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Supercomputing Engine for Mathematica

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Introduction

Parallel Computing

Parallel computation occurs when multiple processing units are working at the same time. This general concept is divided into several categories.

Categories of parallel computing

Type of Parallel Computing	Characteristic architecture	Communication pattern	Possible applications
Independent computing	Many processing machines operating without interaction	No communication	single-processor problems
Distributed computing	One or a few centralized servers directing many slave machines	Master-slave	above plus brute-force problem space sampling
Cluster computing & supercomputing	Interdependent computing nodes coordinating work and data	Peer-to-peer and collective	above plus large problems with strong interdependence

The capabilities of each category of parallel computing build on those of the one before. Many personal computers being used in an office are implementing the independent computing category. Grid computing today typically implements a distributed computing model. Famous examples include SETI@home, Folding@home, and brute force RSA key breaking, where many client machines receive instructions from a central server or servers and report to that server whether they found the answer.

In the 1980s, scientists developed techniques to solve the largest, most complex problems they could conceive using parallel computing. Through much work, development, and trial and error, they also found that communication between different computing processors was required to address such problems. In 1994, the Message-Passing Interface (MPI) standard was established as a supercomputing platform-independent programming interface that could enable any complex problem to be performed on a parallel computer. Today, usage of MPI has since grown so that MPI has become the de-facto supported standard in clusters and supercomputers of all types, while almost all known problem types have been parallelized using MPI.

Pooch, MPI, and Mathematica

Mathematica was created as an advanced calculation tool for scientists. Our idea was to combine this tool with the easy-to-use cluster computing solution embodied by Pooch and MacMPI to enable supercomputing-like behavior and computations within Mathematica. This solution would enable Mathematica kernels, which normally operate as single-processor codes to be harnessed together the way supercomputers are, expanding their scope well beyond what any one of these technologies could accomplish alone.

Setting Up

Setting Up the Supercomputing Engine and mathpooch

The mathpooch executable provides the infrastructure and API of the Supercomputing Engine for Mathematica (SEM) after acquiring nodes of the cluster via Pooch. Setting up SEM and mathpooch is very simple. Simply copy the mathpooch executable to a convenient, and writable, location on your hard drive. Pooch and mathpooch write temporary files to that directory in the course of normal operation.

Running Multiple Mathematica Kernels

The SEM system runs and uses multiple Mathematica Kernels at once. Wolfram Research requires that each kernel have a valid license. The default single-user license allows one extra kernel to run on the same machine. Additional kernels are allowed using their MathLM technology. Wolfram Research provides license and pricing agreements for these technologies, so they should be consulted for such issues.

As far as Mathematica is concerned, it appears that many different users are each using their own a Mathematica kernel, when, in fact, the SEM system is using these kernels collectively as one system. Therefore, no further configuration of the Mathematica kernels are needed.

Installing Pooch

Pooch is very easy to install. Just double-click the Pooch Installer on each node where Mathematica can be run. For command-line installation, use the `poochclinstaller.tar.gz` tar ball. More information at: <http://daugerresearch.com/pooch/>

Using Mathematica's Front End with SEM

The SEM system can intercept commands from Mathematica's Front End and direct them to the cluster of kernels under its control as well as display results back in the original Front End. To do so, one must configure the Front End to think that mathpooch is a Mathematica kernel.

1. Select the Kernel > Kernel Configuration Options... and click Add... in the dialog.
2. Enter a name for this configuration, such as "mathpooch", and select the Advanced Options tab.
3. Replace the "Arguments to MLOpen:" field.
 - If you are using a single-user license, or for debugging or developing code, use: `-LinkMode Launch -LinkName ""/Your/path/to/mathpooch' -n 1 -m 2 -l 1"`
 - If you are using MathLM or other means of managing Mathematica licenses on a network, you have an upper limit, N, on how many licenses you may use at once. Substitute that number into the following string and use it in in this kernel configuration: `-LinkMode Launch -LinkName ""/Your/path/to/mathpooch' -n N -l 1"`

4. Click Okay to dismiss this dialog and again Okay for the next.
5. Select this new configuration from the Kernel > Default Kernel submenu.

This also makes it possible to create multiple Kernel configurations with different settings for number of nodes or number of tasks per node.

Launching Directly via Pooch

1. Locate your mathpooch executable and drag it to the Pooch icon (e.g., in the Dock)
2. Click “Select Nodes...” in the Job window that opens to open the Network Scan window and select nodes that you know have Mathematica properly installed
3. Click Launch Job

Note: It is recommended that you enable “Launch Unix Jobs using Terminal.app” under Pooch’s General preferences so that you can interact with the job.

