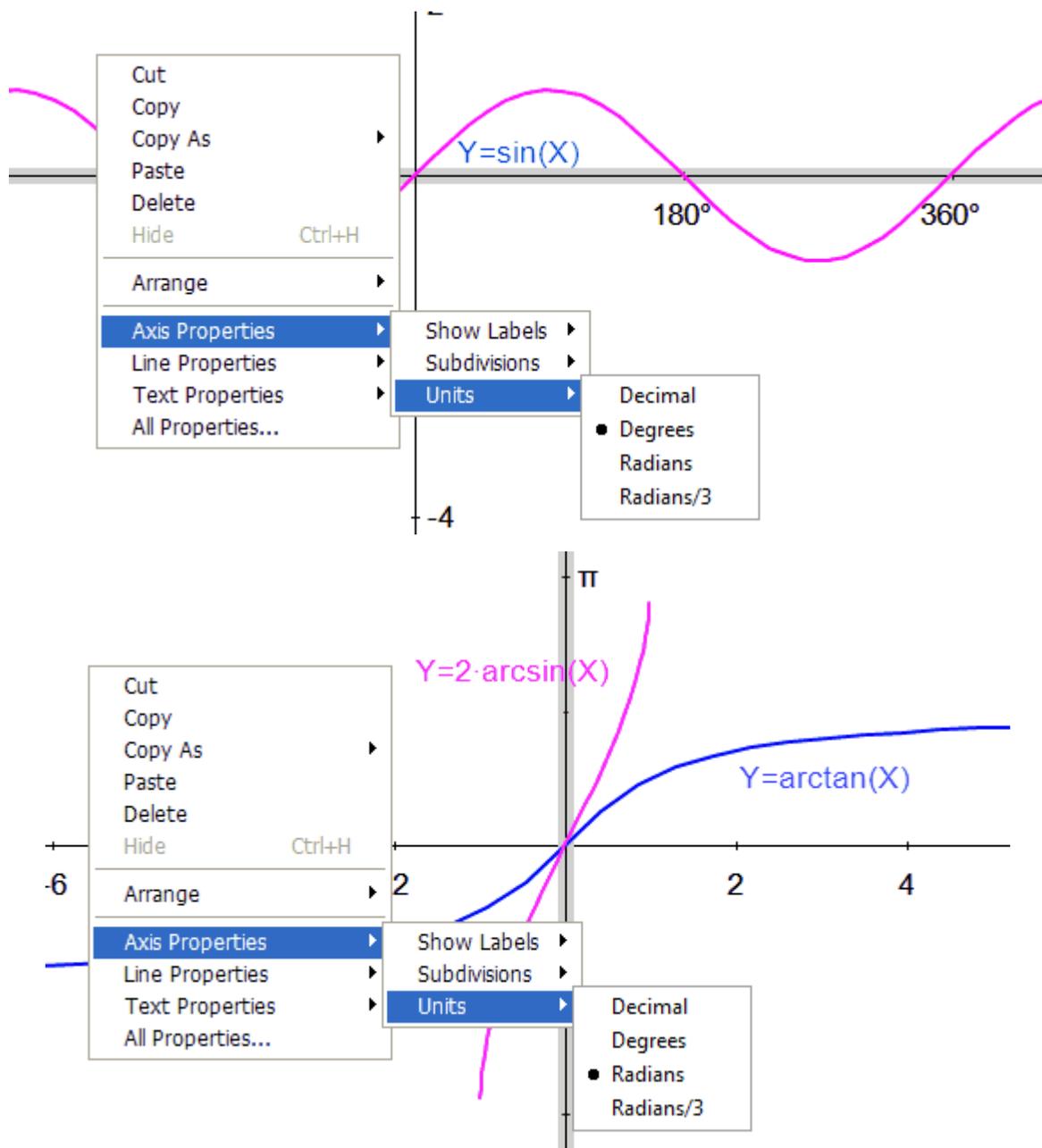
The **All Properties** selection brings up all the **Display Properties** dialog for the axes.



You can configure the X and Y axes in many ways. There are the usual attributes of lines and text.

Show Labels - is useful when the axis labels lie under some part of your diagram making it hard to read. You can turn these off on one or both axes with the attribute set to False.

Units - can be set to the usual decimal, but with trig functions you may find the Degrees, Radians or Radians/3 units more appropriate.  If you use the Degrees or Radians units in trig functions, don't forget to set your Angle Mode to **Radians** on the status bar.



Visibility Condition

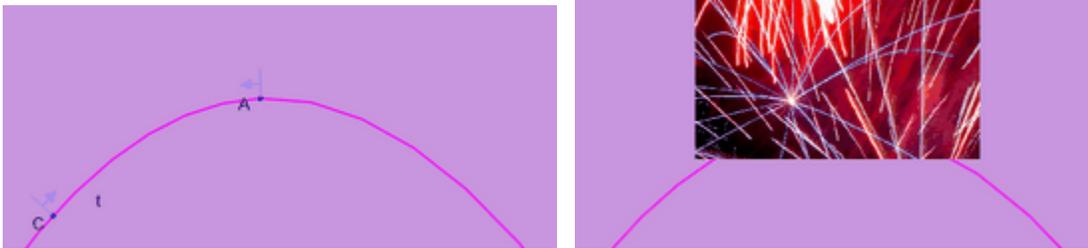
You can set any mathematical condition for one or more object's visibility. Use this with the Animation tools for some great effects. Here are the steps:

1. Select the object(s) that you want to change visibility.
2. Right-click and select **Visibility Condition** from the **Selection**

Context menu.

3. Enter the expression for a defined variable for which you would like your object(s) to be visible.

Here's an example. Point C is t proportional along the parabola. In the first figure the picture is hidden. When the picture was visible, we set the it's **Visibility Condition** to: $|t| \geq 0 \text{ AND } |t| < .3$. With the [Animation](#) tools we set t from -1.5 to 1.5. As point C approaches the top of the arc, BOOM!



Tool Bar

The icons across the top of the screen make some of the routine tasks in the **File**, **Edit**, and **View** menus, and **Help** easily accessible.



- See **The Selection Arrow** for more information.



- See **File Menu** for more information.



- See Edit Menu for more information.



- See View Menu for more information.



- See **Output Calculations** for more information.



[Invokes the embedded Help facility](#)



More About Mechanical Expressions

Where is the Mechanical Expressions Website?

Information on purchases and additional technical support can be found on the *Mechanical Expressions* website at: www.MechanicalExpressions.com.

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