Launching from a Command-Line

1. cd to the directory where mathpooch is (one where files are writable)
2. use “./mathpooch -n N” to launch on N nodes. It should be using Pooch to access the cluster and launch itself in parallel.

Launching from Mathematica’s Front End

With the Front End set with a Kernel configuration as described above, merely enter your first expression. mathpooch will take a moment to access the cluster and launch itself via Pooch, then determine which nodes have Mathematica installed and launch the corresponding kernels.

Ending the Supercomputing Engine for Mathematica Session

At the command-line, typing Quit should be sufficient to have the parallel execution end and release cluster and kernel resources. From the Front End, choosing Quit from the File menu should have the same effect. The release has a built-in three second wait for the processes to come into sync.

If there is a problem releasing these resources, e.g., if a busy cluster is interfering with a new SEM session, you can kill it via Pooch. Using the Network Scan window, click the Job view, and it should show a running job named “mathpooch”. Select this job and click Kill Job. After several seconds, Pooch should ask the other nodes to kill the job, which should in turn end the Mathematica kernels. Alternatively, one could select each BUSY node in the Node view and select Get Node Info, then locate and kill each stray process there.

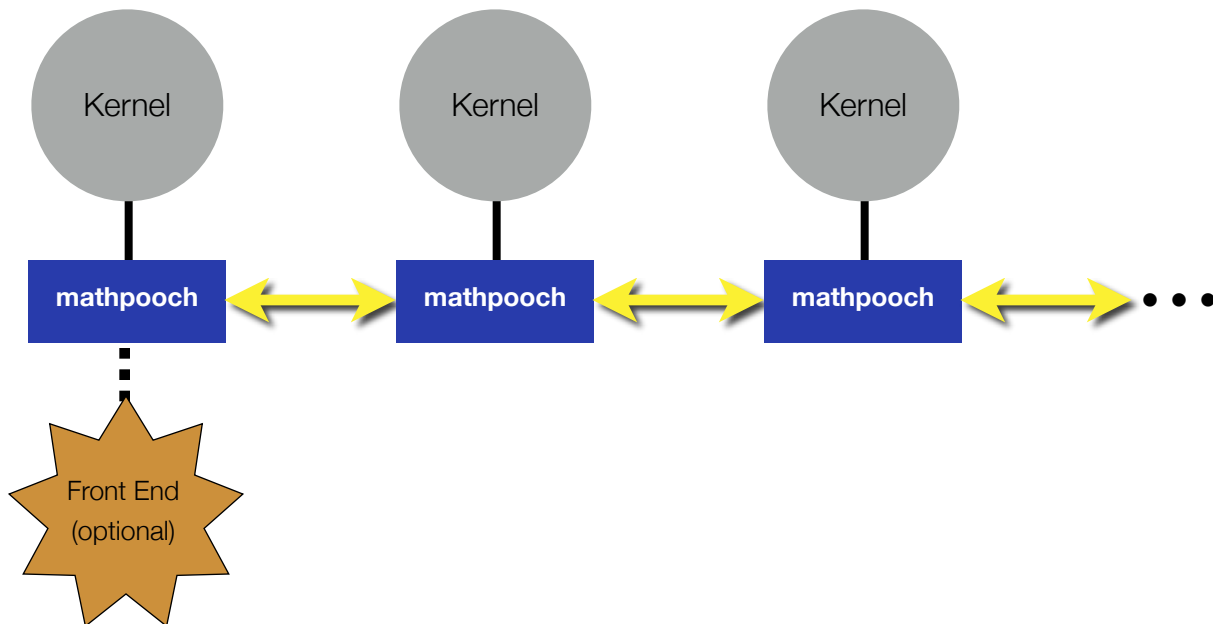
Using MPI in Mathematica

Using MPI

As discussed in the Introduction, Message-Passing Interface (MPI) is the standard language for sending messages between nodes on a cluster. We have created a simplified version of MPI that you can call from Mathematica in a way compatible with its language while offering the power of supercomputing with MPI. Even so, it is not required to use MPI explicitly, but use the higher-level calls that build on MPI.

The parallel computing model used for MPI combines a distributed memory model with support for passing messages between any processor subset. A major advantage of the distributed-memory model over shared-memory models is that there is no way for a processor to manipulate the memory accessed by another unless it explicitly makes an MPI call. This makes debugging and repeatability of parallel codes much easier and more reliable, besides making the hardware design easier to scale.

We have adapted this computing model to Mathematica. Mathematica has two basic parts: a Kernel and a Front End. The user “sees” only the Front End, while the Kernel performs the computations and manages the data. Our adaptation of the technology is diagrammed below.



Organizational diagram of Supercomputing Engine for Mathematica. In actuality, communications between mathpooch can be all-to-all, not just to the nearest neighbors.

Commands are sent from the Front End (or other user interface) to all the Kernels via mathpooch. Results of evaluations by the kernel are returned locally, that is, only the local kernel “speaks” directly back to the Front End. Some of these evaluations could be calls to MPI to direct expressions to be sent from one kernel to others.

Examples

Often the best way to see how a system works is to see examples. We explore some of its basic operations here.

Basic MPI

Fundamental data available to each node is its identification number and total processor count.

```
In[1]:= {$IdProc, $NProc}
Out[1]:= {0, 2}
```

The first element should be unique for each processor, while the second is same for all. Processor 0 can see what other values are using a collective (see below) communications call such as `mpiGather[]`.

```
In[2]:= mpiGather[{$IdProc, $NProc},list,0]; list
Out[2]:= {{0, 2}, {1, 2}}
```

Peer-to-Peer MPI

`mpiSend` and `mpiRecv` make possible basic message passing, but one needs to define which processor to target. The following defines a new variable, `targetProc`, so that each pair of processors will point to each other.

```
In[3]:= targetProc=If[1==Mod[$IdProc, 2],$IdProc-1,$IdProc+1]
Out[3]:= 1
```

The even processors target its “right” processor, while the odd ones point its “left”. Then we can send a message:

```
In[4]:= If[1==Mod[$IdProc, 2],mpiSend[N[Pi,22],targetProc,
    mpiCommWorld,d], mpiRecv[a,targetProc,mpiCommWorld,d]]
```

The `If[]` causes the processors to evaluate different code: the odd processor sends 22 digits of Pi, while the even receives that message. Note that these MPI calls return nothing. The received message is in `a`:

```
In[5]:= a
Out[5]:= 3.1415926535897932384626
In[6]:= Clear[a]
```

yet `a` on the odd processors would have no definition. Also consider that, if `$NProc` is 8, processor 3 sent Pi to processor 2, processor 5 sent Pi to processor 4, and so on. These messages were not sent through processor 0, but they communicated on their own.

`mpiSend` and `mpiRecv` have a letter “l” to indicate asynchronous behavior, making it possible to do other work while messages are being sent and received, or if the other processor is busy. So, the above example could be done asynchronously:

```
In[7]:= If[1==Mod[$IdProc, 2],mpiISend[N[Pi,22],targetProc,
    mpiCommWorld,d,e], mpiIRecv[a,targetProc,mpiCommWorld,d,e]]
```

`e` has important data identifying the message, and `mpiTest[e]` must return `True` before the expressions are to be accessed. At this point, many other evaluations can be performed. Then, check using `mpiTest` when you might need the data:

```
In[29]:= mpiTest[e]
Out[29]:= True
In[30]:= a
Out[30]:= 3.1415926535897932384626
```

```
In[31]:= Clear[a,e]
```

We could have also used `mpiWait[e]`, which does not return until `mpiTest[e]` returns True. The power of using these peer-to-peer calls is that it becomes possible to construct any message-passing pattern for any problem.

Collective MPI

In some cases, such explicit control is not required and a commonly used communication pattern is sufficient. Suppose processor 0 has an expression in `b` that all processors are meant to have? A broadcast MPI call would do:

```
In[8]:= mpiBcast[b, 0, mpiCommWorld]
```

The second argument specifies which processor is the “root” of this broadcast; all others have their `b` overwritten. To collect values from all processors, use `mpiGather[]`:

```
In[9]:= mpiGather[b, c, 0, mpiCommWorld]
```

`c` of processor 0 is written with a list of all the `b` of all the processors in `mpiCommWorld`. The temporal opposite is `mpiScatter[]`:

```
In[10]:= Clear[b]; a = {2, 4, 5, 6}; mpiScatter[a, b, 0, mpiCommWorld];
b
Out[10]:= {2, 4}
```

`mpiScatter` cuts up `a` into even pieces (when possible) and scatters them to the processors. This is the result if `$NProc = 2`, but, if `$NProc = 4`, `b` would only have {2}.

MPI provides reduction operations to perform simple computations mixed with messaging. Consider the following:

```
In[11]:= a = {{2 + $IdProc, 45}, 3, {1 + $IdProc, $NProc}}; mpiReduce
[a, d, mpiSum, 0, mpiCommWorld]
In[12]:= d
Out[12]:= {{5, 90}, 6, {3, 4}}
```

The `mpiSum` constant indicates that `a` of every processor will be summed. In this case, `$NProc` is 2, so those elements that were not identical result in odd sums, while those that were the same are even.

Most of these calls have default values if not all are specified. For example each of the following calls will have the equivalent effect as the above `mpiGather[]` call:

```
mpiGather[b, c, 0]
mpiGather[b, c]
c = mpiGather[b]
```

High-Level SEM Calls

Many of these calls are convenient parallel versions of commonly used Mathematica calls. For example, `ParallelTable[]` is like `Table[]`, except that the evaluations are automatically performed in a distributed manner:

```
In[13]:= ParallelTable[i, {i, 100}, 0]
Out[13]:= {1, 2, 3, 4, 5, ..., 99, 100}
```

while the third argument specifies that the answers are collated back to processor 0. This is a useful, simple way to parallelize many calls to a complex function. One could define a complicated function and evaluate it over a large range of inputs:

```
In[14]:= g[x_] := Gamma[2 + 0.5*(x-1)]; ParallelTable[g[i], {i, 100}, 0]
Out[14]:= {1, 1.32934, 2., 3.32335, 6., 11.6317, 24., 52.3428, 120.,
287.885, 720., ... }
```

`ParallelFunctionToList[]` also provides a simplified way to perform this form of parallelism.

Operations with Non-Trivial Communication

Matrix Operations

Other functions can help solve matrix calculations in parallel:

```
In[15]:= a = Table[i+ 3* $IdProc + 2 j, {i, 2}, {j,4}]
Out[15]:= {{3, 5, 7, 9}, {4, 6, 8, 10}}
In[16]:= t = ParallelTranspose[a]
Out[16]:= {{3, 4, 6, 7}, {5, 6, 8, 9}}
```

Fourier Transforms

A Fourier transform of a large array can be solved faster in parallel, or made possible on a cluster because it can all be held in memory. A two-dimensional Fourier transform of the above example:

```
In[17]:= f = ParallelFourier[a]
Out[17]:= {{32. + 0. I, -4. - 4. I, -4., -4. + 4. I}, {-3. - 3. I, 0. +
0. I, 0., 0. + 0. I}}
```

Edge Cell Management

Many problems require interactions between partitions, but only on the edge elements. Maintaining these edges can be performed using EdgeCell[].

```
In[18]:= a = {2, 4, 5, 6, 7}+8*$IdProc
Out[18]:= {2, 4, 5, 6, 7}
In[19]:= EdgeCell[a]; a
Out[19]:= {14, 4, 5, 6, 12}
```

Element Management

In particle-based problems, these items can drift through space, sometimes outside the partition of a particular processor. This can be solved with ElementManage[]:

```
In[20]:= list={{0,4},{1,3},{1,4},{0,5}}; fcn[x_]:=x[[1]]
In[21]:= ElementManage[list, fcn]
Out[21]:= {{0, 4}, {0, 5}, {0, 4}, {0, 5}}
In[21]:= ElementManage[list, 2]
Out[21]:= {{0, 4}, {0, 5}, {0, 4}, {0, 5}}
```

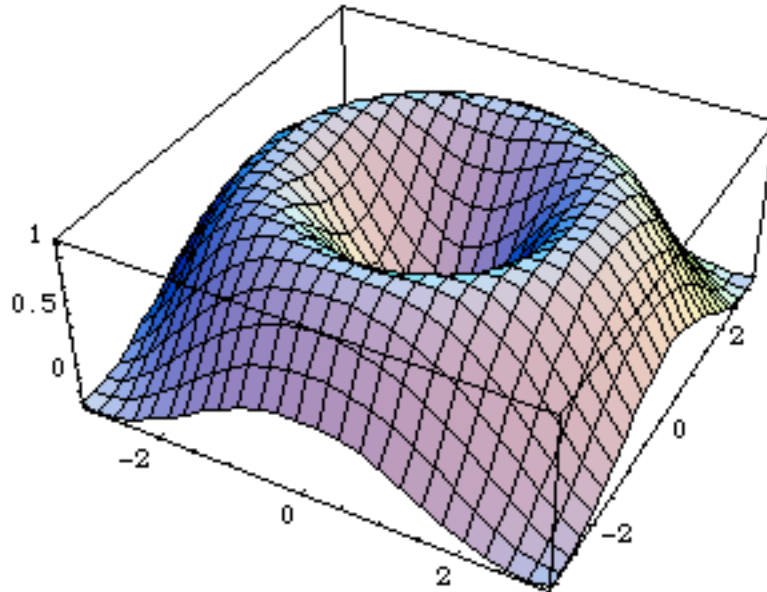
The second argument of ElementManage describes how to test elements of list. fcn returns which processor is the “home” of that element. Passing an integer assumes that each elements is itself a list, whose first element is a number ranging from 0 to the passed argument.

Graphics and Parallelism

Displayed in the Front End, graphics can definitely be combined with parallelism. Frames of an animation can be computed in parallel and displayed on the Front End. For example, the following loads the Animation package, computes a series of 3D Plots, then shows the animation:

```
<< Graphics`Animation`
b = ParallelTable[Plot3D[Module[{r}, r = 2*Sqrt[x^2 + y^2] - (i); Sin
[r]/r], {x, -Pi, Pi}, {y, -Pi, Pi}], {i, 8},0]
ShowAnimation[b]
```

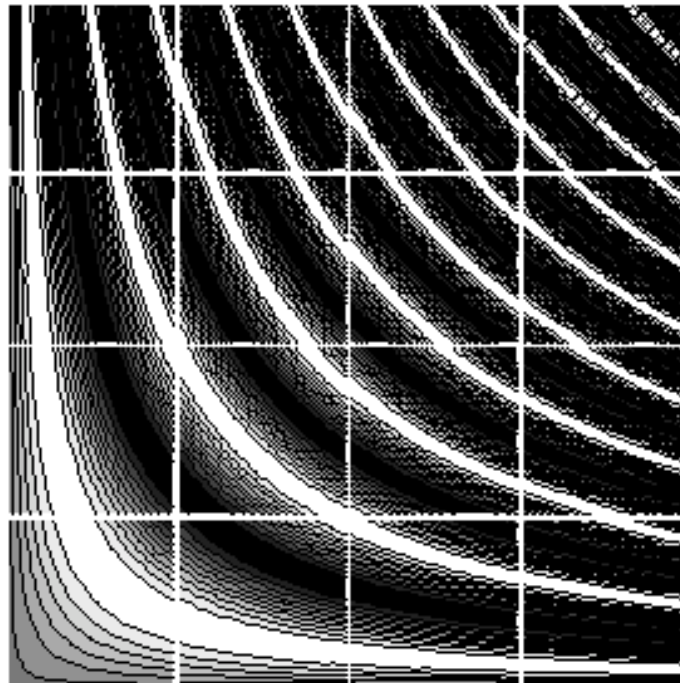
That produces frames like:



Suppose one wanted a contour plot of a large data set, spread over the cluster because it cannot be held on one node, but we know the graphics could be because it is much smaller than the original data set. In this example, we define each subgraphic with `c[]`, calculate and collect them with `ParallelTable`, then plot using `GraphicsArray[]`.

```
c[i_] := Module[{cx,cy}, cx=Mod[i,4]*2; cy=IntegerPart[i/4]*2;  
  ContourPlot[Sin[x y], {x, cx, cx+2}, {y, cy, cy+2}, Frame -> False]]  
c = ParallelTable[c[i-1], {i, 16}, 0]  
Show[GraphicsArray[Reverse[Partition[c, 4]],GraphicsSpacing->0]]
```

The result would look like:



Function List

Calling the Supercomputing Engine for Mathematica

The SEM calls are divided into two general categories. The first category includes the basic MPI calls that closely follow those that are used in supercomputers. Typically, the behavior of the routine with the prefix “mpi” corresponds with the routine with the prefix “MPI_” in the standard MPI references. The second category are higher-level calls, which are built on the MPI calls, that perform commonly used tasks or communication patterns.

MPI Constants

To send messages to nodes or receive messages from them, we need a way of identifying which is which. In MPI, this is accomplished by assigning each a unique integer (\$IdProc) starting with 0. This data, with a knowledge of the total count (\$NProc), makes it possible to programmatically divide any measurable entity.

Constant	Description
\$IdProc	The identification number of the current processor
\$NProc	The number of processors in the current cluster
\$mpiCommWorld	The communicator world of the entire cluster (see MPI Communicator routines, below)
mpiCommWorld	The default communicator world for the high-level routines.

Basic MPI Calls

Simply sending expressions from one node to another is possible with these most basic MPI calls. One node must call to send an expression while the other calls a corresponding routine to receive the sent expression. Because it is possible that the receiver has not yet called mpiRecv even if the message has left the sending node, completion of mpiSend is not a confirmation that it has been received.

Call	Description
mpiSend[expr, target, tag, comm]	Sends an expression expr to a node with the ID target in the communicator world comm, waiting until that expression has left this kernel
mpiRecv [expr, target, tag, comm]	Receives an expression into expr from a node with the ID target in the communicator world comm, waiting until the expression has arrived
mpiSendRecv[sendexpr, dest, recvexpr, source, comm]	Simultaneously sends the expression sendexpr to the node with the ID target and receives an expression into recvexpr from the node with the ID source in the communicator world comm, waiting until both operations have returned.

Asynchronous MPI Calls

Asynchronous calls make it possible for the kernel to do work while communications is proceeding simultaneously. It is also possible that another node may not be able to send or receive data yet, allowing one kernel to continue working while waiting.

Call	Description
mpiSend[expr, target, tag, comm, req]	Sends an expression expr to a processor with the ID target in the communicator world comm, returning immediately. It must be balanced with calls to mpiTest[req] until mpiTest[req] returns True.
mpiRecv[expr, target, tag, comm, req]	Receives an expression expr from a processor with the ID target in the communicator world comm, returning immediately. It must be balanced with calls to mpiTest[req] until mpiTest[req] returns True. Very important: expr is not safe to access until mpiTest[req] returns True.
mpiTest[req]	Completes asynchronous behavior of mpiSend and mpiRecv
mpiWait[req]	Calls mpiTest until it returns True.
mpiWaitall[reqlist]	Calls mpiWait all on every element of reqlist
mpiWaitany[reqlist]	Calls mpiTest on each element of reqlist until one of them returns True

Collective MPI Calls

Collective calls provide commonly mechanisms to send expressions between groups of nodes.

Call	Description
mpiBcast[expr, root, comm]	Performs a broadcast of expr from the root processor to all the others in the communicator world comm. An expression is expected to be supplied by the root processor, while all the others expect expr to be overwritten by the incoming expression.
mpiGather[sendexpr, recvexpr, root, comm]	All processors (including root) in the communicator comm send their expression in sendexpr to the root processor, which produces a list of these expressions, in the order according to comm, in recvexpr. On the processors that are not root, recvexpr is ignored.
mpiAllgather[sendexpr, recvexpr, comm]	All processors in the communicator comm send their expression in sendexpr, which are organized into a list of these expressions, in the order according to comm, in recvexpr on all processors in comm.
mpiScatter[sendexpr, recvexpr, root, comm]	Processor root partitions the list in sendexpr into equal parts (if possible) and places each piece in recvexpr on all the processors (including root) in the communicator world comm, according the order and size of comm.
mpiAlltoall[sendexpr, recvexpr, comm]	Each processor sends equal parts of the list in sendexpr to all other processors in the communicator world comm, which each collects from all other processors are organizes into the order according to comm.

Additional collective calls perform operations that reduce the data in parallel. The operation argument can be one of the constants below.

Call	Description
mpiReduce[sendexpr, rcvexpr, operation, root, comm]	Performs a collective reduction operation between expressions on all processors in the communicator world comm for every element in the list in sendexpr returning the resulting list in rcvexpr on the processor with the ID root.
mpiAllreduce[sendexpr, rcvexpr, operation, comm]	Performs a collective reduction operation between expressions on all processors in the communicator world comm for every element in the list in sendexpr returning the resulting list in rcvexpr on every processor.
mpiReduceScatter[sendexpr, rcvexpr, operation, comm]	Performs a collective reduction operation between expressions on all processors in the communicator world comm for every element in the list in sendexpr, partitioning the resulting list into pieces for each processor's rcvexpr.

Constant	Description
mpiSum	Specifies that all the elements on different processors be added together in a reduction call
mpiMax	Specifies that the maximum of all the elements on different processors be chosen in a reduction call
mpiMin	Specifies that the minimum of all the elements on different processors be chosen in a reduction call

MPI Communicator Calls

Communicators organizes groups of nodes into user-defined subsets. The communicator values returned by mpiCommSplit[] can be used in other MPI calls instead of mpiCommWorld.

Call	Description
mpiCommSize[comm]	Returns the number of processors within the communicator comm
mpiCommRank[comm]	Returns the rank of this processor in the communicator comm
mpiCommDup[comm]	Returns a duplicate communicator of the communicator comm
mpiCommSplit[comm, color, key]	Creates a new communicator into several disjoint subsets each identified by color. The sort order within each subset is first by key, second according to the ordering in the previous communicator. Processors not meant to participate in any new communicator indicates this by passing the constant mpiUndefined. The corresponding communicator is returned to each calling processor.
mpiCommMap[comm] mpiCommMap[comm, target]	Returns the mapping of the communicator comm to the processor indexed according to \$mpiCommWorld. Adding a second argument returns just the ID of the processor with the ID target in the communicator comm.

Call	Description
mpiCommFree[comm]	Frees the communicator comm

Other MPI Support Calls

Other calls that provide other common functions.

Call	Description
mpiWtime[]	Provides wall-clock time since some fixed time in the past. There is no guarantee that this time will read the same on all processors.
mpiWtick[]	Returns the time resolution of mpiWtime[]
MaxByElement[in]	For every nth element of each list of the list in, chooses the maximum according to Max[], and returns the result as one list. Used in the mpiMax reduction operation.
MinByElement[in]	For every nth element of each list of the list in, chooses the minimum according to Min[], and returns the result as one list. Used in the mpiMin reduction operation.

High-Level SEM Calls

Built on the MPI calls, below are calls that provide commonly used communication patterns or parallel versions of Mathematica features. Unless otherwise specified, these are executed in the communicator mpiCommWorld, whose default is \$mpiCommWorld, but can be changed to a valid communicator at run time.

Common Divide-and-Conquer Parallel Evaluation

The following calls address simple parallelization of common tasks.

Call	Description
ParallelDo[expr, loopspec]	Like Do[] except that it evaluates expr across the cluster, rather than on just one processor. The rules for how expr is evaluated is specified in loopspec, like in Do[].
ParallelFunctionToList[f, count] ParallelFunctionToList[f, count, root]	Evaluates the function f[] from 1 to count, but across the cluster, and returns these results in a list. The third argument has it gather this list into the processor whose ID is root.
ParallelTable[expr, loopspec] ParallelTable[expr, loopspec, root]	Like Table[] except that it evaluates expr across the cluster, rather than on just one processor, returning the locally evaluated portion. The third argument has it gather this table in to the processor whose ID is root.
ParallelFunction[f, inputs, root]	Like f[inputs] except that it evaluates f on a subset of inputs scattered across the cluster from processor root and gathered back to root.

Call	Description
ParallelNIntegrate[expr, loopspec]	Like NIntegrate[] except that it evaluates a numerical integration of expr over domains partitioned into the number of processors in the cluster, then returns the sum. The third argument has each numerical integration execute with at least that many digits of precision.
ParallelNIntegrate[expr, loopspec, digits]	

Guard-Cell Management

Typically the space of a problem is divided into partitions. Often, however, neighboring edges of each partition must interact, so a “guard cell” is inserted on both edges as a substitute for the neighboring data. Thus the space a processor sees is two elements wider than the actual space for which the processor is responsible. EdgeCell helps maintain these guard cells.

Call	Description
EdgeCell[list]	Copies the second element of list to the last element of the left processor and the second-to-last element of list to the first element of the right processor while simultaneously receiving the same from its neighbors.

Matrix and Vector Manipulation

Matrices are partitioned and stored in processors across the cluster. These calls manipulate these matrices in common ways.

Call	Description
ParallelTranspose[matrix]	Like Transpose[] except that it transposes matrix that is in fact represented across the cluster, rather than on just one processor. It returns the portion of the transposed matrix meant for that processor.
ParallelProduct[matrix, vector]	Evaluates the product of matrix and vector, as it would on one processor, except that matrix is represented across the cluster.
ParallelDimensions[matrix]	Like Dimensions[] except that matrix is represented across the cluster, rather than on just one processor. It returns a list of each dimension.
ParallelTr[matrix]	Like Tr[] except that the matrix is represented across the cluster, rather than on just one processor. It returns the trace of this matrix.
ParallelIdentity[rank]	Like Identity[], it generates a new identity matrix, except that the matrix is represented across the cluster, rather than on just one processor. It returns the portion of the new matrix for this processor.
ParallelOuter[f, vector1, vector2]	Like Outer[f, vector1, vector2] except that the answer becomes a matrix represented across the cluster, rather than on just one processor. It returns the portion of the new matrix for this processor.
ParallelInverse[matrix]	Like Inverse[] except that the matrix is represented across the cluster, rather than on just one processor. It returns the inverse of the matrix.

Element Management

Besides the obvious divide-and-conquer approach, a list of elements can also be partitioned in arbitrary ways. This is useful if elements need to be organized or sorted onto multiple processors. For example particles of a system may drift out of the space of one processor into another, so their data would need to be redistributed periodically.

Call	Description
ElementManage[list, switch]	Selects which elements of list will be sent to which processors according to the function switch[] is evaluated on each element of list. If switch is a function, switch[] should return the ID of the processor that element should be sent. If switch is an integer, the call assumes that each elements is itself a list, whose first element is a number ranging from 0 to the passed argument. This call returns a list of the elements, from any processor, that is switch selected for this processor.
ElementManage[list]	Each element of list must be a list of two elements, the first being the ID of the processor where the element should be sent, while the second is arbitrary data to send. This call returns those list elements, from any and all processors, whose first element is this processors ID in a list. This call is used internally by the two-argument version of ElementManage[].

Fourier Transform

Fourier transforms of very large arrays can be difficult to manage, not the least of which is the memory requirements. Parallelizing the Fourier transform makes it possible to make use of all the memory available on the entire cluster, making it possible to manipulate problem sizes that no one processor could possibly do alone.

Call	Description
ParallelFourier[list]	Like Fourier[] except that list is a two- or three-dimensional list represented across the cluster, like for matrices, above. It returns the portion of the Fourier-transformed array meant for that processor.

Parallel Disk I/O

Data needs to be read in and out of the cluster, but in such a way that the data is distributed across the cluster evenly. These calls perform these actions.

Call	Description
ParallelPut[expr, filename]	Puts expr into the file with the name filename in order on processor 0. The third argument specifies that the file be written on the processor whose ID is root. The fourth uses the communicator world comm.
ParallelPut[expr, filename, root]	
ParallelPut[expr, filename, root, comm]	

Call	Description
<p>ParallelGet[filename]</p> <p>ParallelGet[filename, root]</p> <p>ParallelGet[filename, root, comm]</p>	<p>Reads and returns data from the file with the name filename on processor 0 partitioned into each processor on the cluster. The second argument specifies that the file is to be read on the processor whose ID is root. The third uses the communicator world comm.</p>
<p>ParallelBinaryPut[expr, type, filename]</p> <p>ParallelBinaryPut[expr, filename, root]</p> <p>ParallelBinaryPut[expr, filename, root, comm]</p>	<p>Puts expr into the file with the binary format type with the name filename in order on processor 0. The fourth argument specifies that the file be written on the processor whose ID is root. The fifth uses the communicator world comm.</p>
<p>ParallelBinaryGet[type, filename]</p> <p>ParallelBinaryGet[type, filename, root]</p> <p>ParallelBinaryGet[type, filename, root, comm]</p>	<p>Reads and returns data in the binary format type from the file with the name filename on processor 0 partitioned into each processor on the cluster. The third argument specifies that the file is to be read on the processor whose ID is root. The fourth uses the communicator world comm.</p>
<p>ParallelPutPerProcessor[expr, filename]</p> <p>ParallelPutPerProcessor[expr, filename, root]</p> <p>ParallelPutPerProcessor[expr, filename, root, comm]</p>	<p>Puts expr into the file with the name filename in order on processor 0, one line per processor. The third argument specifies that the file be written on the processor whose ID is root. The fourth uses the communicator world comm.</p>
<p>ParallelGetPerProcessor [filename]</p> <p>ParallelGetPerProcessor [filename, root]</p> <p>ParallelGetPerProcessor [filename, root, comm]</p>	<p>Reads and returns data from the file with the name filename on processor 0, one line for each processor. The second argument specifies that the file is to be read on the processor whose ID is root. The third uses the communicator world comm.</p>

References

Reference materials

Texts used in the creation of this project include descriptions of the MPI standard and guides to parallel computing.

1. M. Snir, S. Otto, S. Huss-Lederman, D. Walker, J. Dongarra, *MPI-The Complete Reference*, second edition, MIT Press, Cambridge MA, 1998.
2. G. F. Pfister, *In Search of Clusters*, Prentice Hall, 1997.
3. V. K. Decyk, "How to Write (Nearly) Portable Fortran Programs for Parallel Computers", *Computers In Physics*, **7**, p. 418 (1993).
4. V. K. Decyk, "Skeleton PIC Codes for Parallel Computers", *Computers Physics Communications*, **87**, p. 87 (1995).

For additional information

Useful web sites for learning about parallel computing and techniques to use them are on this site:

<http://daugerresearch.com/vault/>

It includes links to eight articles on writing parallel code:

- Parallelization - introduces the basic issues when writing parallel code
- Parallel Zoology - compare and contrast the different parallel computing types
- Parallel Knock - exhibition of basic message-passing code
- Parallel Adder - tutorial on parallelizing a single-processor code of independent work
- Parallel Pascal's Triangle - tutorial on parallelizing propagation-style code requiring local communication
- Parallel Circle Pi - tutorial on creating a load-balancing code divisible into independent work
- Parallel Life - tutorial on parallelizing propagation-style code requiring two-dimensional local communication
- Visualizing Message-Passing - a tutorial on using a graphical monitor window to debug and optimize parallel code

as well as other publications on cluster computing.

Contact information

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